

Package ‘SimSurvNMarker’

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Type Package

Title Simulate Survival Time and Markers

Version 0.1.2

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Description Provides functions to simulate from joint survival and marker models. The user can specify all basis functions of time, random or deterministic covariates, random or deterministic left-truncation and right-censoring times, and model parameters.

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Encoding UTF-8

Suggests testthat (>= 2.1.0), splines, R.rsp, Matrix

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LinkingTo Rcpp, RcppArmadillo

Imports Rcpp

SystemRequirements C++11

VignetteBuilder R.rsp

URL <https://github.com/boennecd/SimSurvNMarker>

BugReports <https://github.com/boennecd/SimSurvNMarker/issues>

NeedsCompilation yes

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draw_U	<i>Samples from a Multivariate Normal Distribution</i>
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Description

Simulates from a multivariate normal distribution and returns a matrix with appropriate dimensions.

Usage

```
draw_U(Psi_chol, n_y)
```

Arguments

Psi_chol	Cholesky decomposition of the covariance matrix.
n_y	number of markers.

Examples

```
library(SimSurvNMarker)
set.seed(1)
n_y <- 2L
K <- 3L * n_y
Psi <- drop(rWishart(1, K, diag(K)))
Psi_chol <- chol(Psi)

# example
dim(draw_U(Psi_chol, n_y))
samples <- replicate(100, draw_U(Psi_chol, n_y))
samples <- t(apply(samples, 3, c))

colMeans(samples) # ~ zeroes
cov(samples) # ~ Psi
```

Description

Evaluates the marker mean given by

$$\vec{\mu}(s, \vec{u}) = \vec{\sigma} + B^T \vec{g}(s) + U^T \vec{m}(s).$$

Usage

```
eval_marker(ti, B, g_func, U, m_func, offset)
```

Arguments

ti	numeric vector with time points.
B	coefficient matrix for time-varying fixed effects. Use NULL if there is no effect.
g_func	basis function for B like poly .
U	random effects matrix for time-varying random effects. Use NULL if there is no effects.
m_func	basis function for U like poly .
offset	numeric vector with non-time-varying fixed effects.

Examples

```
# compare R version with this function
library(SimSurvNMarker)
set.seed(1)
n <- 100L
n_y <- 3L

ti <- seq(0, 1, length.out = n)
offset <- runif(n_y)
B <- matrix(runif(5L * n_y), nr = 5L)
g_func <- function(x)
  cbind(1, x, x^2, x^3, x^4)
U <- matrix(runif(3L * n_y), nr = 3L)
m_func <- function(x)
  cbind(1, x, x^2)

r_version <- function(ti, B, g_func, U, m_func, offset){
  func <- function(ti)
    drop(crossprod(B, drop(g_func(ti))) + crossprod(U, drop(m_func(ti))))

  vapply(ti, func, numeric(n_y)) + offset
}
```

```
# check that we get the same
stopifnot(isTRUE(all.equal(
  c(r_version (ti[1], B, g_func, U, m_func, offset)),
  eval_marker(ti[1], B, g_func, U, m_func, offset))))
stopifnot(isTRUE(all.equal(
  r_version (ti, B, g_func, U, m_func, offset),
  eval_marker(ti, B, g_func, U, m_func, offset))))

# check the computation time
system.time(replicate(100, r_version (ti, B, g_func, U, m_func, offset)))
system.time(replicate(100, eval_marker(ti, B, g_func, U, m_func, offset)))
```

eval_surv_base_fun *Evaluates the Survival Function without a Marker*

Description

Evaluates the survival function at given points where the hazard is given by

$$h(t) = \exp(\vec{\omega}^T \vec{b}(t) + \delta).$$

Usage

```
eval_surv_base_fun(ti, omega, b_func, gl_dat = get_gl_rule(30L), delta = NULL)
```

Arguments

ti	numeric vector with time points.
omega	numeric vector with coefficients for the baseline hazard.
b_func	basis function for the baseline hazard like poly .
gl_dat	Gauss–Legendre quadrature data. See get_gl_rule .
delta	offset on the log hazard scale. Use NULL if there is no effect.

Examples

```
# Example of a hazard function
b_func <- function(x)
  cbind(1, sin(2 * pi * x), x)
omega <- c(-3, 3, .25)
haz_fun <- function(x)
  exp(drop(b_func(x) %*% omega))

plot(haz_fun, xlim = c(0, 10))

# plot the hazard
library(SimSurvNMarker)
gl_dat <- get_gl_rule(60L)
```

```

plot(function(x) eval_surv_base_fun(ti = x, omega = omega,
                                   b_func = b_func, gl_dat = gl_dat),
      xlim = c(1e-4, 10), ylim = c(0, 1), bty = "l", xlab = "time",
      ylab = "Survival", yaxs = "i")

# using too few nodes gives a wrong result in this case!
gl_dat <- get_gl_rule(15L)
plot(function(x) eval_surv_base_fun(ti = x, omega = omega,
                                   b_func = b_func, gl_dat = gl_dat),
      xlim = c(1e-4, 10), ylim = c(0, 1), bty = "l", xlab = "time",
      ylab = "Survival", yaxs = "i")

```

get_gl_rule

Get Gauss–Legendre Quadrature Nodes and Weights

Description

Computes Gauss–Legendre Quadrature nodes and weights.

Usage

```
get_gl_rule(n)
```

Arguments

n number of nodes.

Examples

```

library(SimSurvNMarker)
get_gl_rule(4)
get_gl_rule(25)

# fast
system.time(replicate(10000, get_gl_rule(10)))
system.time(replicate(10000, get_gl_rule(100)))

```

get_ns_spline

Faster Pointwise Function than ns

Description

Creates a function which can evaluate a natural cubic spline like [ns](#).

The result may differ between different BLAS and LAPACK implementations as the QR decomposition is not unique. However, the column space of the returned matrix will always be the same regardless of the BLAS and LAPACK implementation.

Usage

```
get_ns_spline(knots, intercept = TRUE, do_log = TRUE)
```

Arguments

knots	sorted numeric vector with boundary and interior knots.
intercept	logical for whether to include an intercept.
do_log	logical for whether to evaluate the spline at $\log(x)$ or x .

Examples

```
# compare with splines
library(splines)
library(SimSurvNMarker)
xs <- seq(1, 5, length.out = 10L)
bks <- c(1, 5)
iks <- 2:4

# we get the same
if(require(Matrix)){
  r1 <- unclass(ns(xs, knots = iks, Boundary.knots = bks, intercept = TRUE))
  r2 <- get_ns_spline(knots = sort(c(iks, bks)), intercept = TRUE,
                    do_log = FALSE)(xs)

  cat("Rank is correct:      ", rankMatrix(cbind(r1, r2)) == NCOL(r1), "\n")

  r1 <- unclass(ns(log(xs), knots = log(iks), Boundary.knots = log(bks),
                  intercept = TRUE))
  r2 <- get_ns_spline(knots = log(sort(c(iks, bks))), intercept = TRUE,
                    do_log = TRUE)(xs)
  cat("Rank is correct (log):", rankMatrix(cbind(r1, r2)) == NCOL(r1), "\n")
}

# the latter is faster
system.time(
  replicate(100,
            ns(xs, knots = iks, Boundary.knots = bks, intercept = TRUE)))
system.time(
  replicate(100,
            get_ns_spline(knots = sort(c(iks, bks)), intercept = TRUE,
                          do_log = FALSE)(xs)))
func <- get_ns_spline(knots = sort(c(iks, bks)), intercept = TRUE,
                      do_log = FALSE)
system.time(replicate(100, func(xs)))
```

sim_joint_data_set *Simulate Individuals from a Joint Survival and Marker Model*

Description

Simulates individuals from the following model

$$\vec{U}_i \sim N^{(K)}(\vec{0}, \Psi)$$

$$\vec{Y}_{ij} | \vec{U}_i = \vec{u}_i \sim N^{(r)}(\vec{\mu}_i(s_{ij}, \vec{u}_i), \Sigma)$$

$$h(t | \vec{u}) = \exp(\vec{\omega}^\top \vec{b}(t) + \vec{\delta}^\top \vec{z}_i + \vec{1}^\top (\text{diag}(\vec{\alpha}) \otimes \vec{x}_i^\top) \text{vec}(\Gamma) + \vec{1}^\top (\text{diag}(\vec{\alpha}) \otimes \vec{g}(t)^\top) \text{vec}(B) + \vec{1}^\top (\text{diag}(\vec{\alpha}) \otimes \vec{m}(t)^\top) \vec{u})$$

with

$$\vec{\mu}_i(s, \vec{u}) = (I \otimes \vec{x}_i^\top) \text{vec}(\Gamma) + (I \otimes \vec{g}(s)^\top) \text{vec}(B) + (I \otimes \vec{m}(s)^\top) \vec{u}$$

where $h(t | \vec{u})$ is the conditional hazard function.

Usage

```
sim_joint_data_set(
  n_obs,
  B,
  Psi,
  omega,
  delta,
  alpha,
  sigma,
  gamma,
  b_func,
  m_func,
  g_func,
  r_z,
  r_left_trunc,
  r_right_cens,
  r_n_marker,
  r_x,
  r_obs_time,
  y_max,
  use_fixed_latent = TRUE,
  m_func_surv = m_func,
  g_func_surv = g_func,
  gl_dat = get_gl_rule(30L),
  tol = .Machine$double.eps^(1/4)
)
```

Arguments

n_obs	integer with the number of individuals to draw.
B	coefficient matrix for time-varying fixed effects. Use NULL if there is no effect.
Psi	the random effects' covariance matrix.
omega	numeric vector with coefficients for the baseline hazard.
delta	coefficients for fixed effects in the log hazard.
alpha	numeric vector with association parameters.
sigma	the noise's covariance matrix.
gamma	coefficient matrix for the non-time-varying fixed effects. Use NULL if there is no effect.
b_func	basis function for the baseline hazard like poly .
m_func	basis function for U like poly .
g_func	basis function for B like poly .
r_z	generator for the covariates in the log hazard. Takes an integer for the individual's id.
r_left_trunc	generator for the left-truncation time. Takes an integer for the individual's id.
r_right_cens	generator for the right-censoring time. Takes an integer for the individual's id.
r_n_marker	function to generate the number of observed markers. Takes an integer for the individual's id.
r_x	generator for the covariates in for the markers. Takes an integer for the individual's id.
r_obs_time	function to generate the observations times given the number of observed markers. Takes an integer for the number of markers and an integer for the individual's id.
y_max	maximum survival time before administrative censoring.
use_fixed_latent	logical for whether to include the $\bar{\Gamma}^T (\text{diag}(\vec{\alpha}) \otimes \vec{x}_i^T) \text{vec}(\Gamma)$ term in the log hazard. Useful if derivatives of the latent mean should be used.
m_func_surv	basis function for U like poly in the log hazard. Can be different from m_func. Useful if derivatives of the latent mean should be used.
g_func_surv	basis function for B like poly in the log hazard. Can be different from g_func. Useful if derivatives of the latent mean should be used.
gl_dat	Gauss-Legendre quadrature data. See get_gl_rule .
tol	convergence tolerance passed to uniroot .

See Also

See the examples on Github at <https://github.com/boennecd/SimSurvNMarker/tree/master/inst/test-data> or this vignette `vignette("SimSurvNMarker", package = "SimSurvNMarker")`.
[sim_marker](#) and [surv_func_joint](#)

Examples

```
#####
# example with polynomial basis functions
b_func <- function(x){
  x <- x - 1
  cbind(x^3, x^2, x)
}
g_func <- function(x){
  x <- x - 1
  cbind(x^3, x^2, x)
}
m_func <- function(x){
  x <- x - 1
  cbind(x^2, x, 1)
}

# parameters
delta <- c(-.5, -.5, .5)
gamma <- matrix(c(.25, .5, 0, -.4, 0, .3), 3, 2)
omega <- c(1.4, -1.2, -2.1)
Psi <- structure(c(0.18, 0.05, -0.05, 0.1, -0.02, 0.06, 0.05, 0.34, -0.25,
                  -0.06, -0.03, 0.29, -0.05, -0.25, 0.24, 0.04, 0.04,
                  -0.12, 0.1, -0.06, 0.04, 0.34, 0, -0.04, -0.02, -0.03,
                  0.04, 0, 0.1, -0.08, 0.06, 0.29, -0.12, -0.04, -0.08,
                  0.51), .Dim = c(6L, 6L))
B <- structure(c(-0.57, 0.17, -0.48, 0.58, 1, 0.86), .Dim = 3:2)
sig <- diag(c(.6, .3)^2)
alpha <- c(.5, .9)

# generator functions
r_n_marker <- function(id)
  # the number of markers is Poisson distributed
  rpois(1, 10) + 1L
r_obs_time <- function(id, n_markes)
  # the observations times are uniform distributed
  sort(runif(n_markes, 0, 2))
r_z <- function(id)
  # return a design matrix for a dummy setup
  cbind(1, (id %% 3) == 1, (id %% 3) == 2)
r_x <- r_z # same covariates for the fixed effects
r_left_trunc <- function(id)
  # no left-truncation
  0
r_right_cens <- function(id)
  # right-censoring time is exponentially distributed
  rexp(1, rate = .5)

# simulate
gl_dat <- get_gl_rule(30L)
y_max <- 2
n_obs <- 100L
set.seed(1)
```

```

dat <- sim_joint_data_set(
  n_obs = n_obs, B = B, Psi = Psi, omega = omega, delta = delta,
  alpha = alpha, sigma = sig, gamma = gamma, b_func = b_func,
  m_func = m_func, g_func = g_func, r_z = r_z, r_left_trunc = r_left_trunc,
  r_right_cens = r_right_cens, r_n_marker = r_n_marker, r_x = r_x,
  r_obs_time = r_obs_time, y_max = y_max)

# checks
stopifnot(
  NROW(dat$survival_data) == n_obs,
  NROW(dat$marker_data) >= n_obs,
  all(dat$survival_data$y <= y_max))

```

sim_marker

Simulate a Number of Observed Marker for an Individual

Description

Simulates from

$$\vec{U}_i \sim N^{(K)}(\vec{0}, \Psi)$$

$$\vec{Y}_{ij} | \vec{U}_i = \vec{u}_i \sim N^{(r)}(\vec{\mu}(s_{ij}, \vec{u}_i), \Sigma)$$

with

$$\vec{\mu}(s, \vec{u}) = \vec{o} + (I \otimes \vec{g}(s)^\top) \text{vec}(B) + (I \otimes \vec{m}(s)^\top) \vec{u}.$$

The number of observations and the observations times, s_{ij} s, are determined from the passed generating functions.

Usage

```

sim_marker(
  B,
  U,
  sigma_chol,
  r_n_marker,
  r_obs_time,
  m_func,
  g_func,
  offset,
  id = 1L
)

```

Arguments

B	coefficient matrix for time-varying fixed effects. Use NULL if there is no effect.
U	random effects matrix for time-varying random effects. Use NULL if there is no effects.
sigma_chol	Cholesky decomposition of the noise's covariance matrix.
r_n_marker	function to generate the number of observed markers. Takes an integer for the individual's id.
r_obs_time	function to generate the observations times given the number of observed markers. Takes an integer for the number of markers and an integer for the individual's id.
m_func	basis function for U like poly .
g_func	basis function for B like poly .
offset	numeric vector with non-time-varying fixed effects.
id	integer with id passed to r_n_marker and r_obs_time.

See Also

[draw_U](#), [eval_marker](#)

Examples

```
#####
# example with polynomial basis functions
g_func <- function(x){
  x <- x - 1
  cbind(x^3, x^2, x)
}
m_func <- function(x){
  x <- x - 1
  cbind(x^2, x, 1)
}

# parameters
gamma <- matrix(c(.25, .5, 0, -.4, 0, .3), 3, 2)
Psi <- structure(c(0.18, 0.05, -0.05, 0.1, -0.02, 0.06, 0.05, 0.34, -0.25,
-0.06, -0.03, 0.29, -0.05, -0.25, 0.24, 0.04, 0.04,
-0.12, 0.1, -0.06, 0.04, 0.34, 0, -0.04, -0.02, -0.03,
0.04, 0, 0.1, -0.08, 0.06, 0.29, -0.12, -0.04, -0.08,
0.51), .Dim = c(6L, 6L))
B <- structure(c(-0.57, 0.17, -0.48, 0.58, 1, 0.86), .Dim = 3:2)
sig <- diag(c(.6, .3)^2)

# generator functions
r_n_marker <- function(id){
  cat(sprintf("r_n_marker: passed id is %d\n", id))
  # the number of markers is Poisson distributed
  rpois(1, 10) + 1L
}
```

```

r_obs_time <- function(id, n_markes){
  cat(sprintf("r_obs_time: passed id is %d\n", id))
  # the observations times are uniform distributed
  sort(runif(n_markes, 0, 2))
}

# simulate marker
set.seed(1)
U <- draw_U(chol(Psi), NCOL(B))
sim_marker(B = B, U = U, sigma_chol = chol(sig), r_n_marker = r_n_marker,
           r_obs_time = r_obs_time, m_func = m_func, g_func = g_func,
           offset = NULL, id = 1L)

```

surv_func_joint	<i>Evaluates the Conditional Survival Function Given the Random Effects</i>
-----------------	---

Description

Evaluates the conditional survival function given the random effects, \vec{U} . The conditional hazard function is

$$h(t | \vec{u}) = \exp(\vec{\omega}^\top \vec{b}(t) + \delta + \vec{\alpha}^\top \vec{\sigma} + \vec{1}^\top (\text{diag}(\vec{\alpha}) \otimes \vec{g}(t)^\top) \text{vec}(B) + \vec{1}^\top (\text{diag}(\vec{\alpha}) \otimes \vec{m}(t)^\top) \vec{u}).$$

Usage

```

surv_func_joint(
  ti,
  B,
  U,
  omega,
  delta,
  alpha,
  b_func,
  m_func,
  gl_dat = get_gl_rule(30L),
  g_func,
  offset
)

```

Arguments

ti	numeric vector with time points.
B	coefficient matrix for time-varying fixed effects. Use NULL if there is no effect.
U	random effects matrix for time-varying random effects. Use NULL if there is no effects.

omega	numeric vector with coefficients for the baseline hazard.
delta	offset on the log hazard scale. Use NULL if there is no effect.
alpha	numeric vector with association parameters.
b_func	basis function for the baseline hazard like poly .
m_func	basis function for U like poly .
gl_dat	Gauss–Legendre quadrature data. See get_gl_rule .
g_func	basis function for B like poly .
offset	numeric vector with non-time-varying fixed effects.

See Also

[sim_marker](#), [draw_U](#), [eval_surv_base_fun](#)

Examples

```
#####
# example with polynomial basis functions
b_func <- function(x){
  x <- x - 1
  cbind(x^3, x^2, x)
}
g_func <- function(x){
  x <- x - 1
  cbind(x^3, x^2, x)
}
m_func <- function(x){
  x <- x - 1
  cbind(x^2, x, 1)
}

# parameters
omega <- c(1.4, -1.2, -2.1)
Psi <- structure(c(0.18, 0.05, -0.05, 0.1, -0.02, 0.06, 0.05, 0.34, -0.25,
  -0.06, -0.03, 0.29, -0.05, -0.25, 0.24, 0.04, 0.04,
  -0.12, 0.1, -0.06, 0.04, 0.34, 0, -0.04, -0.02, -0.03,
  0.04, 0, 0.1, -0.08, 0.06, 0.29, -0.12, -0.04, -0.08,
  0.51), .Dim = c(6L, 6L))
B <- structure(c(-0.57, 0.17, -0.48, 0.58, 1, 0.86), .Dim = 3:2)
alpha <- c(.5, .9)

# simulate and draw survival curve
gl_dat <- get_gl_rule(30L)
set.seed(1)
U <- draw_U(chol(Psi), NCOL(B))
tis <- seq(0, 2, length.out = 100)
Survs <- surv_func_joint(ti = tis, B = B, U = U, omega = omega,
  delta = NULL, alpha = alpha, b_func = b_func,
  m_func = m_func, gl_dat = gl_dat, g_func = g_func,
  offset = NULL)
par_old <- par(mar = c(5, 5, 1, 1))
```

```
plot(tis, Survs, xlab = "Time", ylab = "Survival", type = "l",  
      ylim = c(0, 1), bty = "n", xaxs = "i", yaxs = "i")  
par(par_old)
```

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