

Package ‘TRMF’

August 16, 2021

Type Package

Title Temporally Regularized Matrix Factorization

Version 0.1.5

Author Chad Hammerquist [aut, cre],
Scentsy Inc [cph]

Maintainer Chad Hammerquist <chammerquist@scentsy.com>

Description Functions to estimate temporally regularized matrix factorizations (TRMF) for forecasting and imputing values in short but high-dimensional time series. Uses regularized alternating least squares to compute the factorization, allows for several types of constraints on matrix factors and natively handles weighted and missing data.

License GPL-3

Encoding UTF-8

Imports Matrix(>= 1.3-3),limSolve,generics

Suggests magrittr, knitr,rmarkdown

VignetteBuilder knitr

RoxygenNote 7.1.1

NeedsCompilation no

Repository CRAN

Date/Publication 2021-08-16 16:20:06 UTC

R topics documented:

coef.TRMF	2
components.TRMF	3
create_TRMF	4
fitted.TRMF	5
impute_TRMF	6
NormalizeMatrix	7
plot.TRMF	8
predict.TRMF	9
residuals.TRMF	10

retrain	11
summary.TRMF	12
train.TRMF	13
TRMF_ar	14
TRMF_columns	15
TRMF_es	17
TRMF_regression	18
TRMF_seasonal	20
TRMF_simple	21
TRMF_trend	22

Index	25
--------------	-----------

coef . TRMF	<i>Extract TRMF Coefficients (Fm)</i>
-------------	---------------------------------------

Description

Returns the Fm (transposed) matrix from the matrix factorization $X_m * F_m$.

Usage

```
## S3 method for class 'TRMF'
coef(object, ...)
```

Arguments

object	a trained TRMF object.
...	other arguments.

Value

the coefficient matrix, $t(F_m)$

Author(s)

Chad Hammerquist

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#)

Examples

```
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
coef(out)
```

components.TRMF	<i>Access TRMF factors</i>
-----------------	----------------------------

Description

This function returns the factors (Xm, Fm) from a trained TRMF object

Usage

```
## S3 method for class 'TRMF'
components(object, XorF = c("Xm", "Fm"), ...)
```

Arguments

object	trained TRMF object
XorF	which factor to return
...	ignored

Details

Returns the matrix factors. Could also use `object$Factors$Xm`, `object$Factors$Fm`. If matrix normalization was used in `create_TRMF`, `Xm%%Fm` could look much different than the input data matrix.

Value

A matrix.

Author(s)

Chad Hammerquist

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#)

Examples

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(rnorm(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
plot(out)
components(out, "Xm")
```

create_TRMF	<i>Create a TRMF object</i>
-------------	-----------------------------

Description

Creates a TRMF object from a data matrix. This function is always needed to initialize a TRMF model.

Usage

```
create_TRMF(dataM, weight = 1,
            normalize = c("none", "standard", "robust", "range"),
            normalize.type = c("global", "columnwise", "rowwise"),
            na.action = c("impute", "fail"))
```

Arguments

dataM	The data matrix, each column represents a time series.
weight	An optional matrix of weights to be used in the fitting process. If used, $\sum(w^2 * e^2)$ is minimized.
normalize	Type of scaling/centering for the data. Recommended to reduce bias when using regularization. none does nothing, standard centers with mean, and scales by <code>sd()</code> , robust centers with the median and scales by <code>mad(, constant=1)</code> , range maps to $[-1, 1]$ interval
normalize.type	how should normalization be applied. global scales and centers matrix by one value. columnwise and rowwise normalize each column or row separately.
na.action	what action to take when data contains NAs

Details

This function doesn't do any computation, it is the entry point for creating a TRMF model. To train the model or add additional details, see examples. Normalization is recommended in general. Regularization biases the factorization toward zero a little bit, centering changes that to bias towards

the mean. Scaling makes the choosing of regularization parameters easier. If the factorization is to be used for forward forecasting, rowwise normalization is not recommended as it could remove some temporal information.

Value

create_TRMF returns an object of `class` "TRMF" to be passed to other TRMF functions.

Author(s)

Chad Hammerquist

References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

See Also

[train.TRMF](#), [TRMF_columns](#), [TRMF_trend](#)

Examples

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%*%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj, reg_type = "interval")
obj = TRMF_trend(obj, numTS=4, order=2)
out = train(obj)
plot(out)
```

fitted.TRMF

Extract TRMF fitted values.

Description

A function to extract fitted values from a trained TRMF object.

Usage

```
## S3 method for class 'TRMF'
fitted(object, impute = FALSE, ...)
```

Arguments

object a trained TRMF object.
impute logical, should imputed values be returned?
... other arguments.

Value

Fitted values extracted from object. If `impute` is TRUE then entire fitted (unscaled and uncentered) matrix is returned, otherwise there are NAs in the same locations as the time series matrix.

Author(s)

Chad Hammerquist

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#)

Examples

```
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
fitted(out)
```

impute_TRMF

Impute missing values in a matrix

Description

Impute missing values in matrix from a pre-trained TRMF object.

Usage

```
impute_TRMF(obj)
```

Arguments

obj a trained TRMF object

Details

Essentially an accessor function. Replaces the missing values in data matrix with values from the fitted TRMF object.

Value

data matrix with missing values imputed

Author(s)

Chad Hammerquist

References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

See Also

[train.TRMF](#), [create_TRMF](#), [TRMF_trend](#)

Examples

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(rnorm(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)
Am[sample.int(210, 20)] = NA

# create model
obj = create_TRMF(Am)
obj = TRMF_trend(obj, numTS=4, order=2)
out = train(obj)
impute_TRMF(out)
```

NormalizeMatrix

Matrix Scaling

Description

A function for normalizing (scaling and centering) a matrix.

Usage

```
NormalizeMatrix(X, method = c("standard", "robust", "range", "none"),
               type = c("global", "rowwise", "columnwise"), na.rm = TRUE)
```

Arguments

<code>x</code>	a numeric matrix(like object)
<code>method</code>	type of scaling to perform, standard centers with mean, and scales by <code>sd()</code> , robust centers with the median and scales by <code>mad(, constant=1)</code> , range maps to <code>[0-1]</code> interval
<code>type</code>	how should normalization be applied. <code>global</code> scales and centers matrix by one value. <code>columnwise</code> and <code>rowwise</code> normalize each column or row separately.
<code>na.rm</code>	logical value, ignore NA values or not.

Details

Scaling and centering quantities are stored as attributes.

Value

The possibly centered and scaled matrix. Scaling and centering quantities are stored as attributes.

Author(s)

Chad Hammerquist

Examples

```
x = matrix(1:10, ncol = 2)
NormalizeMatrix(x)
```

plot.TRMF

Plot Latent Time Series for a TRMF Object

Description

Plots all the time series in `Xm` from a trained TRMF object.

Usage

```
## S3 method for class 'TRMF'
plot(x, ...)
```

Arguments

<code>x</code>	a trained TRMF object.
<code>...</code>	ignored.

Value

No return value, called for side effects

Author(s)

Chad Hammerquist

See Also[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#)**Examples**

```

xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
plot(out)

```

predict.TRMF

*Predict method for TRMF model fit***Description**

Predict values based on the TRMF fit

Usage

```

## S3 method for class 'TRMF'
predict(object, newdata=NULL, ...)

```

Arguments

object	A trained TRMF object
newdata	A list with slot X_m and possibly with slots cX_{reg} and gX_{reg}
...	other arguments, ignored.

Details

If newdata is NULL, returns fitted model. If newdata doesn't have the term X_m or if it has a different number of columns than the number of latent time series, it will throw an error. If the object also contains a global regression, gX_{reg} must be present and appropriately sized. If the object also contains a column-wise regression, cX_{reg} must be present and appropriately sized.

Value

Returns a matrix of predictions.

Author(s)

Chad Hammerquist

See Also[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#), [train.TRMF](#)**Examples**

```
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
fitted(out)
newXm = 1:5
predict(out, newdata=list(Xm=newXm))
```

`residuals.TRMF`*Extract TRMF residuals*

Description

A function to extract residuals from a trained TRMF object.

Usage

```
## S3 method for class 'TRMF'
residuals(object, ...)
```

Arguments

<code>object</code>	a trained TRMF object.
<code>...</code>	ignored

Value

residuals extracted from TRMF object

Author(s)

Chad Hammerquist

See Also[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#)

Examples

```
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
resid(out)
```

retrain	<i>Retrain TRMF objects.</i>
---------	------------------------------

Description

Continue training on a pretrained TRMF object.

Usage

```
retrain(obj, numit, fit_xm_first = TRUE)
```

Arguments

obj	Pretrained TRMF object
numit	Number of training iterations
fit_xm_first	Fit the Xm factor first? This could be useful if modifications are made to one of the factors that we don't want to be overwritten.

Details

This is basically the same function as `train()` but it doesn't create any of the constraint matrices and doesn't do any initialization.

Value

A trained TRMF object.

See Also

[train.TRMF](#)

Examples

```
# create test data
tm = 3*poly(x = (-20:20)/10,degree=3)
sm = diffinv(rnorm(29,0,.1),lag=12,xi=(-5:6)/6)
xm = cbind(sm,tm)
fm = matrix(runif(40),4,10)
Am = xm%*%fm+rnorm(410,0,.1)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj,reg_type = "interval")
obj = TRMF_trend(obj,numTS=3,order=2)
obj = TRMF_seasonal(obj,numTS=1,freq=12,lambdaD=5)

# train
out = train(obj,numit=0) # initialize
plot(out)
new_out = retrain(out,numit=10)
plot(new_out)
```

summary.TRMF

Summarize TRMF

Description

summary method for class "TRMF"

Usage

```
## S3 method for class 'TRMF'
summary(object, ...)
```

Arguments

object	TRMF object.
...	other arguments.

Value

NULL

Author(s)

Chad Hammerquist

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#)

Examples

```

xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%*%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
summary(obj)
summary(out)

```

train.TRMF	<i>Train a TRMF model</i>
------------	---------------------------

Description

This function is the "engine" of the TRMF package. It takes a previously created TRMF object and fits it to the data using an alternating least squares algorithm.

Usage

```

## S3 method for class 'TRMF'
train(x, numit = 10, ...)

```

Arguments

x	A TRMF object to be fit.
numit	Number of alternating least squares iterations
...	ignored

Details

If a coefficient model is not present in object, it adds a L2 regularization model. If no time series models have been added to object, it adds a simple model using [TRMF_simple](#).

Value

train returns a fitted object of `class` "TRMF" that contains the data, all added models, matrix factorization and fitted model. The matrix factors X_m , F_m are stored in `object$Factors$Xm` and `object$Factors$Fm` respectively. Use `fitted` to get fitted model, use `resid` to get residuals, use `coef` to get coefficients (F_m matrix) and `components` to get X_m or F_m .

Author(s)

Chad Hammerquist

References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#)

Examples

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(rnorm(40), 4, 10)
Am = xm%*%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
plot(out)
```

TRMF_ar

Add an Auto-Regressive Regularization Model to a TRMF Object.

Description

Creates a regularization scheme that constrains latent time-series based on auto-regressive parameters and adds it to a TRMF object. In matrix optimization form, it adds the following term to the TRMF cost function: $R(x) = \lambda D^2 \|w(DX_s)\|^2 + \lambda A^2 \|X_s\|^2$ where X_s is sub-set of the X_m matrix controlled by this model and D is a matrix that corresponds to an auto-regressive model.

Usage

```
TRMF_ar(obj, numTS = 1, AR, lambdaD=1, lambdaA=0.0001, weight=1)
```

Arguments

obj	A TRMF object
numTS	number of latent time series in this model
lambdaD	regularization parameter for temporal constraint matrix
lambdaA	regularization parameter to apply simple L2 regularization to this time series model
weight	optional vector of weights to weight constraints, i.e. $R(x) = \lambda D^2 * \ w*(D\%*\%X)\ ^2$
AR	vector of autoregressive parameters. No checks are performed

Details

Setting `AR = c(1)` gives a random walk model, same as `TRMF_trend(..., order=1)`

Value

Returns an updated object of class `TRMF`.

Author(s)

Chad Hammerquist

References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#)

Examples

```
# create test data
xm = matrix(rnorm(80), 20, 4)
fm = matrix(rnorm(40), 4, 10)+1
Am = xm%%fm+rnorm(200, 0, .1)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj, reg_type = "interval")
obj = TRMF_ar(obj, numTS=2, AR=c(0.5), lambdaD=4)
out = train(obj)
plot(out)
```

TRMF_columns

Add a column regularization model to TRMF object

Description

Adds a regularization model to `TRMF` object created by `create_TRMF()` to constrain the fitting process of the coefficient matrix.

`TRMF_coefficient` is a (soon to be deprecated) alias for `TRMF_columns`.

Usage

```
TRMF_columns(obj,
  reg_type = c("l2", "nnls", "constrain", "interval", "none"), lambda = 0.0001)
TRMF_coefficients(obj,
  reg_type = c("l2", "nnls", "constrain", "interval", "none"), lambda = 0.0001)
```

Arguments

obj	TRMF object created by <code>create_TRMF()</code>
reg_type	regularization type to apply when fitting TRMF model. l2 regularizes by simple sum of squares, nnls forces coefficients to be non-negative. constrain constrains coefficients to be non-negative and to sum to 1. interval constrains coefficients to the interval [0-1]
lambda	L2 regularization parameter used for all regularization types. If NULL, uses lambda set in <code>create_TRMF()</code> .

Details

This function doesn't do any computations, it just sets up regularization parameters for the coefficient matrix. This function should only be called once on a TRMF object. If called twice, it will overwrite previous model with a warning.

Value

Returns an updated object of class TRMF.

Author(s)

Chad Hammerquist

References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

See Also

[train.TRMF](#), [create_TRMF](#), [TRMF_trend](#)

Examples

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(abs(rnorm(40)), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj, reg_type = "nnls")
```



```
out = train(obj)
plot(out)
```

TRMF_es

Add exponential smoothing regularization model to a TRMF object.

Description

Creates a regularization scheme that favors exponentially smoothed solutions and adds it to a TRMF object. In matrix optimization form, it adds the following term to the TRMF cost function: $R(x) = \lambda D^2 \|w(DX_s)\|^2 + \lambda A^2 \|X_s\|^2$ where X_s is sub-set of the X_m matrix controlled by this model and D is a matrix with weights from exponential smoothing.

Usage

```
TRMF_es(obj, numTS = 1, alpha=1, es_type=c("single", "double"),
        lambdaD=1, lambdaA=0.0001, weight=1)
```

Arguments

obj	A TRMF object
numTS	number of latent time series in this model
lambdaD	regularization parameter for temporal constraint matrix
lambdaA	regularization parameter to apply simple L2 regularization to this time series model
weight	optional vector of weights to weight constraint, i.e. $R(x) = \lambda D^2 \ w*(D\%*\%X)\ ^2$
es_type	type of exponential smoothing. "double" does Brown's double exponential smoothing.
alpha	exponential smoothing parameter, constrained to be in the interval [0,1]

Details

This creates a non-sparse constraint matrix which could slow training down for longer time series.

Value

Returns an updated object of class TRMF.

Author(s)

Chad Hammerquist

References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

https://en.wikipedia.org/wiki/Exponential_smoothing

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#), [TRMF_seasonal](#)

Examples

```
# create test data
xm = cbind(cumsum(rnorm(20)), cumsum(rnorm(20)))
fm = matrix(runif(20), 2, 10)
Am = xm%*%fm+rnorm(200, 0, .2)

# create model
obj = create_TRMF(Am)
obj = TRMF_es(obj, numTS=2, alpha=0.5)
out = train(obj)
plot(out)
```

TRMF_regression

Add external regressors to TRMF object

Description

A function to add external regressors to a TRMF object.

Usage

```
TRMF_regression(obj, Xreg, type = c("global", "columnwise"))
```

Arguments

obj	TRMF object created by <code>create_TRMF()</code>
Xreg	Vector or matrix of external regressors. If <code>type = "columnwise"</code> , Xreg can be a matrix or array, but the first two dimensions must match those of the data matrix.
type	how are the regressors added to the model. If <code>type = "global"</code> the matrix factorization includes all the regressors. If <code>type = "columnwise"</code> each column in the data matrix is regressed of the corresponding column of Xreg.

Details

The coefficients model for the regressors are subject to the same regularization as the rest of the matrix factorization. Only one columnwise and one global model should be used in the same model. Both types can be include in the same model though.

Value

Returns an updated object of class TRMF.

Author(s)

Chad Hammerquist

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_trend](#)

Examples

```
# ~ Global regression example ~
# create test data
bb = (-10:10)/10
xReg = 10*cos(bb*10)
xm = poly(x = bb,degree=3)
fm = matrix(rnorm(40),4,10)
Am = cbind(xReg,xm)%*%fm+rnorm(210,0,.2)

# creat model and fit
obj = create_TRMF(Am)
obj = TRMF_trend(obj,numTS=3,order=2)
obj = TRMF_regression(obj,Xreg=xReg,type="global")
out = train(obj)
plot(out)

# ~ columnwise regression example ~
# create test data
bb = (-10:10)/10
xm = poly(x = bb,degree=4)
fm = matrix(rnorm(84),4,21)
Am = xm%*%fm+rnorm(441,0,.2)

layers = array(0,dim=c(21,21,2))
layers[, ,1] = 2*cos(2*bb)%o%sin(4*bb)
layers[, ,2] = 2*sqrt(abs(bb%o%bb))
nAm = Am+layers[, ,1]+layers[, ,2]

# creat model and fit
obj = create_TRMF(nAm)
obj = TRMF_trend(obj,numTS=4,order=2)
obj = TRMF_regression(obj,Xreg=layers,type="columnwise")
out = train(obj)
plot(out)
```

TRMF_seasonal	<i>Add seasonal regularization model to a TRMF object</i>
---------------	---

Description

Creates a regularization scheme that favors seasonally varying solutions and adds it to a TRMF object. In matrix optimization form, it adds the following term to the TRMF cost function: $R(x) = \lambda D^2 \|w(DX_s)\|^2 + \lambda A^2 \|X_s\|^2$ where X_s is sub-set of the X_m matrix controlled by this model and D is a (with a lag of freq) finite difference matrix.

Usage

```
TRMF_seasonal(obj, numTS = 1, freq = 12, sumFirst=FALSE, lambdaD=1, lambdaA=0.0001, weight=1)
```

Arguments

obj	A TRMF object
numTS	number of latent time series in this model
lambdaD	regularization parameter for temporal constraint matrix
lambdaA	regularization parameter to apply simple L2 regularization to this time series model
weight	optional vector of weights to weight constraints, i.e. $R(x) = \lambda D^2 \ w(D\%*X)\ ^2$
freq	The frequency of the seasonal time series model. Minimize the differences of lag = freq
sumFirst	minimize the sum of first freq elements in time series

Details

TRMF_seasonal(freq=N) fits a lag N random walk. For monthly data, use freq=12, for quarterly data, freq=4. If sumFirst = TRUE, the sum of the first freq elements in the latent time series are also minimized. This can be used to help force the seasonal component to vary around a zero mean.

Value

Returns an updated object of class TRMF.

Author(s)

Chad Hammerquist

References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_simple](#), [TRMF_trend](#)

Examples

```
# create test data
tm = 3*poly(x = (-20:20)/10,degree=3)
sm = diffinv(rnorm(29,0,.1),lag=12,xi=(-5:6)/6)
xm = cbind(sm,tm)
fm = matrix(runif(40),4,10)
Am = xm%*%fm+rnorm(410,0,.1)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj,reg_type = "interval")
obj = TRMF_trend(obj,numTS=3,order=2)
obj = TRMF_seasonal(obj,numTS=1,freq=12,lambdaD=5)
out = train(obj)
plot(out)
```

TRMF_simple

Add L2 regularization model to a TRMF object

Description

Creates an L2 regularization and adds it to a TRMF object. In matrix optimization form, it adds the following term to the TRMF cost function: $R(x) = \lambda A^2 ||w(X_s)||^2$ where X_s is sub-set of the X_m matrix controlled by this model.

Usage

```
TRMF_simple(obj,numTS = 1,lambdaA=0.0001,weight=1)
```

Arguments

obj	A TRMF object
numTS	number of latent time series in this model
lambdaA	regularization parameter to apply simple L2 regularization to this time series model
weight	optional vector of weights to weight constraints, i.e. $R(x) = \lambda A^2 * w * X ^2$

Details

This is called by `train_TRMF` if the TRMF object doesn't have any time series models.

Value

Returns an updated object of class TRMF.

Author(s)

Chad Hammerquist

References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_seasonal](#), [TRMF_trend](#)

Examples

```
# create test data
xm = matrix(rnorm(160),40,4)
fm = matrix(runif(40),4,10)
Am = xm%%fm+rnorm(400,0,.1)

# create model
obj = create_TRMF(Am)
obj = TRMF_simple(obj,numTS=4,lambdaA=0.1)
out = train(obj)
plot(out)
```

TRMF_trend

Add Trend Model to a TRMF Object

Description

Creates a regularization scheme that favors trend-like solutions and adds it to a TRMF object. In matrix optimization form, it adds the following term to the TRMF cost function: $R(x) = \lambda D^2 \|w(DX_s)\|^2 + \lambda A^2 \|X_s\|^2$ where X_s is sub-set of the X_m matrix controlled by this model and D is a finite difference matrix.

Usage

```
TRMF_trend(obj,numTS = 1,order = 1,lambdaD=1,lambdaA=0.0001,weight=1)
```

Arguments

obj	A TRMF object
numTS	number of latent time series in this model
order	The order of derivative for finite difference constraint matrix. Fractionally and negative values allowed.
lambdaD	regularization parameter for temporal constraint matrix
lambdaA	regularization parameter to apply simple L2 regularization to this time series model
weight	optional vector of weights to weight constraints, i.e. $R(x) = \lambda D^2 * \ w * (D * X)\ ^2$

Details

An arbitrary number of time series models can be added. `TRMF_trend(order = 1)` fits a random walk. `TRMF_trend(order = 2)` fits a cubic smoothing spline. For a single time series, `TRMF_trend(order = 2)` is basically equivalent to the Hodge-Prescot filter. A fractional value for order minimizes a squared fractional derivative. A negative value minimizes a (possibly fractional order) squared integral of time-series. Using a fractional or negative order for `TRMF_trend` or using `TRMF_es` could drastically reduce the sparsity of constraint matrix and slow down training. Fractional or negative order has only been lightly tested, so use with care.

Value

Returns an updated object of class TRMF.

Author(s)

Chad Hammerquist

References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

See Also

[create_TRMF](#), [TRMF_columns](#), [TRMF_simple](#), [TRMF_seasonal](#)

Examples

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm*%*fm+rnorm(210, 0, .1)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj, reg_type = "interval")
```

```
obj = TRMF_trend(obj,numTS=4,order=2,lambdaD=2)
out = train(obj)
plot(out)

# more complex model
require(magrittr) # for pipes

obj = create_TRMF(Am)%>%
  TRMF_columns(reg_type = "interval")%>%
  TRMF_trend(numTS=2,order=1,lambdaD=4)%>%
  TRMF_trend(numTS=2,order=2,lambdaD=4)%>%
  TRMF_trend(numTS=1,order=1.5)

out = train(obj)
plot(out)
```


Index

class, [5](#), [13](#)
coef, [13](#)
coef.TRMF, [2](#)
components, [13](#)
components.TRMF, [3](#)
create_TRMF, [2](#), [3](#), [4](#), [6](#), [7](#), [9](#), [10](#), [12](#), [14–16](#),
[18](#), [19](#), [21–23](#)

fitted, [13](#)
fitted.TRMF, [5](#)

impute_TRMF, [6](#)

NormalizeMatrix, [7](#)

plot.TRMF, [8](#)
predict.TRMF, [9](#)

resid, [13](#)
residuals.TRMF, [10](#)
retrain, [11](#)

summary.TRMF, [12](#)

train.TRMF, [5](#), [7](#), [10](#), [11](#), [13](#), [16](#)
TRMF_ar, [14](#)
TRMF_coefficients (TRMF_columns), [15](#)
TRMF_columns, [2](#), [3](#), [5](#), [6](#), [9](#), [10](#), [12](#), [14](#), [15](#), [15](#),
[18](#), [19](#), [21–23](#)
TRMF_es, [17](#)
TRMF_regression, [18](#)
TRMF_seasonal, [18](#), [20](#), [22](#), [23](#)
TRMF_simple, [13](#), [21](#), [21](#), [23](#)
TRMF_trend, [2](#), [3](#), [5–7](#), [9](#), [10](#), [12](#), [14–16](#), [18](#),
[19](#), [21](#), [22](#), [22](#)