

Package ‘bama’

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Title High Dimensional Bayesian Mediation Analysis

Version 1.2

URL <https://github.com/umich-cphds/bama>

BugReports <https://github.com/umich-cphds/bama/issues>

Description Perform mediation analysis in the presence of high-dimensional mediators based on the potential outcome framework. Bayesian Mediation Analysis (BAMA), developed by Song et al (2019) <doi:10.1111/biom.13189> and Song et al (2020) <arXiv:2009.11409>, relies on two Bayesian sparse linear mixed models to simultaneously analyze a relatively large number of mediators for a continuous exposure and outcome assuming a small number of mediators are truly active. This sparsity assumption also allows the extension of univariate mediator analysis by casting the identification of active mediators as a variable selection problem and applying Bayesian methods with continuous shrinkage priors on the effects.

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Encoding UTF-8

LazyData true

RoxygenNote 7.1.1

LinkingTo Rcpp, RcppArmadillo, RcppDist, BH

Imports Rcpp, parallel

Depends R (>= 3.5)

Suggests knitr, rmarkdown

VignetteBuilder knitr

NeedsCompilation yes

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bama	<i>Bayesian Mediation Analysis</i>
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Description

bama is a Bayesian inference method that uses continuous shrinkage priors for high-dimensional Bayesian mediation analysis, developed by Song et al (2019, 2020). bama provides estimates for the regression coefficients as well as the posterior inclusion probability for ranking mediators.

Usage

```
bama(
  Y,
  A,
  M,
  C1,
  C2,
  method,
  burnin,
  ndraws,
  weights = NULL,
  inits = NULL,
  control = list(k = 2, lm0 = 1e-04, lm1 = 1, l = 1, lambda0 = 0.04, lambda1 = 0.2,
    lambda2 = 0.2, phi0 = 0.01, phi1 = 0.01, a0 = 0.01 * ncol(M), a1 = 0.05 * ncol(M), a2
    = 0.05 * ncol(M), a3 = 0.89 * ncol(M)),
  seed = NULL
)
```

Arguments

Y	Length n numeric outcome vector
A	Length n numeric exposure vector
M	n x p numeric matrix of mediators of Y and A
C1	n x nc1 numeric matrix of extra covariates to include in the outcome model
C2	n x nc2 numeric matrix of extra covariates to include in the mediator model

method	String indicating which method to use. Options are <ul style="list-style-type: none"> • "BSLMM" - mixture of two normal components; Song et al. 2019 • "PTG" - product threshold Gaussian prior; Song et al. 2020 • "GMM" - four-component Gaussian mixture prior; Song et al. 2020
burnin	number of iterations to run the MCMC before sampling
ndraws	number of draws to take from MCMC (includes burnin draws)
weights	Length n numeric vector of weights
inits	list of initial values for the Gibbs sampler. Options are <ul style="list-style-type: none"> • beta.m - Length p numeric vector of initial beta.m in the outcome model. See details for equation • alpha.a - Length p numeric vector of initial alpha.a in the mediator model. See details for equation
control	list of Gibbs algorithm control options. These include prior and hyper-prior parameters. Options vary by method selection. If method = "BSLMM" <ul style="list-style-type: none"> • k - Shape parameter prior for inverse gamma • lm0 - Scale parameter prior for inverse gamma for the small normal components • lm1 - Scale parameter prior for inverse gamma for the large normal components • l - Scale parameter prior for the other inverse gamma distributions If method = "PTG" <ul style="list-style-type: none"> • lambda0 - threshold parameter for product of alpha.a and beta.m effect • lambda1 - threshold parameter for beta.m effect • lambda2 - threshold parameter for alpha.a effect • ha - inverse gamma shape prior for sigma.sq.a • la - inverse gamma scale prior for sigma.sq.a • h1 - inverse gamma shape prior for sigma.sq.e • l1 - inverse gamma scale prior for sigma.sq.e • h2 - inverse gamma shape prior for sigma.sq.g • l2 - inverse gamma scale prior for sigma.sq.g • km - inverse gamma shape prior for tau.sq.b • lm - inverse gamma scale prior for tau.sq.b • kma - inverse gamma shape prior for tau.sq.a • lma - inverse gamma scale prior for tau.sq.a If method = "GMM" <ul style="list-style-type: none"> • phi0 - prior beta.m variance • phi1 - prior alpha.a variance • a0 - prior count of non-zero beta.m and alpha.a effects • a1 - prior count of non-zero beta.m and zero alpha.a effects • a2 - prior count of zero beta.m and non-zero alpha.a effects • a3 - prior count of zero beta.m and zero alpha.a effects

- ha - inverse gamma shape prior for sigma.sq.a
- la - inverse gamma scale prior for sigma.sq.a
- h1 - inverse gamma shape prior for sigma.sq.e
- l1 - inverse gamma scale prior for sigma.sq.e
- h2 - inverse gamma shape prior for sigma.sq.g
- l2 - inverse gamma scale prior for sigma.sq.g

seed numeric seed for GIBBS sampler

Details

bama uses two regression models for the two conditional relationships, $Y|A, M, C$ and $M|A, C$. For the outcome model, bama uses

$$Y = M\beta_M + A * \beta_A + C * \beta_C + \epsilon_Y$$

For the mediator model, bama uses the model

$$M = A * \alpha_A + C * \alpha_C + \epsilon_M$$

For high dimensional tractability, bama employs continuous Bayesian shrinkage priors to select mediators and makes the two following assumptions: First, it assumes that all the potential mediators contribute small effects in mediating the exposure-outcome relationship. Second, it assumes that only a small proportion of mediators exhibit large effects ("active" mediators). bama uses a Metropolis-Hastings within Gibbs MCMC to generate posterior samples from the model.

Value

If method = "BSLMM", then bama returns a object of type "bama" with 12 elements:

beta.m ndraws x p matrix containing outcome model mediator coefficients.

r1 ndraws x p matrix indicating whether or not each beta.m belongs to the larger normal component (1) or smaller normal component (0).

alpha.a ndraws x p matrix containing the mediator model exposure coefficients.

r3 ndraws x p matrix indicating whether or not each alpha.a belongs to the larger normal component (1) or smaller normal component (0).

beta.a Vector of length ndraws containing the beta.a coefficient.

pi.m Vector of length ndraws containing the proportion of non zero beta.m coefficients.

pi.a Vector of length ndraws containing the proportion of non zero alpha.a coefficients.

sigma.m0 Vector of length ndraws containing the standard deviation of the smaller normal component for mediator-outcome coefficients (beta.m).

sigma.m1 Vector of length ndraws containing standard deviation of the larger normal component for mediator-outcome coefficients (beta.m).

sigma.ma0 Vector of length ndraws containing standard deviation of the smaller normal component for exposure-mediator coefficients (alpha.a).

sigma.ma1 Vector of length ndraws containing standard deviation of the larger normal component for exposure-mediator coefficients (alpha.a).

call The R call that generated the output.

If method = "GMM", then bama returns a object of type "bama" with:

beta.m ndraws x p matrix containing outcome model mediator coefficients.

alpha.a ndraws x p matrix containing the mediator model exposure coefficients.

betam_member ndraws x p matrix of 1's and 0's where item = 1 only if beta.m is non-zero.

alphaa_member ndraws x p matrix of 1's and 0's where item = 1 only if alpha.a is non-zero.

alpha.c ndraws x (q2 + p) matrix containing alpha_c coefficients. Since alpha.c is a matrix of dimension q2 x p, the draws are indexed as $\alpha_c(w, j) = w * p + j$

beta.c ndraws x q1 matrix containing beta_c coefficients. Since beta.c is a matrix of dimension q1 x p

beta.a Vector of length ndraws containing the beta.a coefficient.

sigma.sq.a Vector of length ndraws variance of beta.a effect

sigma.sq.e Vector of length ndraws variance of outcome model error

sigma.sq.g Vector of length ndraws variance of mediator model error

If method = "PTG", then bama returns a object of type "bama" with:

beta.m ndraws x p matrix containing outcome model mediator coefficients.

alpha.a ndraws x p matrix containing the mediator model exposure coefficients.

alpha.c ndraws x (q2 + p) matrix containing alpha_c coefficients. Since alpha.c is a matrix of dimension q2 x p, the draws are indexed as $\alpha_c(w, j) = w * p + j$

beta.c ndraws x q1 matrix containing beta_c coefficients. Since beta.c is a matrix of dimension q1 x p

betam_member ndraws x p matrix of 1's and 0's where item = 1 only if beta.m is non-zero.

alphaa_member ndraws x p matrix of 1's and 0's where item = 1 only if alpha.a is non-zero.

beta.a Vector of length ndraws containing the beta.a coefficient.

sigma.sq.a Vector of length ndraws variance of beta.a effect

sigma.sq.e Vector of length ndraws variance of outcome model error

sigma.sq.g Vector of length ndraws variance of mediator model error

References

Song, Y, Zhou, X, Zhang, M, et al. Bayesian shrinkage estimation of high dimensional causal mediation effects in omics studies. *Biometrics*. 2019; 1-11. doi: [10.1111/biom.13189](https://doi.org/10.1111/biom.13189)

Song, Yanyi, Xiang Zhou, Jian Kang, Max T. Aung, Min Zhang, Wei Zhao, Belinda L. Needham et al. "Bayesian Sparse Mediation Analysis with Targeted Penalization of Natural Indirect Effects." arXiv preprint arXiv:2008.06366 (2020).

Examples

```

library(bama)

Y <- bama.data$y
A <- bama.data$a

# grab the mediators from the example data.frame
M <- as.matrix(bama.data[, paste0("m", 1:100)], nrow(bama.data))

# We just include the intercept term in this example as we have no covariates
C1 <- matrix(1, 1000, 1)
C2 <- matrix(1, 1000, 1)
beta.m <- rep(0, 100)
alpha.a <- rep(0, 100)

out <- bama(Y = Y, A = A, M = M, C1 = C1, C2 = C2, method = "BSLMM", seed = 1234,
            burnin = 1000, ndraws = 1100, weights = NULL, inits = NULL,
            control = list(k = 2, lm0 = 1e-04, lm1 = 1, l = 1))

# The package includes a function to summarise output from 'bama'
summary <- summary(out)
head(summary)

# Product Threshold Gaussian
ptgmod = bama(Y = Y, A = A, M = M, C1 = C1, C2 = C2, method = "PTG", seed = 1234,
             burnin = 1000, ndraws = 1100, weights = NULL, inits = NULL,
             control = list(lambda0 = 0.04, lambda1 = 0.2, lambda2 = 0.2))

mean(ptgmod$beta.a)
apply(ptgmod$beta.m, 2, mean)
apply(ptgmod$alpha.a, 2, mean)
apply(ptgmod$betam_member, 2, mean)
apply(ptgmod$alphaa_member, 2, mean)

# Gaussian Mixture Model
gmmmod = bama(Y = Y, A = A, M = M, C1 = C1, C2 = C2, method = "GMM", seed = 1234,
             burnin = 1000, ndraws = 1100, weights = NULL, inits = NULL,
             control = list(phi0 = 0.01, phi1 = 0.01))

mean(gmmmod$beta.a)
apply(gmmmod$beta.m, 2, mean)
apply(gmmmod$alpha.a, 2, mean)

mean(gmmmod$sigma.sq.a)
mean(gmmmod$sigma.sq.e)
mean(gmmmod$sigma.sq.g)

```

bama.data	<i>Synthetic example data for bama</i>
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Description

Synthetic example data for bama

Usage

```
bama.data
```

Format

A data.frame with 1000 observations on 102 variables:

y Numeric response variable.

a Numeric exposure variable.

m[1-100] Numeric mediator variables

fdr.bama	<i>Bayesian Mediation Analysis Controlling For False Discovery</i>
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Description

fdr.bama uses the permutation test to estimate the null PIP distribution for each mediator and determines a threshold (based off of the fdr parameter) for significance.

Usage

```
fdr.bama(  
  Y,  
  A,  
  M,  
  C1,  
  C2,  
  beta.m,  
  alpha.a,  
  burnin,  
  ndraws,  
  weights = NULL,  
  npermutations = 200,  
  fdr = 0.1,  
  k = 2,  
  lm0 = 1e-04,  
  lm1 = 1,
```

```

l = 1,
mc.cores = 1,
type = "PSOCK"
)

```

Arguments

Y	Length n numeric outcome vector
A	Length n numeric exposure vector
M	n x p numeric matrix of mediators of Y and A
C1	n x nc1 numeric matrix of extra covariates to include in the outcome model
C2	n x nc2 numeric matrix of extra covariates to include in the mediator model
beta.m	Length p numeric vector of initial beta.m in the outcome model
alpha.a	Length p numeric vector of initial alpha.a in the mediator model
burnin	Number of iterations to run the MCMC before sampling
ndraws	Number of draws to take from MCMC after the burnin period
weights	Length n numeric vector of weights
npermutations	The number of permutations to generate while estimating the null pip distribution. Default is 200
fdr	False discovery rate. Default is 0.1
k	Shape parameter prior for inverse gamma. Default is 2.0
lm0	Scale parameter prior for inverse gamma for the small normal components. Default is 1e-4
lm1	Scale parameter prior for inverse gamma for the large normal components. Default is 1.0
l	Scale parameter prior for the other inverse gamma distributions. Default is 1.0
mc.cores	The number of cores to use while running fdr.bama. fdr.bama uses the parallel package for parallelization, so see that for more information. Default is 1 core
type	Type of cluster to make when mc.cores > 1. See makeCluster in the parallel package for more details. Default is "PSOCK"

Value

fdr.bama returns a object of type "fdr.bama" with 5 elements:

bama.out Output from the bama run.

pip.null A p x npermutations matrices containing the estimated null PIP distribution for each mediator.

threshold The cutoff significance threshold for each PIP controlling for the false discovery rate.

fdr The false discovery rate used to calculate threshold.

call The R call that generated the output.

Author(s)

Alexander Rix

References

Song, Y, Zhou, X, Zhang, M, et al. Bayesian shrinkage estimation of high dimensional causal mediation effects in omics studies. *Biometrics*. 2019; 1-11. doi: [10.1111/biom.13189](https://doi.org/10.1111/biom.13189)

Examples

```
library(bama)

Y <- bama.data$y
A <- bama.data$a

# grab the mediators from the example data.frame
M <- as.matrix(bama.data[, paste0("m", 1:100)], nrow(bama.data))

# We just include the intercept term in this example as we have no covariates
C1 <- matrix(1, 1000, 1)
C2 <- matrix(1, 1000, 1)
beta.m <- rep(0, 100)
alpha.a <- rep(0, 100)

set.seed(12345)

out <- fdr.bama(Y, A, M, C1, C2, beta.m, alpha.a, burnin = 100,
               ndraws = 120, npermutations = 10)

# The package includes a function to summarise output from 'fdr.bama'
summary(out)
```

print.bama

Printing bama objects

Description

Print a bama object.

Usage

```
## S3 method for class 'bama'
print(x, ...)
```

Arguments

x An object of class 'bama'.
... Additional arguments to pass to print.data.frame or summary.bama

print.fdr.bama	<i>Printing bama objects</i>
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Description

Print a bama object.

Usage

```
## S3 method for class 'fdr.bama'
print(x, ...)
```

Arguments

x	An object of class 'bama'.
...	Additional arguments to pass to print.data.frame or summary.bama

summary.bama	<i>Summarize objects of type "bama"</i>
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Description

summary.bama summarizes the 'beta.m' estimates from bama and generates an overall estimate, credible interval, and posterior inclusion probability.

Usage

```
## S3 method for class 'bama'
summary(object, rank = F, ci = c(0.025, 0.975), ...)
```

Arguments

object	An object of class "bama".
rank	Whether or not to rank the output by posterior inclusion probability. Default is TRUE.
ci	The credible interval to calculate. ci should be a length 2 numeric vector specifying the upper and lower bounds of the CI. By default, ci = c(0.025, .975).
...	Additional optional arguments to summary

Value

A data.frame with 4 elements. The beta.m estimates, the estimates' *credible* interval (which by default is 95\ inclusion probability (pip) of each 'beta.m').

summary.fdr.bama *Summarize objects of type "fdr.bama"*

Description

summary.fdr.bama summarizes the beta.m estimates from fdr.bama and for each mediator generates an overall estimate, credible interval, posterior inclusion probability (PIP), and PIP threshold for significance controlling for the specified false discovery rate (FDR).

Usage

```
## S3 method for class 'fdr.bama'
summary(
  object,
  rank = F,
  ci = c(0.025, 0.975),
  fdr = object$fdr,
  filter = T,
  ...
)
```

Arguments

object	An object of class "bama".
rank	Whether or not to rank the output by posterior inclusion probability. Default is TRUE.
ci	The credible interval to calculate. ci should be a length 2 numeric vector specifying the upper and lower bounds of the CI. By default, ci = c(0.025, .975).
fdr	False discovery rate. By default, it is set to whatever the fdr of object is. However, it can be changed to recalculate the PIP cutoff threshold.
filter	Whether or not to filter out mediators with PIP less than the PIP threshold.
...	Additional optional arguments to summary

Value

A data.frame with 4 elements. The beta.m estimates, the estimates' *credible* interval (which by default is 95\ inclusion probability (pip) of each 'beta.m'.

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