

Package ‘binfunest’

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Type Package

Title Estimates Parameters of Functions Driving Binomial Random Variables

Version 0.1.0

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Description Provides maximum likelihood estimates of the performance parameters that drive a binomial distribution of observed errors, and takes full advantage of zero error observations. High performance communications systems typically have inherent noise sources and other performance limitations that need to be estimated. Measurements made at high signal to noise ratios typically result in zero errors due to limitation in available measurement time. Package includes theoretical performance functions for common modulation schemes (Proakis, "Digital Communications" (1995, <ISBN:0-07-051726-6>)), polarization shifted QPSK (Agrell & Karlsson (2009, <DOI:10.1109/JLT.2009.2029064>)), and utility functions to work with the performance functions.

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Suggests covr, knitr, rmarkdown, testthat (>= 3.0.0)

VignetteBuilder knitr

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Imports pracma, stats, stats4

URL <https://github.com/PhilShea/binfunest>

BugReports <https://github.com/PhilShea/binfunest/issues>

Depends R (>= 2.10)

NeedsCompilation no

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R topics documented:

B2BConvert	2
BERDFc	3
mleB2B	3
Theoretical	5

Index	8
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B2BConvert	<i>B2BConvert Converts a function of SNR into one of SNR, B2B, and Offset.</i>
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Description

Creates a function $f(-dB(\text{undB}(-s) + \text{undB}(-B2B)) - \text{offset})$

Usage

B2BConvert(f)

Arguments

f A function of a single argument $f(s)$.

Details

Note that all quantities are assumed to be in Decibels.

Value

A function of three arguments $f(s, B2B, \text{offset})$..

Examples

```
QPSKdB.B2B <- B2BConvert( QPSKdB)
```

BERDFc	<i>An example BERDF dataframe created by <code>simsigs()</code>, a function in a forthcoming package coherent.</i>
--------	--

Description

BERDF is a standard R data frame created by the `simsigs()` function in the forthcoming coherent package. The observations have been condensed

Usage

```
BERDFc
```

Format

A dataframe with the following fields:

Name Name of constellation used to create the record.

SNR The SNR in Decibels of the observation.

Bps The number of bits per symbol. The number of bits in a simulation run is $\text{Bps} * N$

NoisePower The actual noise power in the simulation run. Since the noise is randomly generated, this is a stochastic item.

N The number of symbols in the simulation run.

SER The number of symbols errors observed in the simulation run.

BER The number of bit errors observed in the simulation run.

mleB2B	<i>mleB2B Estimates Back-to-Back "Q" and Offsets to a bit error rate function.</i>
--------	--

Description

Bit error counts modeled as independent binary decisions result in a log-likelihood dependent on the bit error probability. This function inserts the supplied bit error probability function into the binomial log-likelihood function, and passes that to `stats4::mle`, which ultimately calls `stats::optim`. The function will optimize a binomial probability of the form $r = N * P(x_1, x_2, \dots, x_n, a_1, a_2, \dots, a_k)$, where the x_i are variables from data, and the a_j are parameters to be estimated.

Usage

```
mleB2B(data = NULL, Errors, N, f, fparms, start, method = "Nelder-Mead", ...)
```

Arguments

data	a data frame or list with named components. If a list, each component must be the same length (just like a data frame). This is not checked, so usual rules of recycling will apply. Partial matching not performed, so you must use full column names.
Errors	A vector of error counts, or a string identifying a column of data from which to draw the error counts
N	A single number, or a vector of the same length as data, or a string identifying a column of data specifying the number of trials used to measure the error counts in Errors. If a single number, then that number is used as the number of trials for all error counts.
f	A function that predicts the probability of errors.
fparms	a list of named components that are the arguments of f. Each component can be a string, a single number, or a vector. If a string that names a column of data, that column will be used, otherwise the string will be passed to f. Note the potential for errors if a column name was misspelled. A single number or vector will be passed to f. Between fparms, start, and function defaults, all parameters that need to be supplied to f should be specified, and (except for defaults) not duplicated.
start	Named list of initial values for the parameters of f to be estimated.
method	Optimization method. See <code>stats::optim()</code> .
...	Optional arguments to be passed to <code>mle</code> .

Details

The function estimates the parameters identified in `start` in the constructed call to `f`. For a function `f` of the form `fun(SNR, x2, x3, B2B, offset)` A call of the form

```
mleB2B( data=df, Errors="r", N="trials", f=fun, fparm=list( SNR="s", x2=1, x3="noise"),
start=list(B2B=1, offset=2))
```

will construct a call to `mle` of the form:

```
mle( minuslogl=ll, start=start, nobs=length( Errors), method=method)
```

where the function `ll` is defined as

```
ll <- function( a, b) -sum( dbinom( df$r, df$n, fun( SNR=df$s, x2=1, x3=df$noise, B2B=B2B,
offset=offset), log=TRUE))
```

Value

An object of class `stats4:mle` with the parameters identified in `start` estimated.

See Also

`stats4::mle()`, `stats::optim()`

Examples

```

QPSKdB.B2B <- B2BConvert( QPSKdB)
O1 <- 3
B1 <- 16
s <- 0:20
N <- 1000000
r <- rbinom( length( s), N, QPSKdB.B2B( s, B1, O1))
df <- data.frame( Errors=r, SNR=s, N=N)
llsb2 <- function( b2b, offset)
  -sum( dbinom( r, N, QPSKdB.B2B( s, b2b, offset), log=TRUE))
mle1 <- stats4::mle( llsb2, start=c( b2b=20, offset=0), nobs=length(s),
  method="Nelder-Mead")
est1 <- mleB2B( data=df, Errors="Errors", N=N, f=QPSKdB.B2B,
  fparams=list( x="SNR"), start=c(b2b=20, offset=0))

```

Theoretical

Theoretical error rate functions

Description

Functions to calculate the theoretical performance of common modulation formats. Includes the functions $\text{dB}(x)$ (returns $10\log_{10}(x)$), $\text{undB}(x)$ (reverses $\text{dB}(x)$), $Q_{\cdot}(x)$ (Markum's Q function), and $Q_{\cdot}\text{Inv}(x)$ (returns the SNR in Decibels to get probability x). Also includes mod_Inv , which returns the SNR required for a the function f to reach the supplied BER (bit error rate, or bit error probability).

Usage

```
is.wholenumber(x, tol = sqrt(.Machine$double.eps))
```

```
dB(x)
```

```
undB(x)
```

```
Q_{\cdot}(x)
```

```
Q_{\cdot}\text{Inv}(perr)
```

```
QPSKdB(x)
```

```
DQPSKdB(x)
```

```
DQPSKDDdB(x)
```

```
PSQPSKdB(x)
```

```
MPSKdB(x, M)
```

MPSKdB.8(x)

QAMdB.8.star(x)

QAMdB(x, M)

QAMdB.16(x)

mod_Inv(f, perr, guess = Q_Inv(perr))

mod_InvV(f, pv, offset = 0)

Arguments

x	a real number
tol	the tolerance to test x with.
perr	a probability of a bit error.
M	The integer number of symbols > 4.
f	a function (usually a BER function).
guess	a guess for the perr (the default usually works).
pv	a vector of BERs.
offset	an offset in Decibels for guesses in mod_InvV.

Details

The rest of the functions return the probability of a bit error given the SNR in Decibels.

- QPSKdB is Quadrature Phase shift keyed: two bits per symbol.
- DQPSK is differentially detected differentially coded QPSK.
- DQPSKDDdB is differentially detected differential QPSK (coherently detected but differentially decoded. See DQPSK above).
- PSQPSKdB is polarization-shifted QPSK: it is dual pole, but only one pole is active at any one time, thus supplying three bits per symbol. (See Agrell & Karlsson (2009, DOI:10.1109/JLT.2009.2029064)).
- MPSKdB(x, M) is generic M-ary phase shift keying of M points in a circle.
- MPSKdB.8 simply returns MPSKdB(x, 8)
- QAMdB.8.star is the optimal star configuration of 8-ary Quadrature Amplitude Modulation (QAM), such that the legs are at ± 1 and $\pm(1 + \sqrt{3})$.
- QAMdB(x, M) is generic rectangular QAM constellation of M points.
- QAMdB.16 Returns the BER for the rectangular QAM constellation according to Proakis Eq. 5-2-80.
- mod_Inv will take a function $f(x)$ and return the x such that $f(x) == perr$ but it does this based on the $\log(f(x))$ and the $\log(perr)$, so $f(x) > 0$.
- mod_InvV is a vectorized version (give it a vector of BERs and it returns a vector of SNRs).

Value

`is.wholenumber(x)` returns TRUE if $\text{c-round}(x) < \text{tol}$.

`dB(x)` returns $10 \cdot \log_{10}(x)$

`undB(x)` returns $10^{(x/10)}$

`Q_Inv(x)` returns $2 \cdot \text{dB}(-\text{qnorm}(x))$, which is the SNR (in Decibels) required to get a probability of error of x . $\text{Q_Inv}(\text{Q}(\text{undB}(x/2))) = x$ and $\text{Q}(\text{undB}(\text{Q_Inv}(x)/2)) = x$

`mod_Inv(f, x)` returns a list with the SNR in Decibels to reach the BER `perr` such that $f(\text{mod_Inv}(f, x)[x]) = x$. The returned list has elements `$x` as the SNR and `$fval` as the function value.

See Also

[pracma::fzero\(\)](#)

Examples

```
dB( 10) # == 10
```

```
undB( 20) # == 100
```

```
Q_Inv( Q_( undB( 10/2))) # = 10
```

```
Q_( undB( Q_Inv( 0.001)/2)) # = 0.001
```

```
mod_Inv( QPSKdB, QPSKdB( 7)) # yields 7
```

```
mod_InvV(QPSKdB, QPSKdB(c(6,7)))
```

Index

* datasets

BERDFc, 3

B2BConvert, 2

BERDFc, 3

dB (Theoretical), 5

DQPSKdB (Theoretical), 5

DQPSKDDdB (Theoretical), 5

is.wholenumber (Theoretical), 5

mle, 4

mleB2B, 3

mod_Inv (Theoretical), 5

mod_InvV (Theoretical), 5

MPSKdB (Theoretical), 5

pracma::fzero(), 7

PSQPSKdB (Theoretical), 5

Q_ (Theoretical), 5

Q_Inv (Theoretical), 5

QAMdB (Theoretical), 5

QPSKdB (Theoretical), 5

stats4::mle, 3, 4

stats4::mle(), 4

stats::optim, 3

stats::optim(), 4

Theoretical, 5

undB (Theoretical), 5