

Package ‘breakfast’

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Title Methods for Fast Multiple Change-Point Detection and Estimation

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Description A developing software suite for multiple change-point detection/estimation (data segmentation) in data sequences.

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breakfast-package	<i>Breakfast: Methods for Fast Multiple Change-point Detection and Estimation</i>
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Description

A developing software suite for multiple change-point detection/estimation (data segmentation) in data sequences.

Details

The current version implements the Gaussian mean-shift model, in which the data are assumed to be a piecewise-constant signal observed with i.i.d. Gaussian noise. Change-point detection in `breakfast` is carried out in two stages: (i) computation of a solution path, and (ii) model selection along the path. A variety of solution path and model selection methods are included, which can be accessed individually, or through `breakfast`. Currently supported solution path methods are: `sol.idetect`, `sol.idetect_seq`, `sol.wbs`, `sol.wbs2`, `sol.not` and `sol.tguh`.

Currently supported model selection methods are: `model.ic`, `model.lp`, `model.sdll` `model.thresh`.

Check back future versions for more change-point models and further methods.

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See Also

`browseVignettes(package = "breakfast")` contains a detailed comparative simulation study of various methods implemented in `breakfast` for the Gaussian mean-shift model.

Description

This function estimates the number and locations of change-points in a data sequence, which is modelled as a piecewise-constant function plus i.i.d. Gaussian noise. This is carried out via a two-stage procedure combining solution path generation and model selection methodologies.

Usage

```
breakfast(x, solution.path = NULL, model.selection = NULL)
```

Arguments

- x** A numeric vector containing the data to be processed
- solution.path** A string or a vector of strings containing the name(s) of solution path generating method(s); if individual methods are accessed via this option, default tuning parameters are used. Alternatively, you can directly access each solution path generating method via `sol.[method]`, see below. If both `solution.path` and `model.selection` are unspecified, we return the output from the suggested combinations based on their performance, which are: ("idetect", "ic"), ("idetect_seq", "thresh"), ("not", "ic"), ("tguh", "lp"), ("wbs", "ic") and ("wbs2", "sdll"). If `solution.path` is specified but `model.selection` is not, we return the output from the specified `solution.path` methods combined with the suggested model selection methods (respectively) as above.
- "idetect" IDetect, see [sol.idetect](#)
 - "idetect_seq" Sequential IDetect, see [sol.idetect_seq](#)
 - "not" Narrowest-Over-Threshold, see [sol.not](#)
 - "tguh" Tail-Greedy Unbalanced Haar, see [sol.tguh](#)
 - "wbs" Wild Binary Segmentation, see [sol.wbs](#)
 - "wbs2" Wild Binary Segmentation 2, see [sol.wbs2](#)
 - "all" All of the above
- model.selection** A string or a vector of strings containing the name(s) of model selection method(s); if individual methods are accessed via this option, default tuning parameters are used. Alternatively, you can directly access each model selection method via `model.[method]`, see below. If both `solution.path` and `model.selection` are unspecified, we return the output from the suggested combinations based on their performance, which are: ("idetect", "ic"), ("idetect_seq", "thresh"), ("not", "ic"), ("tguh", "lp"), ("wbs", "ic") and ("wbs2", "sdll"). If `model.selection` is specified but `solution.path` is not, we return the output from the specified `model.selection` methods combined with the suggested solution path methods (respectively) as above.
- "ic" Strengthened Schwarz information criterion, see [model.ic](#)

- "lp" Localised pruning, see [model.lp](#)
- "sdll" Steepest Drop to Low Levels method, see [model.sdll](#)
- "thresh" Thresholding, see [model.thresh](#)
- "all" All of the above

Details

Please also take a look at the vignette for tips/suggestions/examples of using the breakfast package.

Value

An S3 object of class `breakfast.cpts`, which contains the following fields:

- `x` Input vector `x`
- `cptmodel.list` A list containing S3 objects of class `cptmodel`; each contains the following fields:
 - `solution.path` The solution path method used
 - `model.selection` The model selection method used to return the final change-point estimators object
 - `no.of.cpt` The number of estimated change-points in the piecewise-constant mean of the vector `cptpath.object$x`
 - `cpts` The locations of estimated change-points in the piecewise-constant mean of the vector `cptpath.object$x`. These are the end-points of the corresponding constant-mean intervals
 - `est` An estimate of the piecewise-constant mean of the vector `cptpath.object$x`; the values are the sample means of the data (replicated a suitable number of times) between each pair of consecutive detected change-points

References

- A. Anastasiou & P. Fryzlewicz (2019). Detecting multiple generalized change-points by isolating single ones. *arXiv preprint arXiv:1901.10852*.
- R. Baranowski, Y. Chen & P. Fryzlewicz (2019). Narrowest-over-threshold detection of multiple change points and change-point-like features. *Journal of the Royal Statistical Society: Series B*, 81(3), 649–672.
- H. Cho & C. Kirch (2021) Two-stage data segmentation permitting multiscale change points, heavy tails and dependence. *arXiv preprint arXiv:1910.12486*.
- P. Fryzlewicz (2014). Wild binary segmentation for multiple change-point detection. *The Annals of Statistics*, 42(6), 2243–2281.
- P. Fryzlewicz (2020). Detecting possibly frequent change-points: Wild Binary Segmentation 2 and steepest-drop model selection. *To appear in Journal of the Korean Statistical Society*.
- P. Fryzlewicz (2018). Tail-greedy bottom-up data decompositions and fast multiple change-point detection. *The Annals of Statistics*, 46(6B), 3390–3421.

Examples

```
f <- rep(rep(c(0, 1), each = 50), 10)
x <- f + rnorm(length(f)) * .5
breakfast(x)
```

model.ic	<i>Estimating change-points in the piecewise-constant mean of a noisy data sequence via the strengthened Schwarz information criterion</i>
----------	--

Description

This function estimates the number and locations of change-points in the piecewise-constant mean of a noisy data sequence via the sSIC (strengthened Schwarz information criterion) method.

Usage

```
model.ic(cptpath.object, alpha = 1.01, q.max = NULL)
```

Arguments

cptpath.object	A solution-path object, returned by a sol.[name] routine. Note that the field <code>cptpath.object\$x</code> contains the input data sequence.
alpha	The parameter associated with the sSIC. The default value is 1.01. Note that the SIC is recovered when $\alpha = 1$.
q.max	The maximum number of change-points allowed. If nothing or NULL is provided, the default value of $\min(100, n/\log(n))$ (rounded to an integer) will be used.

Details

The model selection method for algorithms that produce nested solution path is described in "Wild binary segmentation for multiple change-point detection", P. Fryzlewicz (2014), *The Annals of Statistics*, 42: 2243–2281. The corresponding description for those that produce non-nested solution set can be found in "Narrowest-over-threshold detection of multiple change points and change-point-like features", R. Baranowski, Y. Chen and P. Fryzlewicz (2019), *Journal of Royal Statistical Society: Series B*, 81(3), 649–672.

Value

An S3 object of class `cptmodel`, which contains the following fields:

solution.path	The solution path method used to obtain <code>cptpath.object</code>
model.selection	The model selection method used to return the final change-point estimators object, here its value is "ic"
no.of.cpt	The number of estimated change-points in the piecewise-constant mean of the vector <code>cptpath.object\$x</code>

cpts	The locations of estimated change-points in the piecewise-constant mean of the vector <code>cptpath.object\$x</code> . These are the end-points of the corresponding constant-mean intervals
est	An estimate of the piecewise-constant mean of the vector <code>cptpath.object\$x</code> ; the values are the sample means of the data (replicated a suitable number of times) between each pair of consecutive detected change-points

References

- P. Fryzlewicz (2014). Wild binary segmentation for multiple change-point detection. *The Annals of Statistics*, 42(6), 2243–2281.
- R. Baranowski, Y. Chen & P. Fryzlewicz (2019). Narrowest-over-threshold detection of multiple change points and change-point-like features. *Journal of the Royal Statistical Society: Series B*, 81(3), 649–672.

See Also

[sol.idetect](#), [sol.not](#), [sol.tguh](#), [sol.wbs](#), [sol.wbs2](#), [breakfast](#)

Examples

```
x <- c(rep(0, 100), rep(1, 100), rep(0, 100)) + rnorm(300)
model.ic(sol.wbs(x))
model.ic(sol.not(x))
```

model.lp	<i>Estimating change-points in the piecewise-constant mean of a noisy data sequence via the localised pruning</i>
----------	---

Description

This function estimates the number and locations of change-points in the piecewise-constant mean of a noisy data sequence via the localised pruning method, which performs a Schwarz criterion-based model selection on the given candidate set in a localised way.

Usage

```
model.lp(
  cptpath.object,
  min.d = 5,
  penalty = c("log", "polynomial"),
  pen.exp = 1.01,
  do.thr = TRUE,
  th.const = 0.5
)
```

Arguments

<code>cptpath.object</code>	A solution-path object, returned by a <code>sol.[name]</code> routine. Note that the field <code>cptpath.object\$x</code> contains the input data sequence.
<code>min.d</code>	A number specifying the minimal spacing between change points; <code>min.d = 5</code> by default
<code>penalty</code>	A string specifying the type of penalty term to be used in Schwarz criterion; possible values are: <ul style="list-style-type: none"> • "log" Use $\text{penalty} = \log(\text{length}(x))^{\text{pen.exp}}$ • "polynomial" Use $\text{penalty} = \text{length}(x)^{\text{pen.exp}}$
<code>pen.exp</code>	Exponent for the penalty term (see <code>penalty</code>)
<code>do.thr</code>	If <code>do.thr = TRUE</code> , mild threshoding on the CUSUM test statistics is performed after internal standardisation step in order to "pre-prune down" the candidates
<code>th.const</code>	A constant multiplied to $\sqrt{2 \cdot \log(\text{length}(x))}$ to form a mild threshold; if not supplied, a default value ($0.5 \cdot$ a value suggested in Fryzlewicz (2020)) is used, see <code>th.const</code> in model.sd11

Details

Further information can be found in Cho and Kirch (2021).

Value

An S3 object of class `cptmodel`, which contains the following fields:

<code>solution.path</code>	The solution path method used to obtain <code>cptpath.object</code>
<code>model.selection</code>	The model selection method used to return the final change-point estimators object, here its value is "lp"
<code>no.of.cpt</code>	The number of estimated change-points in the piecewise-constant mean of the vector <code>cptpath.object\$x</code>
<code>pts</code>	The locations of estimated change-points in the piecewise-constant mean of the vector <code>cptpath.object\$x</code> . These are the end-points of the corresponding constant-mean intervals
<code>est</code>	An estimate of the piecewise-constant mean of the vector <code>cptpath.object\$x</code> ; the values are the sample means of the data (replicated a suitable number of times) between each pair of consecutive detected change-points

References

H. Cho & C. Kirch (2021) Two-stage data segmentation permitting multiscale change points, heavy tails and dependence. *arXiv preprint arXiv:1910.12486*.

See Also

[sol.idetect](#), [sol.idetect_seq](#), [sol.not](#), [sol.tguh](#), [sol.wbs](#), [sol.wbs2](#), [breakfast](#)

Examples

```
f <- rep(rep(c(0, 1), each = 50), 10)
x <- f + rnorm(length(f)) * .5
model.lp(sol.not(x))
```

model.sdll

Estimating change-points in the piecewise-constant mean of a noisy data sequence via the Steepest Drop to Low Levels method

Description

This function estimates the number and locations of change-points in the piecewise-constant mean of a noisy data sequence via the Steepest Drop to Low Levels method.

Usage

```
model.sdll(
  cptpath.object,
  sigma = stats::mad(diff(cptpath.object$x)/sqrt(2)),
  universal = TRUE,
  th.const = NULL,
  th.const.min.mult = 0.3,
  lambda = 0.9
)
```

Arguments

- | | |
|----------------|--|
| cptpath.object | A solution-path object, returned by a sol.[name] routine. In particular, SDLL model selection should work well when cptpath.object is an object returned by the sol.wbs2 routine. Note that the field cptpath.object\$x contains the input data sequence. |
| sigma | An estimate of the standard deviation of the noise in the data cptpath.object\$x. Can be a functional of cptpath.object\$x or a specific value if known. The default is the Median Absolute Deviation of the vector diff(cptpath.object\$x)/sqrt(2), tuned to the Gaussian distribution. Note that model.sdll works particularly well when the noise is i.i.d. Gaussian. |
| universal | If TRUE, then the threshold that decides if there are any change-points is chosen automatically, so that the probability of type-I error (i.e. indicating change-points if there are none) is approximately 1 -alpha when the number M of intervals drawn in the sol.wbs2 solution path routine is 1000. If FALSE, then th.const must be specified. |
| th.const | Only relevant if universal == FALSE; in that case a numerical value must be provided. Used to create the threshold (applicable to the CUSUM magnitudes stored in cptpath.object) that decides if there are any change-points in the mean vector; that threshold is then th.const * sqrt(2 * log(n)) * sigma, where n is the length of the data vector cptpath.object\$x. |

th.const.min.mult	A fractional multiple of the threshold, used to decide the lowest magnitude of CUSUMs from <code>cptpath.object</code> still considered by the SDLL model selection criterion as potentially change-point-carrying.
lambda	Only relevant if <code>universal == TRUE</code> ; can be set to 0.9 or 0.95. The approximate probability of not detecting any change-points if the truth does not contain any, when the number <code>M</code> of intervals drawn in the <code>sol.wbs2</code> solution path routine is 1000.

Details

The Steepest Drop to Low Levels method is described in "Detecting possibly frequent change-points: Wild Binary Segmentation 2 and steepest-drop model selection", P. Fryzlewicz (2020), *Journal of the Korean Statistical Society*, 49, 1027–1070.

Value

An S3 object of class `cptmodel`, which contains the following fields:

<code>solution.path</code>	The solution path method used to obtain <code>cptpath.object</code>
<code>model.selection</code>	The model selection method used to return the final change-point estimators object, here its value is "sdll"
<code>no.of.cpt</code>	The number of estimated change-points in the piecewise-constant mean of the vector <code>cptpath.object\$x</code>
<code>cpts</code>	The locations of estimated change-points in the piecewise-constant mean of the vector <code>cptpath.object\$x</code> . These are the end-points of the corresponding constant-mean intervals
<code>est</code>	An estimate of the piecewise-constant mean of the vector <code>cptpath.object\$x</code> ; the values are the sample means of the data (replicated a suitable number of times) between each pair of consecutive detected change-points

References

P. Fryzlewicz (2020). Detecting possibly frequent change-points: Wild Binary Segmentation 2 and steepest-drop model selection. *Journal of the Korean Statistical Society*, 49, 1027–1070.

See Also

[sol.idetect](#), [sol.idetect_seq](#), [sol.not](#), [sol.tguh](#), [sol.wbs](#), [sol.wbs2](#), [breakfast](#)

Examples

```
f <- rep(rep(c(0, 1), each = 50), 10)
x <- f + rnorm(length(f))
model.sdll(sol.wbs2(x))
```

model.thresh	<i>Estimating change-points in the piecewise-constant mean of a noisy data sequence via thresholding</i>
--------------	--

Description

This function estimates the number and locations of change-points in the piecewise-constant mean of a noisy data sequence via thresholding.

Usage

```
model.thresh(
  cptpath.object,
  sigma = stats::mad(diff(cptpath.object$x)/sqrt(2)),
  th_const = 1.15
)
```

Arguments

cptpath.object	A solution-path object, returned by a sol.[name] routine. Note that the field sols.object\$x contains the input data sequence.
sigma	An estimate of the standard deviation of the noise in the data cptpath.object\$x. Can be a functional of cptpath.object\$x or a specific value if known. The default is the Median Absolute Deviation of the vector diff(cptpath.object\$x)/sqrt(2), tuned to the Gaussian distribution. Note that model.thresh works particularly well when the noise is i.i.d. Gaussian.
th_const	A positive real number with default value equal to 1. It is used to define the threshold for the detection process.

Value

An S3 object of class cptmodel, which contains the following fields:

solution.path	The solution path method used to obtain cptpath.object
model.selection	The model selection method used to return the final change-point estimators object, here its value is "thresh"
no.of.cpt	The number of estimated change-points in the piecewise-constant mean of the vector cptpath.object\$x
cpts	The locations of estimated change-points in the piecewise-constant mean of the vector cptpath.object\$x. These are the end-points of the corresponding constant-mean intervals
est	An estimate of the piecewise-constant mean of the vector cptpath.object\$x; the values are the sample means of the data (replicated a suitable number of times) between each pair of consecutive detected change-points

See Also

[sol.idetect_seq](#), [sol.idetect_seq](#), [sol.not](#), [sol.tguh](#), [sol.wbs](#), [sol.wbs2](#), [breakfast](#)

Examples

```
f <- rep(rep(c(0, 1), each = 50), 10)
x <- f + rnorm(length(f))
model.thresh(sol.idetect_seq(x))
```

plot.breakfast.cpts *Change-points estimated by breakfast*

Description

Plot method for objects of class `breakfast.cpts`

Usage

```
## S3 method for class 'breakfast.cpts'
plot(x, display.data = TRUE, ...)
```

Arguments

<code>x</code>	a <code>breakfast.cpts</code> object
<code>display.data</code>	if <code>display.data = TRUE</code> , change-point estimators are plotted against the data by method. If <code>display.data = FALSE</code> , only the estimators are plotted; this option is recommended when <code>length(x)</code> is large.
<code>...</code>	current not in use

Examples

```
f <- rep(rep(c(0, 1), each = 50), 5)
x <- f + rnorm(length(f)) * .5
plot(breakfast(x, solution.path = 'all', model.selection = 'all'), display.data = TRUE)
plot(breakfast(x), display.data = FALSE)
```

```
print.breakfast.cpts Change-points estimated by breakfast
```

Description

Print method for objects of class `breakfast.cpts`

Usage

```
## S3 method for class 'breakfast.cpts'
print(x, by = c("method", "estimator"), ...)
```

Arguments

<code>x</code>	a <code>breakfast.cpts</code> object
<code>by</code>	if <code>by = 'method'</code> , change-point estimators are printed by method; if <code>by = 'estimator'</code> , each change-point estimator is printed with the methods that detect it.
<code>...</code>	current not in use

Examples

```
f <- rep(rep(c(0, 1), each = 50), 5)
x <- f + rnorm(length(f)) * .5
print(breakfast(x, solution.path = 'all', model.selection = 'all'), by = 'method')
print(breakfast(x), by = 'estimator')
```

```
print.cptmodel Change-points estimated by solution path generation + model selection methods
```

Description

Print method for objects of class `cptmodel`

Usage

```
## S3 method for class 'cptmodel'
print(x, ...)
```

Arguments

<code>x</code>	a <code>cptmodel</code> object
<code>...</code>	current not in use

Examples

```
f <- rep(rep(c(0, 1), each = 50), 5)
x <- f + rnorm(length(f)) * .5
print(model.ic(sol.idetect(x)))
```

sol.idetect

*Solution path generation via the Isolate-Detect method***Description**

This function arranges all possible change-points in the mean of the input vector in the order of importance, via the Isolate-Detect (ID) method. It is developed to be used with the sdll and information criterion (ic) model selection rules.

Usage

```
sol.idetect(x, thr_ic = 0.9, points = 3)
```

Arguments

x	A numeric vector containing the data to be processed.
thr_ic	A positive real number with default value equal to 0.9. It is used to create the solution path. The lower the value, the larger the solution path vector.
points	A positive integer with default value equal to 3. It defines the distance between two consecutive end- or start-points of the right- or left-expanding intervals, as described in the Isolate-Detect methodology.

Details

The Isolate-Detect method and its algorithm is described in "Detecting multiple generalized change-points by isolating single ones", A. Anastasiou & P. Fryzlewicz (2021), *Metrika*, <https://doi.org/10.1007/s00184-021-00821-6>.

Value

An S3 object of class `cptpath`, which contains the following fields:

solutions.nested	TRUE, i.e., the change-point outputs are nested
solution.path	Locations of possible change-points in the mean of x, arranged in decreasing order of change-point importance
solution.set	Empty list
x	Input vector x

cands	Matrix of dimensions $\text{length}(x) - 1$ by 4. The first two columns are (start, end)-points of the detection intervals of the corresponding possible change-point location in the third column. The fourth column is a measure of strength of the corresponding possible change-point. The order of the rows is the same as the order returned in <code>solution.path</code>
method	The method used, which has value "idetect" here

References

A. Anastasiou & P. Fryzlewicz (2021). Detecting multiple generalized change-points by isolating single ones. *Metrika*, <https://doi.org/10.1007/s00184-021-00821-6>.

See Also

[sol.idetect_seq](#), [sol.not](#), [sol.wbs](#), [sol.wbs2](#), [sol.tguh](#),

Examples

```
r3 <- rnorm(1000) + c(rep(0,300), rep(2,200), rep(-4,300), rep(0,200))
sol.idetect(r3)
```

sol.idetect_seq	<i>Solution path generation using the sequential approach of the Isolate-Detect method</i>
-----------------	--

Description

This function uses the Isolate-Detect method in its original sequential way in order to create the solution path. It is developed to be used with the thresholding model selection rule.

Usage

```
sol.idetect_seq(x, points = 3)
```

Arguments

x	A numeric vector containing the data to be processed
points	A positive integer with default value equal to 3. It defines the distance between two consecutive end- or start-points of the right- or left-expanding intervals, as described in the Isolate-Detect methodology.

Details

The Isolate-Detect method and its algorithm is described in "Detecting multiple generalized change-points by isolating single ones", A. Anastasiou & P. Fryzlewicz (2021), *Metrika*, <https://doi.org/10.1007/s00184-021-00821-6>.

Value

An S3 object of class `cptpath`, which contains the following fields:

<code>solutions.nested</code>	TRUE, i.e., the change-point outputs are nested
<code>solution.path</code>	Locations of possible change-points in the mean of <code>x</code> , arranged in decreasing order of change-point importance
<code>solution.set</code>	Empty list
<code>x</code>	Input vector <code>x</code>
<code>cands</code>	Matrix of dimensions <code>length(x) - 1</code> by 4. The first two columns are (start, end)-points of the detection intervals of the corresponding possible change-point location in the third column. The fourth column is a measure of strength of the corresponding possible change-point. The order of the rows is the same as the order returned in <code>solution.path</code>
<code>method</code>	The method used, which has value "idetect_seq" here

References

A. Anastasiou & P. Fryzlewicz (2021). Detecting multiple generalized change-points by isolating single ones. *Metrika*, <https://doi.org/10.1007/s00184-021-00821-6>.

See Also

[sol.idetect](#), [sol.not](#), [sol.wbs](#), [sol.wbs2](#), [sol.tguh](#),

Examples

```
r3 <- rnorm(1000) + c(rep(0,300), rep(2,200), rep(-4,300), rep(0,200))
sol.idetect_seq(r3)
```

sol.not

Solution path generation via the Narrowest-Over-Threshold method

Description

This function arranges all possible change-points in the mean of the input vector in the order of importance, via the Narrowest-Over-Threshold (NOT) method.

Usage

```
sol.not(x, M = 10000, systematic.intervals = TRUE, seed = NULL)
```

Arguments

<code>x</code>	A numeric vector containing the data to be processed
<code>M</code>	The maximum number of all data sub-samples at the beginning of the algorithm. The default is <code>M = 10000</code>
<code>systematic.intervals</code>	When drawing the sub-intervals, whether to use a systematic (and fixed) or random scheme. The default is <code>systematic.intervals = TRUE</code>
<code>seed</code>	If a random scheme is used, a random seed can be provided so that every time the same sets of random sub-intervals would be drawn. The default is <code>seed = NULL</code> , which means that this option is not taken

Details

The Narrowest-Over-Threshold method and its algorithm is described in "Narrowest-over-threshold detection of multiple change points and change-point-like features", R. Baranowski, Y. Chen and P. Fryzlewicz (2019), *Journal of Royal Statistical Society: Series B*, 81(3), 649–672.

Value

An S3 object of class `cptpath`, which contains the following fields:

<code>solutions.nested</code>	FALSE, i.e., the change-point outputs are not nested
<code>solution.path</code>	Empty list
<code>solution.set</code>	Locations of possible change-points in the mean of <code>x</code> for each threshold level (in the decreasing order), arranged in the form of a list of lists
<code>solution.set.th</code>	A list that contains threshold levels corresponding to the detections in <code>solution.set</code>
<code>x</code>	Input vector <code>x</code>
<code>M</code>	Input parameter <code>M</code>
<code>cands</code>	Matrix of dimensions <code>length(x) - 1</code> by 4. The first two columns are (start, end)-points of the detection intervals of the corresponding possible change-point location in the third column resulted from applying NOT to all threshold levels. The fourth column is a measure of strength of the corresponding possible change-point. The order of the rows reflect the strength of each detection in decreasing order. To avoid repetition, each possible location would appear at most once in the matrix (with the sub-interval that carries its highest possible strength)
<code>method</code>	The method used, which has value "not" here

References

R. Baranowski, Y. Chen & P. Fryzlewicz (2019). Narrowest-over-threshold detection of multiple change points and change-point-like features. *Journal of the Royal Statistical Society: Series B*, 81(3), 649–672.

See Also

[sol.idetect](#), [sol.tguh](#), [sol.wbs](#), [sol.wbs2](#)

Examples

```
r3 <- rnorm(1000) + c(rep(0,300), rep(2,200), rep(-4,300), rep(0,200))
sol.not(r3)
```

sol.tguh	<i>Solution path generation via the Tail-Greedy Unbalanced Haar method</i>
----------	--

Description

This function arranges all possible change-points in the mean of the input vector in the order of importance, via the Tail-Greedy Unbalanced Haar method.

Usage

```
sol.tguh(x, p = 0.01)
```

Arguments

x	A numeric vector containing the data to be processed
p	Specifies the number of region pairs merged in each pass through the data, as the proportion of all remaining region pairs. The default is $p = 0.01$

Details

The Tail-Greedy Unbalanced Haar decomposition algorithm is described in "Tail-greedy bottom-up data decompositions and fast multiple change-point detection", P. Fryzlewicz (2018), The Annals of Statistics, 46, 3390–3421.

Value

An S3 object of class `cptpath`, which contains the following fields:

<code>solutions.nested</code>	TRUE, i.e., the change-point outputs are nested
<code>solution.path</code>	Locations of possible change-points in the mean of <code>x</code> , arranged in decreasing order of change-point importance
<code>solution.set</code>	Empty list
<code>x</code>	Input vector <code>x</code>
<code>M</code>	Input parameter <code>M</code>

cands	Matrix of dimensions $\text{length}(x) - 1$ by 4. The first two columns are (start, end)-points of the detection intervals of the corresponding possible change-point location in the third column. The fourth column is a measure of strength of the corresponding possible change-point. The order of the rows is the same as the order returned in <code>solution.path</code>
method	The method used, which has value "tguh" here

References

P. Fryzlewicz (2018). Tail-greedy bottom-up data decompositions and fast multiple change-point detection. *The Annals of Statistics*, 46, 3390–3421.

See Also

[sol.idetect](#), [sol.idetect_seq](#), [sol.not](#), [sol.wbs](#), [sol.wbs2](#)

Examples

```
r3 <- rnorm(1000) + c(rep(0,300), rep(2,200), rep(-4,300), rep(0,200))
sol.tguh(r3)
```

sol.wbs

Solution path generation via the Wild Binary Segmentation method

Description

This function arranges all possible change-points in the mean of the input vector in the order of importance, via the Wild Binary Segmentation (WBS) method.

Usage

```
sol.wbs(x, M = 10000, systematic.intervals = TRUE, seed = NULL)
```

Arguments

x	A numeric vector containing the data to be processed
M	The maximum number of all data sub-samples at the beginning of the algorithm. The default is $M = 10000$
systematic.intervals	When drawing the sub-intervals, whether to use a systematic (and fixed) or random scheme. The default is <code>systematic.intervals = TRUE</code>
seed	If a random scheme is used, a random seed can be provided so that every time the same sets of random sub-intervals would be drawn. The default is <code>seed = NULL</code> , which means that this option is not taken

Details

The Wild Binary Segmentation algorithm is described in "Wild binary segmentation for multiple change-point detection", P. Fryzlewicz (2014), *The Annals of Statistics*, 42: 2243–2281.

Value

An S3 object of class `cptpath`, which contains the following fields:

<code>solutions.nested</code>	TRUE, i.e., the change-point outputs are nested
<code>solution.path</code>	Locations of possible change-points in the mean of <code>x</code> , arranged in decreasing order of change-point importance
<code>solution.set</code>	Empty list
<code>x</code>	Input vector <code>x</code>
<code>M</code>	Input parameter <code>M</code>
<code>cands</code>	Matrix of dimensions <code>length(x) - 1</code> by 4. The first two columns are (start, end)-points of the detection intervals of the corresponding possible change-point location in the third column. The fourth column is a measure of strength of the corresponding possible change-point. The order of the rows is the same as the order returned in <code>solution.path</code>
<code>method</code>	The method used, which has value "wbs" here

References

P. Fryzlewicz (2014). Wild binary segmentation for multiple change-point detection. *The Annals of Statistics*, 42(6), 2243–2281.

See Also

[sol.idetect](#), [sol.not](#), [sol.tguh](#), [sol.wbs2](#)

Examples

```
r3 <- rnorm(1000) + c(rep(0,300), rep(2,200), rep(-4,300), rep(0,200))
sol.wbs(r3)
```

sol.wbs2

Solution path generation via the Wild Binary Segmentation 2 method

Description

This function arranges all possible change-points in the mean of the input vector in the order of importance, via the Wild Binary Segmentation 2 method.

Usage

```
sol.wbs2(x, M = 1000, systematic.intervals = TRUE)
```

Arguments

x	A numeric vector containing the data to be processed.
M	The maximum number of data sub-samples drawn at each recursive stage of the algorithm. The default is $M = 1000$. Setting $M = 0$ executes the standard binary segmentation.
systematic.intervals	Whether data sub-intervals for CUSUM computation are drawn systematically (TRUE; start- and end-points taken from an approximately equispaced grid) or randomly (FALSE; obtained uniformly with replacement). The default is TRUE.

Details

The Wild Binary Segmentation 2 algorithm is described in "Detecting possibly frequent change-points: Wild Binary Segmentation 2 and steepest-drop model selection", P. Fryzlewicz (2020), *Journal of the Korean Statistical Society*, 49, 1027-1070.

Value

An S3 object of class `cptpath`, which contains the following fields:

solutions.nested	TRUE, i.e., the change-point outputs are nested
fmax	
solution.path	Locations of possible change-points in the mean of x , arranged in decreasing order of change-point importance
solution.set	Empty list
x	Input vector x
M	Input parameter M
cands	Matrix of dimensions $\text{length}(x) - 1$ by 4. The first two columns are (start, end)-points of the detection intervals of the corresponding possible change-point location in the third column. The fourth column is a measure of strength of the corresponding possible change-point. The order of the rows is the same as the order returned in <code>solution.path</code>
method	The method used, which has value "wbs2" here

References

P. Fryzlewicz (2020). Detecting possibly frequent change-points: Wild Binary Segmentation 2 and steepest-drop model selection. *Journal of the Korean Statistical Society*, 49, 1027-1070.

See Also

[sol.idetect](#), [sol.idetect_seq](#), [sol.not](#), [sol.tguh](#), [sol.wbs](#)

Examples

```
r3 <- rnorm(1000) + c(rep(0,300), rep(2,200), rep(-4,300), rep(0,200))
sol.wbs2(r3)
```

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