

# Package ‘bssn’

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**Type** Package

**Title** Birnbaum-Saunders Model

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**Imports** sn, ssmn, mvtnorm, ClusterR

**Description** It provides the density, distribution function, quantile function, random number generator, reliability function, failure rate, likelihood function, moments and EM algorithm for Maximum Likelihood estimators, also empirical quantile and generated envelope for a given sample, all this for the three parameter Birnbaum-Saunders model based on Skew-Normal Distribution. Also, it provides the random number generator for the mixture of Birnbaum-Saunders model based on Skew-Normal distribution. Additionally, we incorporate the EM algorithm based on the assumption that the error term follows a finite mixture of Sinh-normal distributions.

**License** GPL (>= 2)

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bssn-package

*Birnbaum-Saunders model*

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## Description

It provides the density, distribution function, quantile function, random number generator, reliability function, failure rate, likelihood function, moments and EM algorithm for Maximum Likelihood estimators, also empirical quantile and generated envelope for a given sample, all this for the three parameter Birnbaum-Saunders model based on Skew-Normal Distribution. Also, it provides the random number generator for the mixture of Birbaum-Saunders model based on Skew-Normal distribution. Additionally, we incorporate the EM algorithm based on the assumption that the error term follows a finite mixture of Sinh-normal distributions.

## Details

Package: bssn  
Type: Package  
Version: 1.5  
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License: GPL (>=2)

## Author(s)

Rocio Maehara <rmaeharaa@gmail.com> and Luis Benites <lbenitesanchez@gmail.com>

## References

Vilca, Filidor; Santana, L. R.; Leiva, Victor; Balakrishnan, N. (2011). Estimation of extreme percentiles in Birnbaum Saunders distributions. Computational Statistics & Data Analysis (Print), 55, 1665-1678.

Santana, Lucia; Vilca, Filidor; Leiva, Victor (2011). Influence analysis in skew-Birnbaum Saunders regression models and applications. Journal of Applied Statistics, 38, 1633-1649.

## See Also

[bssn](#), [EMbssn](#), [momentsbssn](#), [ozone](#), [reliabilitybssn](#), [FMshnReg](#)

## Examples

#See examples for the bssnEM function linked above.

**Description**

It provides the density, distribution function, quantile function, random number generator, likelihood function, moments and EM algorithm for Maximum Likelihood estimators for a given sample, all this for the three parameter Birnbaum-Saunders model based on Skew-Normal Distribution. Also, we have the random number generator for the mixture of Birbaum-Saunders model based on Skew-Normal distribution. Finally, the function `mmmeth()` is used to find the initial values for the parameters  $\alpha$  and  $\beta$  using modified-moment method.

**Usage**

```
dbssn(ti, alpha=0.5, beta=1, lambda=1.5)
pbssn(q, alpha=0.5, beta=1, lambda=1.5)
qbssn(p, alpha=0.5, beta=1, lambda=1.5)
rbssn(n, alpha=0.5, beta=1, lambda=1.5)
rmixbssn(n, alpha, beta, lambda, pii)
mmmeth(ti)
```

**Arguments**

<code>ti</code>	vector of observations.
<code>q</code>	vector of quantiles.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations.
<code>alpha</code>	shape parameter.
<code>beta</code>	scale parameter.
<code>lambda</code>	skewness parameter.
<code>pii</code>	Are weights adding to 1. Each one of them ( $\alpha$ , $\beta$ and $\lambda$ ) must be a vector of length $g$ if you want to generate a random numbers from a mixture distribution BSSN.

**Details**

If  $\alpha$ ,  $\sigma$  or  $\lambda$  are not specified they assume the default values of 0.5, 1 and 1.5, respectively, belonging to the Birnbaum-Saunders model based on Skew-Normal distribution denoted by  $BSSN(0.5, 1, 1.5)$ .

As discussed in Filidor et. al (2011) we say that a random variable  $T$  is distributed as an BSSN with shape parameter  $\alpha > 0$ , scale parameter  $\beta > 0$  and skewness parameter  $\lambda$  in  $R$ , if its probability density function (pdf) is given by

$$f(t) = 2\phi(a(t; \alpha, \beta))\Phi(\lambda a(t; \alpha, \beta))A(t; \alpha, \beta), t > 0$$

where  $\phi(\cdot)$  and  $\Phi(\cdot)$  are the standard normal density and cumulative distribution function respectively. Also  $a(t; \alpha, \beta) = (1/\alpha)(\sqrt{t/\beta} - \sqrt{\beta/t})$  and  $A(t; \alpha, \beta) = t^{-3/2}(t + \beta)/(2\alpha\beta^{1/2})$

**Value**

dbssn gives the density, pbssn gives the distribution function, qbssn gives the quantile function, rbssn generates a random sample and rmixbssn generates a mixture random sample.

The length of the result is determined by n for rbssn, and is the maximum of the lengths of the numerical arguments for the other functions dbssn, pbssn and qbssn.

**Author(s)**

Rocio Maehara <rmaeharaa@gmail.com> and Luis Benites <lbenitesanchez@gmail.com>

**References**

Vilca, Filidor; Santana, L. R.; Leiva, Victor; Balakrishnan, N. (2011). Estimation of extreme percentiles in Birnbaum Saunders distributions. *Computational Statistics & Data Analysis (Print)*, 55, 1665-1678.

Santana, Lucia; Vilca, Filidor; Leiva, Victor (2011). Influence analysis in skew-Birnbaum Saunders regression models and applications. *Journal of Applied Statistics*, 38, 1633-1649.

**See Also**

[EMbssn](#), [momentsbssn](#), [ozone](#), [reliabilitybssn](#)

**Examples**

```
## Not run:
## Let's plot an Birnbaum-Saunders model based on Skew-Normal distribution!

## Density
sseq <- seq(0,3,0.01)
dens <- dbssn(sseq,alpha=0.2,beta=1,lambda=1.5)
plot(sseq, dens,type="l", lwd=2,col="red", xlab="x", ylab="f(x)", main="BSSN Density function")

# Differing densities on a graph
# positive values of lambda
y <- seq(0,3,0.01)
f1 <- dbssn(y,0.2,1,1)
f2 <- dbssn(y,0.2,1,2)
f3 <- dbssn(y,0.2,1,3)
f4 <- dbssn(y,0.2,1,4)
den <- cbind(f1,f2,f3,f4)

matplot(y,den,type="l", col=c("deepskyblue4", "firebrick1", "darkmagenta", "aquamarine4"), ylab
="Density function",xlab="y",lwd=2,sub="(a)")

legend(1.5,2.8,c("BSSN(0.2,1,1)", "BSSN(0.2,1,2)", "BSSN(0.2,1,3)", "BSSN(0.2,1,4)"),
col = c("deepskyblue4", "firebrick1", "darkmagenta", "aquamarine4"), lty=1:4,lwd=2,
seg.len=2,cex=0.8,box.lty=0,bg=NULL)

#negative values of lambda
```

```

y <- seq(0,3,0.01)
f1 <- dbssn(y,0.2,1,-1)
f2 <- dbssn(y,0.2,1,-2)
f3 <- dbssn(y,0.2,1,-3)
f4 <- dbssn(y,0.2,1,-4)
den <- cbind(f1,f2,f3,f4)

matplot(y,den,type="l", col=c("deepskyblue4", "firebrick1", "darkmagenta", "aquamarine4"),
ylab ="Density function",xlab="y",lwd=2,sub="(a)")
legend(1.5,2.8,c("BSSN(0.2,1,-1)", "BSSN(0.2,1,-2)", "BSSN(0.2,1,-3)", "BSSN(0.2,1,-4)"),
col=c("deepskyblue4", "firebrick1", "darkmagenta", "aquamarine4"),lty=1:4,lwd=2,seg.len=2,
cex=1,box.lty=0,bg=NULL)

## Distribution Function
sseq <- seq(0.1,6,0.05)
df <- pbssn(q=sseq,alpha=0.75,beta=1,lambda=3)
plot(sseq, df, type = "l", lwd=2, col="blue", xlab="x", ylab="F(x)",
main = "BSSN Distribution function")
abline(h=1,lty=2)

#Inverse Distribution Function
prob <- seq(0,1,length.out = 1000)
idf <- qbssn(p=prob,alpha=0.75,beta=1,lambda=3)
plot(prob, idf, type="l", lwd=2, col="gray30", xlab="x", ylab =
expression(F^{-1}~(x)), mgp=c(2.3,1,.8))
title(main="BSSN Inverse Distribution function")
abline(v=c(0,1),lty=2)

#Random Sample Histogram
sample <- rbssn(n=10000,alpha=0.75,beta=1,lambda=3)
hist(sample,breaks = 70,freq = FALSE,main="")
title(main="Histogram and True density")
sseq <- seq(0,8,0.01)
dens <- dbssn(sseq,alpha=0.75,beta=1,lambda=3)
lines(sseq,dens,col="red",lwd=2)

##Random Sample Histogram for Mixture of BSSN
alpha=c(0.55,0.25);beta=c(1,1.5);lambda=c(3,2);pii=c(0.3,0.7)
sample <- rmixbssn(n=1000,alpha,beta,lambda,pii)
hist(sample$y,breaks = 70,freq = FALSE,main="")
title(main="Histogram and True density")
temp <- seq(min(sample$y), max(sample$y), length.out=1000)
lines(temp, (pii[1]*dbssn(temp, alpha[1], beta[1],lambda[1]))+(pii[2]*dbssn(temp, alpha[2],
beta[2],lambda[2])), col="red", lty=3, lwd=3) # the theoretical density
lines(temp, pii[1]*dbssn(temp, alpha[1], beta[1],lambda[1]), col="blue", lty=2, lwd=3)
# the first component
lines(temp, pii[2]*dbssn(temp, alpha[2], beta[2],lambda[2]), col="green", lty=2, lwd=3)
# the second component

```

```
## End(Not run)
```

---

EMbssn	<i>EM Algorithm Birnbaum-Saunders model based on Skew-Normal distribution</i>
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---

## Description

Performs the EM algorithm for Birnbaum-Saunders model based on Skew-Normal distribution.

## Usage

```
EMbssn(ti,alpha,beta,delta,initial.values=FALSE, loglik=F,accuracy=1e-8,
show.envelope="FALSE",iter.max=500)
```

## Arguments

ti	Vector of observations.
alpha,beta,delta	Initial values.
initial.values	Logical; if TRUE, get the initial values for the parameters.
loglik	Logical; if TRUE, showvalue of the log-likelihood.
accuracy	The convergence maximum error.
show.envelope	Logical; if TRUE, show the simulated envelope for the fitted model.
iter.max	The maximum number of iterations of the EM algorithm

## Value

The function returns a list with 11 elements detailed as

iter	Number of iterations.
alpha	Returns the value of the MLE of the shape parameter.
beta	Returns the value of the MLE of the scale parameter.
lambda	Returns the value of the MLE of the skewness parameter.
SE	Standard Errors of the ML estimates.
table	Table containing the ML estimates with the corresponding standard errors.
loglik	Log-likelihood.
AIC	Akaike information criterion.
BIC	Bayesian information criterion.
HQC	Hannan-Quinn information criterion.
time	processing time.

**Author(s)**

Rocio Maehara <rmaeharaa@gmail.com> and Luis Benites <lbenitesanchez@gmail.com>

**References**

Vilca, Filidor; Santana, L. R.; Leiva, Victor; Balakrishnan, N. (2011). Estimation of extreme percentiles in Birnbaum Saunders distributions. *Computational Statistics & Data Analysis (Print)*, 55, 1665-1678.

Santana, Lucia; Vilca, Filidor; Leiva, Victor (2011). Influence analysis in skew-Birnbaum Saunders regression models and applications. *Journal of Applied Statistics*, 38, 1633-1649.

**See Also**

[bssn](#), [EMbssn](#), [momentsbssn](#), [ozone](#), [reliabilitybssn](#)

**Examples**

```
## Not run:
#Using the ozone data

data(ozone)
attach(ozone)

#####
#The model
ti      <- dailyozonelevel

#Initial values for the parameters
initial <- mmmeth(ti)
alpha0  <- initial$alpha0ini
beta0   <- initial$beta0init
lambda0 <- 0
delta0  <- lambda0/sqrt(1+lambda0^2)

#Estimated parameters of the model (by default)
est_param <- EMbssn(ti,alpha0,beta0,delta0,loglik=T,
  accuracy = 1e-8,show.envelope = "TRUE", iter.max=500)

#ML estimates
alpha    <- est_param$res$alpha
beta    <- est_param$res$beta
lambda  <- est_param$res$lambda

#####
#A simple output example

-----
Birnbaum-Saunders model based on Skew-Normal distribution
-----
```

```

Observations = 116
-----
Estimates
-----

      Estimate Std. Error z value Pr(>|z|)
alpha  1.26014    0.23673  5.32311  0.00000
beta   14.65730    4.01984  3.64624  0.00027
lambda  1.06277    0.54305  1.95706  0.05034
-----
Model selection criteria
-----

      Loglik  AIC  BIC  HQC
Value -542.768 4.705 4.741 4.719
-----
Details
-----

Iterations = 415
Processing time = 0.4283214 secs
Convergence = TRUE

## End(Not run)

```

---

enzyme

*Enzymatic activity in the blood*

---

### Description

These data correspond to representing the metabolism of carcinogenic substances among 245 unrelated individuals.

### Usage

```
data(enzyme)
```

### Format

enzyme is a data frame with 245 cases (rows).

### Details

For more information about dataset see Bechtel et al. (1993).

### Source

Bechtel, Y., Bonaiti-Pellie, C., Poisson, N., Magnette, J. and Bechtel, P. (1993). A population and family study of n-acetyltransferase using caffeine urinary metabolites. *Clinical Pharmacology and Therapeutics*, 54, 134-141.



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FMshnReg	<i>Linear regression models using finite mixture of Sinh-normal distribution</i>
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---

### Description

Performs the EM-type algorithm with conditional maximization to perform maximum likelihood inference of the parameters of the proposed model based on the assumption that the error term follows a finite mixture of Sinh-normal distributions.

### Usage

```
FMshnReg(y, x1, alpha = NULL, Abetas = NULL, medj=NULL,
  pii = NULL, g = NULL, get.init = TRUE, algorithm = "K-means",
  accuracy = 10^-6, show.envelope="FALSE", iter.max = 100)
```

### Arguments

y	the response matrix (dimension nx1).
x1	Matrix or vector of covariates.
alpha	Value of the shape parameter for the EM algorithm. Each of them must be a vector of length g. (the algorithm considers the number of components to be adjusted based on the size of these vectors).
Abetas	Parameters of vector regression dimension ( $p + 1$ ) include intercept.
medj	a list of g arguments of vectors of values (dimension p) for the location parameters.
pii	Value for the EM algorithm. Each of them must be a vector of length g. (the algorithm considers the number of components to be adjusted based on the size of these vectors).
g	The number of cluster to be considered in fitting.
get.init	if TRUE, the initial values are generated via k-means.
algorithm	clustering procedure of a series of vectors according to a criterion. The clustering algorithms may classified in 4 main categories: exclusive, overlapping, hierarchical and probabilistic.
accuracy	The convergence maximum error.
show.envelope	Logical; if TRUE, show the simulated envelope for the fitted model.
iter.max	The maximum number of iterations of the EM algorithm

### Value

The function returns a list with 10 elements detailed as

iter	Number of iterations.
criteria	Attained criteria value.

convergence	Convergence reached or not.
SE	Standard Error estimates, if the output shows NA the function does not provide the standard error for this parameter.
table	Table containing the inference for the estimated parameters.
LK	log-likelihood.
AIC	Akaike information criterion.
BIC	Bayesian information criterion.
EDC	Efficient Determination criterion.
time	Processing time.

### Author(s)

Rocio Maehara <rmaeharaa@gmail.com> and Luis Benites <lbenitesanchez@gmail.com>

### References

Maehara, R. and Benites, L. (2020). Linear regression models using finite mixture of Sinh-normal distribution. In Progress.

Bartolucci, F. and Scaccia, L. (2005). The use of mixtures for dealing with non-normal regression errors, Computational Statistics & Data Analysis 48(4): 821-834.

### Examples

```
## Not run:
#Using the AIS data

library(FMsmsnReg)
data(ais)

#####
#The model
x1  <- cbind(1,ais$SSF,ais$Ht)
y   <- ais$Bfat

library(ClusterR) #This library is useful for using the k-medoids algorithm.

FMshnReg(y, x1, get.init = TRUE, g=2, algorithm="k-medoids",
accuracy = 10^-6, show.envelope="FALSE", iter.max = 1000)

#####
#A simple output example

-----
Finite Mixture of Sinh Normal Regression Model
-----

Observations = 202

-----
```

## Estimates

-----

	Estimate	SE
alpha1	0.81346	0.10013
alpha2	3.04894	0.32140
beta0	15.08998	1.70024
beta1	0.17708	0.00242
beta2	-0.07687	0.00934
mu1	-0.25422	0.18069
mu2	0.37944	0.38802
pii1	0.59881	0.41006

## Model selection criteria

-----

	Loglik	AIC	BIC	EDC
Value	-355.625	721.25	737.791	725.463

-----

## Details

-----

Convergence reached? = TRUE  
 EM iterations = 39 / 1000  
 Criteria = 6.58e-07  
 Processing time = 0.725559 secs

## End(Not run)

---

momentsbssn

*Moments for the Birnbaum-Saunders model based on Skew-Normal distribution*


---

**Description**

Mean, variance, skewness and kurtosis for the Birnbaum-Saunders model based on Skew-Normal distribution defined in Filidor et. al (2011).

**Usage**

```
meanbssn(alpha=0.5,beta=1,lambda=1.5)
varbssn(alpha=0.5,beta=1,lambda=1.5)
skewbssn(alpha=0.5,beta=1,lambda=1.5)
kurtbssn(alpha=0.5,beta=1,lambda=1.5)
```

**Arguments**

alpha	shape parameter $\alpha$ .
beta	scale parameter $\beta$ .
lambda	skewness parameter $\lambda$ .

**Value**

meanbssn gives the mean, varbssn gives the variance, skewbssn gives the skewness, kurtbssn gives the kurtosis.

**Author(s)**

Rocio Maehara <rmaeharaa@gmail.com> and Luis Benites <lbenitesanchez@gmail.com>

**References**

Vilca, Filidor; Santana, L. R.; Leiva, Victor; Balakrishnan, N. (2011). Estimation of extreme percentiles in Birnbaum Saunders distributions. *Computational Statistics & Data Analysis (Print)*, 55, 1665-1678.

Santana, Lucia; Vilca, Filidor; Leiva, Victor (2011). Influence analysis in skew-Birnbaum Saunders regression models and applications. *Journal of Applied Statistics*, 38, 1633-1649.

**See Also**

[bssn](#), [EMbssn](#), [momentsbssn](#), [ozone](#), [reliabilitybssn](#)

**Examples**

```
## Let's compute some moments for a Birnbaum-Saunders model based on Skew normal Distribution.
# The well known mean, variance, skewness and kurtosis
meanbssn(alpha=0.5,beta=1,lambda=1.5)
varbssn(alpha=0.5,beta=1,lambda=1.5)
skewbssn(alpha=0.5,beta=1,lambda=1.5)
kurtbssn(alpha=0.5,beta=1,lambda=1.5)
```

---

ozone

*Daily ozone level measurements*

---

**Description**

These data correspond to daily ozone level measurements (in *ppb* = *ppm.x1000*) in New York in May-September, 1973, from the New York State Department of Conservation.

**Usage**

data(ozone)

**Format**

ozone is a data frame with 116 cases (rows).

**Details**

For a complete description of various distributions applied to data concentration of air pollutants see Gokhale and Khare (2004).

**Source**

Leiva, V., Barros, M., Paula, G. e Sanhueza, A. (2007). Generalized BirnbaumSaunders distribution applied to air pollutant concentration. *Environmetrics*, 19, 235-249.

Nadarajah, S. (2007). A truncated inverted beta distribution with application to air pollution data. *Stoch. Environ. Res. Risk. Assess.*, 22, 285-289.

Gokhale, S. e Khare, M. (2004) A review of deterministic, stochastic and hybrid vehicular exhaust emission models *International. J. Transp. Manag.*, 2, 59-74.

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reliabilitybssn	<i>Reliability Function for the Birnbaum-Saunders model based on Skew-Normal distribution</i>
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---

**Description**

Two useful descriptors in reliability analysis are the reliability function (rf), and the failure rate (fr) function or hazard function. For a non-negative random variable  $t$  with pdf  $f(t)$  (and cdf  $F(t)$ ), its distribution can be characterized equally in terms of the rf, or of the fr, which are respectively defined by  $R(t) = 1 - F(t)$ , and  $h(t) = f(t)/R(t)$ , for  $t > 0$ , and  $0 < R(t) < 1$ .

**Usage**

```
Rebssn(ti, alpha=0.5, beta=1, lambda=1.5)
Fbssn(ti, alpha=0.5, beta=1, lambda=1.5)
```

**Arguments**

ti	dataset.
alpha	shape parameter $\alpha$ .
beta	scale parameter $\beta$ .
lambda	skewness parameter $\lambda$ .

**Value**

Rebssn gives the reliability function, Fbssn gives the failure rate or hazard function.

**Author(s)**

Rocio Maehara <rmaeharaa@gmail.com> and Luis Benites <lbenitesanchez@gmail.com>

## References

Leiva, V., Vilca-Labra, F. E., Balakrishnan, N. e Sanhueza, A. (2008). A skewed sinh-normal distribution and its properties and application to air pollution. *Comm. Stat. Theoret. Methods*. Submetido.

Guiraud, P., Leiva, V., Fierro, R. (2009). A non-central version of the Birnbaum-Saunders distribution for reliability analysis. *IEEE Transactions on Reliability* 58, 152-160.

## See Also

[bssn](#), [EMbssn](#), [momentsbssn](#), [ozone](#), [Rebssn](#)

## Examples

```
## Let's compute some reliability functions for a Birnbaum-Saunders model based on
## Skew normal Distribution for different values of the shape parameter.
```

```
ti <- seq(0,2,0.01)
f1 <- Rebssn(ti,0.75,1,1)
f2 <- Rebssn(ti,1,1,1)
f3 <- Rebssn(ti,1.5,1,1)
f4 <- Rebssn(ti,2,1,1)
den <- cbind(f1,f2,f3,f4)
```

```
matplot(ti,den,type="l", col=c("deepskyblue4","firebrick1","darkmagenta","aquamarine4"),
ylab="S(t)", xlab="t",lwd=2)
legend(1.5,1,c(expression(alpha==0.75), expression(alpha==1), expression(alpha==1.5),
expression(alpha==2)),col= c("deepskyblue4","firebrick1","darkmagenta","aquamarine4"),
lty=1:4,lwd=2,seg.len=2,cex=0.9,box.lty=0,bg=NULL)
```

```
## Let's compute some hazard functions for a Birnbaum Saunders model based on
## Skew normal Distribution for different values of the skewness parameter.
```

```
ti <- seq(0,2,0.01)
f1 <- Fbssn(ti,0.5,1,-1)
f2 <- Fbssn(ti,0.5,1,-2)
f3 <- Fbssn(ti,0.5,1,-3)
f4 <- Fbssn(ti,0.5,1,-4)
den <- cbind(f1,f2,f3,f4)
matplot(ti,den,type = "l", col = c("deepskyblue4","firebrick1", "darkmagenta", "aquamarine4"),
ylab = "h(t)" , xlab="t",lwd=2)
legend(0.1,23, c(expression(lambda==1), expression(lambda==2), expression(lambda == -3),
expression(lambda == -4)), col = c("deepskyblue4", "firebrick1", "darkmagenta","aquamarine4"),
lty=1:4,lwd=2,seg.len=2,cex=0.9,box.lty=1,bg=NULL)
```

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