Package 'estimatr'

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Type Package

Title Fast Estimators for Design-Based Inference

Version 1.0.0

Description Fast procedures for small set of commonly-used, design-appropriate estimators with robust standard errors and confidence intervals. Includes estimators for linear regression, instrumental variables regression, difference-in-means, Horvitz-Thompson estimation, and regression improving precision of experimental estimates by interacting treatment with centered pretreatment covariates introduced by Lin (2013) <doi:10.1214/12-AOAS583>.

URL https://declaredesign.org/r/estimatr/,

https://github.com/DeclareDesign/estimatr

BugReports https://github.com/DeclareDesign/estimatr/issues

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Depends R (>= 3.5.0)

Imports Formula, generics, methods, Rcpp (>= 0.12.16), rlang (>= 0.2.0)

LinkingTo Rcpp, RcppEigen

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LazyData true

Suggests fabricatr (>= 0.10.0), randomizr (>= 0.20.0), AER, clubSandwich, emmeans (>= 1.4), estimability, margins, modelsummary, prediction, RcppEigen, sandwich, stargazer, testthat, car

Enhances texreg

NeedsCompilation yes

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R topics documented:

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alo_star_men   *Replication data for Lin 2013*

Description

A dataset containing the data to replicate: Lin, Winston. 2013. "Agnostic notes on regression adjustments to experimental data: Reexamining Freedman's critique." The Annals of Applied Statistics. Stat. 7(1): 295-318. doi:10.1214/12-AOAS583. https://projecteuclid.org/euclid.aoas/1365527200.

Usage

```
alo_star_men
```

Format

A data frame with educational treatments and outcomes:

gpa0 high school GPA

sfsp financial incentives and support treatment

ssp support only treatment

GPA_year1 college GPA year 1

GPA_year2 college GPA year 2

Details

This data was originally taken from the following paper, subset to men who showed up to college, were in one of the arms with the support condition, and had GPA data for their first year in college.

Angrist, Joshua, Daniel Lang, and Philip Oreopoulos. 2009. "Incentives and Services for College Achievement: Evidence from a Randomized Trial." American Economic Journal: Applied Economics 1(1): 136-63. https://www.aeaweb.org/articles?id=10.1257/app.1.1.136

Source

https://www.aeaweb.org/articles?id=10.1257/app.1.1.136

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commarobust	*Build lm_robust object from lm fit*

Description

Build lm_robust object from lm fit

Usage

```
commarobust(model, se_type = NULL, clusters = NULL, ci = TRUE, alpha = 0.05)
```

Arguments

model	an lm model object
se_type	The sort of standard error sought. If `clusters` is not specified the options are "HC0", "HC1" (or "stata", the equivalent), "HC2" (default), "HC3", or "classical". If `clusters` is specified the options are "CR0", "CR2" (default), or "stata". Can also specify "none", which may speed up estimation of the coefficients.
clusters	A vector corresponding to the clusters in the data.
ci	logical. Whether to compute and return p-values and confidence intervals, TRUE by default.
alpha	The significance level, 0.05 by default.

Value

an [lm_robust](#) object.

Examples

```
lmo <- lm(mpg ~ hp, data = mtcars)

# Default HC2
commarobust(lmo)

commarobust(lmo, se_type = "HC3")

commarobust(lmo, se_type = "stata", clusters = mtcars$carb)
```

---

declaration_to_condition_pr_mat

Builds condition probability matrices for Horvitz-Thompson estima-
tion from **randomizr** *declaration*

Description

Builds condition probability matrices for Horvitz-Thompson estimation from **randomizr** declaration

Usage

```
declaration_to_condition_pr_mat(
  ra_declaration,
  condition1 = NULL,
  condition2 = NULL,
  prob_matrix = NULL
)
```

Arguments

ra_declaration   An object of class "ra_declaration", generated by the [declare_ra](#) function
                 in **randomizr**. This object contains the experimental design that will be repre-
                 sented in a condition probability matrix

condition1   The name of the first condition, often the control group. If NULL, defaults to first
                 condition in randomizr declaration. Either both condition1 and condition2
                 have to be specified or both left as NULL.

condition2   The name of the second condition, often the treatment group. If NULL, de-
                 faults to second condition in randomizr declaration. Either both condition1
                 and condition2 have to be specified or both left as NULL.

prob_matrix   An optional probability matrix to override the one in ra_declaration

Details

This function takes a "ra_declaration", generated by the [declare_ra](#) function in **randomizr** and returns a 2n*2n matrix that can be used to fully specify the design for [horvitz_thompson](#) estimation. This is done by passing this matrix to the condition_pr_mat argument of [horvitz_thompson](#).

Currently, this function can learn the condition probability matrix for a wide variety of randomizations: simple, complete, simple clustered, complete clustered, blocked, block-clustered.

A condition probability matrix is made up of four submatrices, each of which corresponds to the joint and marginal probability that each observation is in one of the two treatment conditions.

The upper-left quadrant is an n*n matrix. On the diagonal is the marginal probability of being in condition 1, often control, for every unit ($Pr(Z_i = Condition1)$ where Z represents the vector of treatment conditions). The off-diagonal elements are the joint probabilities of each unit being in condition 1 with each other unit, $Pr(Z_i = Condition1, Z_j = Condition1)$ where i indexes the rows and j indexes the columns.

The upper-right quadrant is also an n*n matrix. On the diagonal is the joint probability of a unit being in condition 1 and condition 2, often the treatment, and thus is always 0. The off-diagonal elements are the joint probability of unit i being in condition 1 and unit j being in condition 2, $Pr(Z_i = Condition1, Z_j = Condition2)$.

The lower-left quadrant is also an n*n matrix. On the diagonal is the joint probability of a unit being in condition 1 and condition 2, and thus is always 0. The off-diagonal elements are the joint probability of unit i being in condition 2 and unit j being in condition 1, $Pr(Z_i = Condition2, Z_j = Condition1)$.

The lower-right quadrant is an n*n matrix. On the diagonal is the marginal probability of being in condition 2, often treatment, for every unit ($Pr(Z_i = Condition2)$). The off-diagonal elements are the joint probability of each unit being in condition 2 together, $Pr(Z_i = Condition2, Z_j = Condition2)$.

Value

a numeric 2n*2n matrix of marginal and joint condition treatment probabilities to be passed to the condition_pr_mat argument of [horvitz_thompson](#). See details.

See Also

[permutations_to_condition_pr_mat](#)

Examples

```
# Learn condition probability matrix from complete blocked design
library(randomizr)
n <- 100
dat <- data.frame(
  blocks = sample(letters[1:10], size = n, replace = TRUE),
  y = rnorm(n)
)

# Declare complete blocked randomization
bl_declaration <- declare_ra(blocks = dat$blocks, prob = 0.4, simple = FALSE)
```

```
# Get probabilities
block_pr_mat <- declaration_to_condition_pr_mat(bl_declaration, 0, 1)
# Do randomiztion
dat$z <- conduct_ra(bl_declaration)

horvitz_thompson(y ~ z, data = dat, condition_pr_mat = block_pr_mat)

# When you pass a declaration to horvitz_thompson, this function is called

# Equivalent to above call
horvitz_thompson(y ~ z, data = dat, ra_declaration = bl_declaration)
```

---

difference_in_means   *Design-based difference-in-means estimator*

Description

Difference-in-means estimators that selects the appropriate point estimate, standard errors, and degrees of freedom for a variety of designs: unit randomized, cluster randomized, block randomized, block-cluster randomized, matched-pairs, and matched-pair cluster randomized designs

Usage

```
difference_in_means(
  formula,
  data,
  blocks,
  clusters,
  weights,
  subset,
  se_type = c("default", "none"),
  condition1 = NULL,
  condition2 = NULL,
  ci = TRUE,
  alpha = 0.05
)
```

Arguments

formula   an object of class formula, as in [lm](#), such as Y ~ Z with only one variable on the
               right-hand side, the treatment.

data   A data.frame.

blocks   An optional bare (unquoted) name of the block variable. Use for blocked designs
               only.

clusters   An optional bare (unquoted) name of the variable that corresponds to the clusters
               in the data; used for cluster randomized designs. For blocked designs, clusters
               must nest within blocks.

weights	the bare (unquoted) names of the weights variable in the supplied data.
subset	An optional bare (unquoted) expression specifying a subset of observations to be used.
se_type	An optional string that can be one of c("default", "none"). If "default" (the default), it will use the default standard error estimator for the design, and if "none" then standard errors will not be computed which may speed up run time if only the point estimate is required.
condition1	value in the treatment vector of the condition to be the control. Effects are estimated with condition1 as the control and condition2 as the treatment. If unspecified, condition1 is the "first" condition and condition2 is the "second" according to levels if the treatment is a factor or according to a sortif it is a numeric or character variable (i.e if unspecified and the treatment is 0s and 1s, condition1 will by default be 0 and condition2 will be 1). See the examples for more.
condition2	value in the treatment vector of the condition to be the treatment. See condition1.
ci	logical. Whether to compute and return p-values and confidence intervals, TRUE by default.
alpha	The significance level, 0.05 by default.

Details

This function implements a difference-in-means estimator, with support for blocked, clustered, matched-pairs, block-clustered, and matched-pair clustered designs. One specifies their design by passing the blocks and clusters in their data and this function chooses which estimator is most appropriate.

If you pass only blocks, if all blocks are of size two, we will infer that the design is a matched-pairs design. If they are all size four or larger, we will infer that it is a regular blocked design. If you pass both blocks and clusters, we will similarly infer whether it is a matched-pairs clustered design or a block-clustered design the number of clusters per block. If the user passes only clusters, we will infer that the design was cluster-randomized. If the user specifies neither the blocks nor the clusters, a regular Welch's t-test will be performed.

Importantly, if the user specifies weights, the estimation is handed off to [lm_robust](#) with the appropriate robust standard errors as weighted difference-in-means estimators are not implemented here. More details of the about each of the estimators can be found in the [mathematical notes](#).

Value

Returns an object of class "difference_in_means".

The post-estimation commands functions summary and [tidy](#) return results in a data.frame. To get useful data out of the return, you can use these data frames, you can use the resulting list directly, or you can use the generic accessor functions coef and confint.

An object of class "difference_in_means" is a list containing at least the following components:

coefficients	the estimated difference in means
std.error	the estimated standard error
statistic	the t-statistic

df	the estimated degrees of freedom
p.value	the p-value from a two-sided t-test using `coefficients`, `std.error`, and `df`
conf.low	the lower bound of the 1 - alpha percent confidence interval
conf.high	the upper bound of the 1 - alpha percent confidence interval
term	a character vector of coefficient names
alpha	the significance level specified by the user
N	the number of observations used
outcome	the name of the outcome variable
design	the name of the design learned from the arguments passed

References

Gerber, Alan S, and Donald P Green. 2012. Field Experiments: Design, Analysis, and Interpretation. New York: W.W. Norton.

Imai, Kosuke, Gary King, Clayton Nall. 2009. "The Essential Role of Pair Matching in Cluster-Randomized Experiments, with Application to the Mexican Universal Health Insurance Evaluation." Statistical Science 24 (1). Institute of Mathematical Statistics: 29-53. doi:10.1214/08STS274.

See Also

[lm_lin](#)

Examples

```
library(fabricatr)
library(randomizr)
# Get appropriate standard errors for unit-randomized designs

# ----------
# 1. Unit randomized
# ----------
dat <- fabricate(
  N = 100,
  Y = rnorm(100),
  Z_comp = complete_ra(N, prob = 0.4),
)

table(dat$Z_comp)
difference_in_means(Y ~ Z_comp, data = dat)

# ----------
# 2. Cluster randomized
# ----------
# Accurates estimates and standard errors for clustered designs
dat$clust <- sample(20, size = nrow(dat), replace = TRUE)
dat$Z_clust <- cluster_ra(dat$clust, prob = 0.6)
```

```
table(dat$Z_clust, dat$clust)
summary(difference_in_means(Y ~ Z_clust, clusters = clust, data = dat))

# ----------
# 3. Block randomized
# ----------
dat$block <- rep(1:10, each = 10)
dat$Z_block <- block_ra(dat$block, prob = 0.5)

table(dat$Z_block, dat$block)
difference_in_means(Y ~ Z_block, blocks = block, data = dat)

# ----------
# 4. Block cluster randomized
# ----------
# Learns this design if there are two clusters per block
dat$small_clust <- rep(1:50, each = 2)
dat$big_blocks <- rep(1:5, each = 10)

dat$Z_blcl <- block_and_cluster_ra(
  blocks = dat$big_blocks,
  clusters = dat$small_clust
 )

difference_in_means(
  Y ~ Z_blcl,
  blocks = big_blocks,
  clusters = small_clust,
  data = dat
 )

# ----------
# 5. Matched-pairs
# ----------
# Matched-pair estimates and standard errors are also accurate
# Specified same as blocked design, function learns that
# it is matched pair from size of blocks!
dat$pairs <- rep(1:50, each = 2)
dat$Z_pairs <- block_ra(dat$pairs, prob = 0.5)

table(dat$pairs, dat$Z_pairs)
difference_in_means(Y ~ Z_pairs, blocks = pairs, data = dat)

# ----------
# 6. Matched-pair cluster randomized
# ----------
# Learns this design if there are two clusters per block
dat$small_clust <- rep(1:50, each = 2)
dat$cluster_pairs <- rep(1:25, each = 4)
table(dat$cluster_pairs, dat$small_clust)

dat$Z_mpcl <- block_and_cluster_ra(
  blocks = dat$cluster_pairs,
```

```
  clusters = dat$small_clust
 )

difference_in_means(
  Y ~ Z_mpcl,
  blocks = cluster_pairs,
  clusters = small_clust,
  data = dat
 )

# ----------
# Other examples
# ----------

# Also works with multi-valued treatments if users specify
# comparison of interest
dat$Z_multi <- simple_ra(
  nrow(dat),
  conditions = c("Treatment 2", "Treatment 1", "Control"),
  prob_each = c(0.4, 0.4, 0.2)
)

# Only need to specify which condition is treated `condition2` and
# which is control `condition1`
difference_in_means(
  Y ~ Z_multi,
  condition1 = "Treatment 2",
  condition2 = "Control",
  data = dat
)
difference_in_means(
  Y ~ Z_multi,
  condition1 = "Treatment 1",
  condition2 = "Control",
  data = dat
)

# Specifying weights will result in estimation via lm_robust()
dat$w <- runif(nrow(dat))
difference_in_means(Y ~ Z_comp, weights = w, data = dat)
lm_robust(Y ~ Z_comp, weights = w, data = dat)
```

---

estimatr   *estimatr*

Description

Fast procedures for small set of commonly-used, design-appropriate estimators with robust standard
errors and confidence intervals. Includes estimators for linear regression, instrumental variables re-
gression, difference-in-means, Horvitz-Thompson estimation, and regression improving precision

of experimental estimates by interacting treatment with centered pre-treatment covariates introduced by Lin (2013) <doi:10.1214/12-AOAS583>.

---

estimatr_glancers   *Glance at an estimatr object*

Description

Glance at an estimatr object

Usage

```
## S3 method for class 'lm_robust'
glance(x, ...)

## S3 method for class 'lh_robust'
glance(x, ...)

## S3 method for class 'iv_robust'
glance(x, ...)

## S3 method for class 'difference_in_means'
glance(x, ...)

## S3 method for class 'horvitz_thompson'
glance(x, ...)
```

Arguments

x	An object returned by one of the estimators
...	extra arguments (not used)

Value

For `glance.lm_robust`, a data.frame with columns:

r.squared	the R^2,

$$R^2 = 1 - Sum(e[i]^2)/Sum((y[i] - y^*)^2),$$

where y^* is the mean of $y[i]$ if there is an intercept and zero otherwise, and $e[i]$ is the ith residual.

adj.r.squared	the R^2 but penalized for having more parameters, rank
se_type	the standard error type specified by the user
statistic	the value of the F-statistic
p.value	p-value from the F test
df.residual	residual degrees of freedom

nobs   the number of observations used

For glance.lh_robust, we glance the lm_robust component only. You can access the linear hypotheses as a data.frame directy from the lh component of the lh_robust object

For glance.iv_robust, a data.frame with columns:

r.squared   The R^2 of the second stage regression

adj.r.squared   The R^2 but penalized for having more parameters, rank

df.residual   residual degrees of freedom

N   the number of observations used

se_type   the standard error type specified by the user

statistic   the value of the F-statistic

p.value   p-value from the F test

statistic.weakinst
                        the value of the first stage F-statistic, useful for the weak instruments test; only
                        reported if there is only one endogenous variable

p.value.weakinst
                        p-value from the first-stage F test, a test of weak instruments; only reported if
                        there is only one endogenous variable

statistic.endogeneity
                        the value of the F-statistic for the test of endogeneity; often called the Wu-
                        Hausman statistic, with robust standard errors, we employ the regression based
                        test

p.value.endogeneity
                        p-value from the F-test for endogeneity

statistic.overid
                        the value of the chi-squared statistic for the test of instrument correlation with
                        the error term; only reported with overidentification

p.value.overid   p-value from the chi-squared test; only reported with overidentification

For glance.difference_in_means, a data.frame with columns:

design   the design used, and therefore the estimator used

df   the degrees of freedom

nobs   the number of observations used

nblocks   the number of blocks, if used

nclusters   the number of clusters, if used

condition2   the second, "treatment", condition

condition1   the first, "control", condition

For glance.horvitz_thompson, a data.frame with columns:

nobs   the number of observations used

se_type   the type of standard error estimator used

condition2   the second, "treatment", condition

condition1   the first, "control", condition

See Also

[generics::glance()](), [lm_robust()](), [lm_lin()](), [iv_robust()](), [difference_in_means()](), [horvitz_thompson()]()

---

estimatr_tidiers   *Tidy an estimatr object*

Description

Tidy an estimatr object

Usage

```
## S3 method for class 'lm_robust'
tidy(x, conf.int = TRUE, conf.level = NULL, ...)

## S3 method for class 'iv_robust'
tidy(x, conf.int = TRUE, conf.level = NULL, ...)

## S3 method for class 'difference_in_means'
tidy(x, conf.int = TRUE, conf.level = NULL, ...)

## S3 method for class 'horvitz_thompson'
tidy(x, conf.int = TRUE, conf.level = NULL, ...)

## S3 method for class 'lh_robust'
tidy(x, conf.int = TRUE, conf.level = NULL, ...)

## S3 method for class 'lh'
tidy(x, conf.int = TRUE, conf.level = NULL, ...)
```

Arguments

x	An object returned by one of the estimators
conf.int	Logical indicating whether or not to include a confidence interval in the tidied output. Defaults to 'TRUE'.
conf.level	The confidence level to use for the confidence interval if 'conf.int = TRUE'. Must be strictly greater than 0 and less than 1. Defaults to 0.95, which corresponds to a 95 percent confidence interval.
...	extra arguments (not used)

Value

A data.frame with columns for coefficient names, estimates, standard errors, confidence intervals, p-values, degrees of freedom, and the name of the outcome variable

See Also

generics::tidy(), lm_robust(), iv_robust(), difference_in_means(), horvitz_thompson()

---

extract.robust_default

Extract model data for **texreg** *package*

Description

Prepares a `"lm_robust"` or `"iv_robust"` object for the **texreg** package. This is largely a clone of the `extract.lm` method.

Usage

```
extract.robust_default(
  model,
  include.ci = TRUE,
  include.rsquared = TRUE,
  include.adjrs = TRUE,
  include.nobs = TRUE,
  include.fstatistic = FALSE,
  include.rmse = TRUE,
  include.nclusts = TRUE,
  ...
)

extract.lm_robust(
  model,
  include.ci = TRUE,
  include.rsquared = TRUE,
  include.adjrs = TRUE,
  include.nobs = TRUE,
  include.fstatistic = FALSE,
  include.rmse = TRUE,
  include.nclusts = TRUE,
  ...
)

extract.iv_robust(
  model,
  include.ci = TRUE,
  include.rsquared = TRUE,
  include.adjrs = TRUE,
  include.nobs = TRUE,
  include.fstatistic = FALSE,
  include.rmse = TRUE,
```

```
    include.nclusts = TRUE,
    ...
)
```

Arguments

model	an object of class [lm_robust](#) or "iv_robust"
include.ci	logical. Defaults to TRUE
include.rsquared	
	logical. Defaults to TRUE
include.adjrs	logical. Defaults to TRUE
include.nobs	logical. Defaults to TRUE
include.fstatistic	
	logical. Defaults to TRUE
include.rmse	logical. Defaults to TRUE
include.nclusts	
	logical. Defaults to TRUE if clusters in model
...	unused

---

gen_pr_matrix_cluster   *Generate condition probability matrix given clusters and probabilities*

Description

Generate condition probability matrix given clusters and probabilities

Usage

```
gen_pr_matrix_cluster(clusters, treat_probs, simple)
```

Arguments

clusters	A vector of clusters
treat_probs	A vector of treatment (condition 2) probabilities
simple	A boolean for whether the assignment is a random sample assignment (TRUE, default) or complete random assignment (FALSE)

Value

a numeric 2n*2n matrix of marginal and joint condition treatment probabilities to be passed to the condition_pr_mat argument of [horvitz_thompson](#).

See Also

[declaration_to_condition_pr_mat](#)

---

horvitz_thompson   *Horvitz-Thompson estimator for two-armed trials*

Description

Horvitz-Thompson estimators that are unbiased for designs in which the randomization scheme is known

Usage

```
horvitz_thompson(
  formula,
  data,
  blocks,
  clusters,
  simple = NULL,
  condition_prs,
  condition_pr_mat = NULL,
  ra_declaration = NULL,
  subset,
  condition1 = NULL,
  condition2 = NULL,
  se_type = c("youngs", "constant", "none"),
  ci = TRUE,
  alpha = 0.05,
  return_condition_pr_mat = FALSE
)
```

Arguments

formula	an object of class formula, as in `lm`, such as Y ~ Z with only one variable on the right-hand side, the treatment.
data	A data.frame.
blocks	An optional bare (unquoted) name of the block variable. Use for blocked designs only. See details.
clusters	An optional bare (unquoted) name of the variable that corresponds to the clusters in the data; used for cluster randomized designs. For blocked designs, clusters must be within blocks.
simple	logical, optional. Whether the randomization is simple (TRUE) or complete (FALSE). This is ignored if `blocks` are specified, as all blocked designs use complete randomization, or either `ra_declaration` or `condition_pr_mat` are passed. Otherwise, it defaults to TRUE.
condition_prs	An optional bare (unquoted) name of the variable with the condition 2 (treatment) probabilities. See details. May also use a single number for the condition 2 probability if it is constant.

condition_pr_mat

    An optional 2n * 2n matrix of marginal and joint probabilities of all units in condition1 and condition2. See details.

ra_declaration   An object of class "ra_declaration", from the [declare_ra](#) function in the **randomizr** package. This is the third way that one can specify a design for this estimator. Cannot be used along with any of condition_prs, blocks, clusters, or condition_pr_mat. See details.

subset   An optional bare (unquoted) expression specifying a subset of observations to be used.

condition1   value in the treatment vector of the condition to be the control. Effects are estimated with condition1 as the control and condition2 as the treatment. If unspecified, condition1 is the "first" condition and condition2 is the "second" according to levels if the treatment is a factor or according to a sortif it is a numeric or character variable (i.e if unspecified and the treatment is 0s and 1s, condition1 will by default be 0 and condition2 will be 1). See the examples for more.

condition2   value in the treatment vector of the condition to be the treatment. See condition1.

se_type   can be one of c("youngs", "constant", "none") and corresponds the estimator of the standard errors. Default estimator uses Young's inequality (and is conservative) while the other uses a constant treatment effects assumption and only works for simple randomized designs at the moment. If "none" then standard errors will not be computed which may speed up run time if only the point estimate is required.

ci   logical. Whether to compute and return p-values and confidence intervals, TRUE by default.

alpha   The significance level, 0.05 by default.

return_condition_pr_mat

    logical. Whether to return the condition probability matrix. Returns NULL if the design is simple randomization, FALSE by default.

Details

This function implements the Horvitz-Thompson estimator for treatment effects for two-armed trials. This estimator is useful for estimating unbiased treatment effects given any randomization scheme as long as the randomization scheme is known.

In short, the Horvitz-Thompson estimator essentially reweights each unit by the probability of it being in its observed condition. Pivotal to the estimation of treatment effects using this estimator are the marginal condition probabilities (i.e., the probability that any one unit is in a particular treatment condition). Pivotal to the estimating the variance variance whenever the design is more complicated than simple randomization, are the joint condition probabilities (i.e., the probabilities that any two units have a particular set of treatment conditions, either the same or different). The estimator we provide here considers the case with two treatment conditions.

Users interested in more details can see the [mathematical notes](#) for more information and references, or see the references below.

There are three distinct ways that users can specify the design to the function. The preferred way is to use the [declare_ra](#) function in the **randomizr** package. This function takes several arguments, including blocks, clusters, treatment probabilities, whether randomization is simple or not,

and more. Passing the outcome of that function, an object of class "ra_declaration" to the ra_declaration argument in this function, will lead to a call of the declaration_to_condition_pr_mat function which generates the condition probability matrix needed to estimate treatment effects and standard errors. We provide many examples below of how this could be done.

The second way is to pass the names of vectors in your data to condition_prs, blocks, and clusters. You can further specify whether the randomization was simple or complete using the simple argument. Note that if blocks are specified the randomization is always treated as complete. From these vectors, the function learns how to build the condition probability matrix that is used in estimation.

In the case where condition_prs is specified, this function assumes those probabilities are the marginal probability that each unit is in condition2 and then uses the other arguments (blocks, clusters, simple) to learn the rest of the design. If users do not pass condition_prs, this function learns the probability of being in condition2 from the data. That is, none of these arguments are specified, we assume that there was a simple randomization where the probability of each unit being in condition2 was the average of all units in condition2. Similarly, we learn the block-level probability of treatment within blocks by looking at the mean number of units in condition2 if condition_prs is not specified.

The third way is to pass a condition_pr_mat directly. One can see more about this object in the documentation for declaration_to_condition_pr_mat and permutations_to_condition_pr_mat. Essentially, this 2n * 2n matrix allows users to specify marginal and joint marginal probabilities of units being in conditions 1 and 2 of arbitrary complexity. Users should only use this option if they are certain they know what they are doing.

Value

Returns an object of class "horvitz_thompson".

The post-estimation commands functions summary and tidy return results in a data.frame. To get useful data out of the return, you can use these data frames, you can use the resulting list directly, or you can use the generic accessor functions coef and confint.

An object of class "horvitz_thompson" is a list containing at least the following components:

coefficients	the estimated difference in totals
std.error	the estimated standard error
statistic	the z-statistic
df	the estimated degrees of freedom
p.value	the p-value from a two-sided z-test using coefficients and std.error
conf.low	the lower bound of the 1 - alpha percent confidence interval
conf.high	the upper bound of the 1 - alpha percent confidence interval
term	a character vector of coefficient names
alpha	the significance level specified by the user
nobs	the number of observations used
outcome	the name of the outcome variable
condition_pr_mat	the condition probability matrix if return_condition_pr_mat is TRUE

References

Aronow, Peter M, and Joel A Middleton. 2013. "A Class of Unbiased Estimators of the Average Treatment Effect in Randomized Experiments." Journal of Causal Inference 1 (1): 135-54. http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.712.5830&rep=rep1&type=pdf.

Aronow, Peter M, and Cyrus Samii. 2017. "Estimating Average Causal Effects Under Interference Between Units." Annals of Applied Statistics, forthcoming. https://arxiv.org/abs/1305.6156v3.

Middleton, Joel A, and Peter M Aronow. 2015. "Unbiased Estimation of the Average Treatment Effect in Cluster-Randomized Experiments." Statistics, Politics and Policy 6 (1-2): 39-75. doi:10.1515/spp20130002.

See Also

declare_ra

Examples

```
# Set seed
set.seed(42)

# Simulate data
n <- 10
dat <- data.frame(y = rnorm(n))

library(randomizr)

#----------
# 1. Simple random assignment
#----------
dat$p <- 0.5
dat$z <- rbinom(n, size = 1, prob = dat$p)

# If you only pass condition_prs, we assume simple random sampling
horvitz_thompson(y ~ z, data = dat, condition_prs = p)
# Assume constant effects instead
horvitz_thompson(y ~ z, data = dat, condition_prs = p, se_type = "constant")

# Also can use randomizr to pass a declaration
srs_declaration <- declare_ra(N = nrow(dat), prob = 0.5, simple = TRUE)
horvitz_thompson(y ~ z, data = dat, ra_declaration = srs_declaration)

#----------
# 2. Complete random assignment
#----------

dat$z <- sample(rep(0:1, each = n/2))
# Can use a declaration
crs_declaration <- declare_ra(N = nrow(dat), prob = 0.5, simple = FALSE)
horvitz_thompson(y ~ z, data = dat, ra_declaration = crs_declaration)
# Can precompute condition_pr_mat and pass it
```

```
# (faster for multiple runs with same condition probability matrix)
crs_pr_mat <- declaration_to_condition_pr_mat(crs_declaration)
horvitz_thompson(y ~ z, data = dat, condition_pr_mat = crs_pr_mat)

#----------
# 3. Clustered treatment, complete random assigment
#-----------
# Simulating data
dat$cl <- rep(1:4, times = c(2, 2, 3, 3))
dat$prob <- 0.5
clust_crs_decl <- declare_ra(N = nrow(dat), clusters = dat$cl, prob = 0.5)
dat$z <- conduct_ra(clust_crs_decl)
# Easiest to specify using declaration
ht_cl <- horvitz_thompson(y ~ z, data = dat, ra_declaration = clust_crs_decl)
# Also can pass the condition probability and the clusters
ht_cl_manual <- horvitz_thompson(
  y ~ z,
  data = dat,
  clusters = cl,
  condition_prs = prob,
  simple = FALSE
)
ht_cl
ht_cl_manual

# Blocked estimators specified similarly

#----------
# More complicated assignment
#----------

# arbitrary permutation matrix
possible_treats <- cbind(
  c(1, 1, 0, 1, 0, 0, 0, 1, 1, 0),
  c(0, 1, 1, 0, 1, 1, 0, 1, 0, 1),
  c(1, 0, 1, 1, 1, 1, 1, 0, 0, 0)
)
arb_pr_mat <- permutations_to_condition_pr_mat(possible_treats)
# Simulating a column to be realized treatment
dat$z <- possible_treats[, sample(ncol(possible_treats), size = 1)]
horvitz_thompson(y ~ z, data = dat, condition_pr_mat = arb_pr_mat)
```

---

iv_robust   *Two-Stage Least Squares Instrumental Variables Regression*

Description

This formula estimates an instrumental variables regression using two-stage least squares with a variety of options for robust standard errors

Usage

```
iv_robust(
  formula,
  data,
  weights,
  subset,
  clusters,
  fixed_effects,
  se_type = NULL,
  ci = TRUE,
  alpha = 0.05,
  diagnostics = FALSE,
  return_vcov = TRUE,
  try_cholesky = FALSE
)
```

Arguments

formula	an object of class formula of the regression and the instruments. For example, the formula y ~ x1 + x2 | z1 + z2 specifies x1 and x2 as endogenous regressors and z1 and z2 as their respective instruments.
data	A data.frame
weights	the bare (unquoted) names of the weights variable in the supplied data.
subset	An optional bare (unquoted) expression specifying a subset of observations to be used.
clusters	An optional bare (unquoted) name of the variable that corresponds to the clusters in the data.
fixed_effects	An optional right-sided formula containing the fixed effects that will be projected out of the data, such as ~ blockID. Do not pass multiple-fixed effects with intersecting groups. Speed gains are greatest for variables with large numbers of groups and when using "HC1" or "stata" standard errors. See 'Details'.
se_type	The sort of standard error sought. If clusters is not specified the options are "HC0", "HC1" (or "stata", the equivalent), "HC2" (default), "HC3", or "classical". If clusters is specified the options are "CR0", "CR2" (default), or "stata". Can also specify "none", which may speed up estimation of the coefficients.
ci	logical. Whether to compute and return p-values and confidence intervals, TRUE by default.
alpha	The significance level, 0.05 by default.
diagnostics	logical. Whether to compute and return instrumental variable diagnostic statistics and tests.
return_vcov	logical. Whether to return the variance-covariance matrix for later usage, TRUE by default.
try_cholesky	logical. Whether to try using a Cholesky decomposition to solve least squares instead of a QR decomposition, FALSE by default. Using a Cholesky decomposition may result in speed gains, but should only be used if users are sure their model is full-rank (i.e., there is no perfect multi-collinearity)

Details

This function performs two-stage least squares estimation to fit instrumental variables regression. The syntax is similar to that in ivreg from the AER package. Regressors and instruments should be specified in a two-part formula, such as y ~ x1 + x2 | z1 + z2 + z3, where x1 and x2 are regressors and z1, z2, and z3 are instruments. Unlike ivreg, you must explicitly specify all exogenous regressors on both sides of the bar.

The default variance estimators are the same as in [lm_robust](#). Without clusters, we default to HC2 standard errors, and with clusters we default to CR2 standard errors. 2SLS variance estimates are computed using the same estimators as in [lm_robust](#), however the design matrix used are the second-stage regressors, which includes the estimated endogenous regressors, and the residuals used are the difference between the outcome and a fit produced by the second-stage coefficients and the first-stage (endogenous) regressors. More notes on this can be found at [the mathematical appendix](#).

If fixed_effects are specified, both the outcome, regressors, and instruments are centered using the method of alternating projections (Halperin 1962; Gaure 2013). Specifying fixed effects in this way will result in large speed gains with standard error estimators that do not need to invert the matrix of fixed effects. This means using "classical", "HC0", "HC1", "CR0", or "stata" standard errors will be faster than other standard error estimators. Be wary when specifying fixed effects that may result in perfect fits for some observations or if there are intersecting groups across multiple fixed effect variables (e.g. if you specify both "year" and "country" fixed effects with an unbalanced panel where one year you only have data for one country).

If diagnostics are requested, we compute and return three sets of diagnostics. First, we return tests for weak instruments using first-stage F-statistics (diagnostic_first_stage_fstatistic). Specifically, the F-statistics reported compare the model regressing each endogeneous variable on both the included exogenous variables and the instruments to a model where each endogenous variable is regressed only on the included exogenous variables (without the instruments). A significant F-test for weak instruments provides evidence against the null hypothesis that the instruments are weak. Second, we return tests for the endogeneity of the endogenous variables, often called the Wu-Hausman test (diagnostic_endogeneity_test). We implement the regression test from Hausman (1978), which allows for robust variance estimation. A significant endogeneity test provides evidence against the null that all the variables are exogenous. Third, we return a test for the correlation between the instruments and the error term (diagnostic_overid_test). We implement the Wooldridge (1995) robust score test, which is identical to Sargan's (1958) test with classical standard errors. This test is only reported if the model is overidentified (i.e. the number of instruments is greater than the number of endogenous regressors), and if no weights are specified.

Value

An object of class "iv_robust".

The post-estimation commands functions summary and [tidy](#) return results in a data.frame. To get useful data out of the return, you can use these data frames, you can use the resulting list directly, or you can use the generic accessor functions coef, vcov, confint, and predict.

An object of class "iv_robust" is a list containing at least the following components:

coefficients   the estimated coefficients
std.error   the estimated standard errors

statistic	the t-statistic
df	the estimated degrees of freedom
p.value	the p-values from a two-sided t-test using `coefficients`, `std.error`, and `df`
conf.low	the lower bound of the `1 - alpha` percent confidence interval
conf.high	the upper bound of the `1 - alpha` percent confidence interval
term	a character vector of coefficient names
alpha	the significance level specified by the user
se_type	the standard error type specified by the user
res_var	the residual variance
nobs	the number of observations used
k	the number of columns in the design matrix (includes linearly dependent columns!)
rank	the rank of the fitted model
vcov	the fitted variance covariance matrix
r.squared	the R^2 of the second stage regression
adj.r.squared	the R^2 of the second stage regression, but penalized for having more parameters, `rank`
fstatistic	a vector with the value of the second stage F-statistic with the numerator and denominator degrees of freedom
firststage_fstatistic	
	a vector with the value of the first stage F-statistic with the numerator and denominator degrees of freedom, useful for a test for weak instruments
weighted	whether or not weights were applied
call	the original function call
fitted.values	the matrix of predicted means

We also return `terms` with the second stage terms and `terms_regressors` with the first stage terms, both of which used by `predict`. If `fixed_effects` are specified, then we return `proj_fstatistic`, `proj_r.squared`, and `proj_adj.r.squared`, which are model fit statistics that are computed on the projected model (after demeaning the fixed effects).

We also return various diagnostics when `diagnostics` == TRUE. These are stored in `diagnostic_first_stage_fstatistic`, `diagnostic_endogeneity_test`, and `diagnostic_overid_test`. They have the test statistic, relevant degrees of freedom, and p.value in a named vector. See 'Details' for more. These are printed in a formatted table when the model object is passed to `summary()`.

References

Gaure, Simon. 2013. "OLS with multiple high dimensional category variables." Computational Statistics & Data Analysis 66: 8-1. doi:10.1016/j.csda.2013.03.024

Halperin, I. 1962. "The product of projection operators." Acta Scientiarum Mathematicarum (Szeged) 23(1-2): 96-99.

Examples

```
library(fabricatr)
dat <- fabricate(
  N = 40,
  Y = rpois(N, lambda = 4),
  Z = rbinom(N, 1, prob = 0.4),
  D  = Z * rbinom(N, 1, prob = 0.8),
  X = rnorm(N),
  G = sample(letters[1:4], N, replace = TRUE)
)

# Instrument for treatment `D` with encouragement `Z`
tidy(iv_robust(Y ~ D + X | Z + X, data = dat))

# Instrument with Stata's `ivregress 2sls , small rob` HC1 variance
tidy(iv_robust(Y ~ D | Z, data = dat, se_type = "stata"))

# With clusters, we use CR2 errors by default
dat$cl <- rep(letters[1:5], length.out = nrow(dat))
tidy(iv_robust(Y ~ D | Z, data = dat, clusters = cl))

# Again, easy to replicate Stata (again with `small` correction in Stata)
tidy(iv_robust(Y ~ D | Z, data = dat, clusters = cl, se_type = "stata"))

# We can also specify fixed effects, that will be taken as exogenous regressors
# Speed gains with fixed effects are greatests with "stata" or "HC1" std.errors
tidy(iv_robust(Y ~ D | Z, data = dat, fixed_effects = ~ G, se_type = "HC1"))
```

---

lh_robust	*Linear Hypothesis for Ordinary Least Squares with Robust Standard Errors*

Description

This function fits a linear model with robust standard errors and performs linear hypothesis test.

Usage

```
lh_robust(..., data, linear_hypothesis)
```

Arguments

...	Other arguments to be passed to `lm_robust`
data	A data.frame
linear_hypothesis	
	A character string or a matrix specifying combination, to be passed to the hypothesis.matrix argument of car::linearHypothesis See `linearHypothesis` for more details.

Details

This function is a wrapper for [lm_robust](#) and for [linearHypothesis](#). It first runs lm_robust and next passes "lm_robust" object as an argument to linearHypothesis.

Value

An object of class "lh_robust" containing the two following components:

lm_robust   an object as returned by lm_robust.

lh   A data frame with most of its columns pulled from linearHypothesis' output.

The only analyis directly performed by lh_robust is a t-test for the null hypothesis of no effects of the linear combination of coefficients as specified by the user. All other output components are either extracted from linearHypothesis or lm_robust.

The original output returned by linearHypothesis is added as an attribute under the "linear_hypothesis" attribute.

Examples

```
library(fabricatr)
dat <- fabricate(
  N = 40,
  y = rpois(N, lambda = 4),
  x = rnorm(N),
  z = rbinom(N, 1, prob = 0.4),
  clusterID = sample(1:4, 40, replace = TRUE)
)

# Default variance estimator is HC2 robust standard errors
lhro <- lh_robust(y ~ x + z, data = dat, linear_hypothesis = "z + 2x = 0")

# The linear hypothesis argument can be specified equivalently as:
lh_robust(y ~ x + z, data = dat, linear_hypothesis = "z = 2x")
lh_robust(y ~ x + z, data = dat, linear_hypothesis = "2*x +1*z")
lh_robust(y ~ x + z, data = dat, linear_hypothesis = "z + 2x = 0")

# Also recovers other sorts of standard erorrs just as specified in \code{\link{lm_robust}}
lh_robust(y ~ x + z, data = dat, linear_hypothesis = "z + 2x = 0", se_type = "classical")
lh_robust(y ~ x + z, data = dat, linear_hypothesis = "z + 2x = 0", se_type =  "HC1")

#  Can tidy() main output and subcomponents in to a data.frame
lhro <- lh_robust(y ~ x + z, data = dat, linear_hypothesis = "z + 2x = 0")
tidy(lhro )
tidy(lhro$lm_robust)
tidy(lhro$lh)

# Can use summary() to get more statistics on the main output and subcomponents.
summary(lhro)
summary(lhro$lm_robust)
summary(lhro$lh)
```

lm_lin   *Linear regression with the Lin (2013) covariate adjustment*

Description

This function is a wrapper for `lm_robust` that is useful for estimating treatment effects with pre-treatment covariate data. This implements the method described by Lin (2013).

Usage

```
lm_lin(
  formula,
  covariates,
  data,
  weights,
  subset,
  clusters,
  se_type = NULL,
  ci = TRUE,
  alpha = 0.05,
  return_vcov = TRUE,
  try_cholesky = FALSE
)
```

Arguments

formula	an object of class formula, as in `lm`, such as Y ~ Z with only one variable on the right-hand side, the treatment
covariates	a right-sided formula with pre-treatment covariates on the right hand side, such as ~ x1 + x2 + x3.
data	A data.frame
weights	the bare (unquoted) names of the weights variable in the supplied data.
subset	An optional bare (unquoted) expression specifying a subset of observations to be used.
clusters	An optional bare (unquoted) name of the variable that corresponds to the clusters in the data.
se_type	The sort of standard error sought. If clusters is not specified the options are "HC0", "HC1" (or "stata", the equivalent), "HC2" (default), "HC3", or "classical". If clusters is specified the options are "CR0", "CR2" (default), or "stata" are permissible.
ci	logical. Whether to compute and return p-values and confidence intervals, TRUE by default.
alpha	The significance level, 0.05 by default.

return_vcov	logical. Whether to return the variance-covariance matrix for later usage, TRUE by default.
try_cholesky	logical. Whether to try using a Cholesky decomposition to solve least squares instead of a QR decomposition, FALSE by default. Using a Cholesky decomposition may result in speed gains, but should only be used if users are sure their model is full-rank (i.e., there is no perfect multi-collinearity)

Details

This function is simply a wrapper for `lm_robust` and implements the Lin estimator (see the reference below). This method pre-processes the data by taking the covariates specified in the `covariates` argument, centering them by subtracting from each covariate its mean, and interacting them with the treatment. If the treatment has multiple values, a series of dummies for each value is created and each of those is interacted with the demeaned covariates. More details can be found in the Getting Started vignette and the mathematical notes.

Value

An object of class `"lm_robust"`.

The post-estimation commands functions summary and `tidy` return results in a data.frame. To get useful data out of the return, you can use these data frames, you can use the resulting list directly, or you can use the generic accessor functions coef, vcov, confint, and predict. Marginal effects and uncertainty about them can be gotten by passing this object to `margins` from the **margins**.

Users who want to print the results in TeX of HTML can use the `extract` function and the **texreg** package.

An object of class `"lm_robust"` is a list containing at least the following components:

coefficients	the estimated coefficients
std.error	the estimated standard errors
statistic	the t-statistic
df	the estimated degrees of freedom
p.value	the p-values from a two-sided t-test using coefficients, std.error, and df
conf.low	the lower bound of the 1 - alpha percent confidence interval
conf.high	the upper bound of the 1 - alpha percent confidence interval
term	a character vector of coefficient names
alpha	the significance level specified by the user
se_type	the standard error type specified by the user
res_var	the residual variance
N	the number of observations used
k	the number of columns in the design matrix (includes linearly dependent columns!)
rank	the rank of the fitted model
vcov	the fitted variance covariance matrix

r.squared   The R^2,
$$R^2 = 1 - Sum(e[i]^2)/Sum((y[i] - y^*)^2),$$

where y^* is the mean of $y[i]$ if there is an intercept and zero otherwise, and $e[i]$ is the ith residual.

adj.r.squared   The R^2 but penalized for having more parameters, rank

weighted   whether or not weights were applied

call   the original function call

fitted.values   the matrix of predicted means

We also return terms and contrasts, used by predict, and scaled_centerthe means of each of the covariates used for centering them

See Also

[lm_robust](#)

#' @references Freedman, David A. 2008. "On Regression Adjustments in Experiments with Several Treatments." The Annals of Applied Statistics. JSTOR, 176-96. doi:10.1214/07AOAS143.

Lin, Winston. 2013. "Agnostic Notes on Regression Adjustments to Experimental Data: Reexamining Freedman's Critique." The Annals of Applied Statistics 7 (1). Institute of Mathematical Statistics: 295-318. doi:10.1214/12AOAS583.

Examples

```
library(fabricatr)
library(randomizr)
dat <- fabricate(
  N = 40,
  x = rnorm(N, mean = 2.3),
  x2 = rpois(N, lambda = 2),
  x3 = runif(N),
  y0 = rnorm(N) + x,
  y1 = rnorm(N) + x + 0.35
)

dat$z <- complete_ra(N = nrow(dat))
dat$y <- ifelse(dat$z == 1, dat$y1, dat$y0)

# Same specification as lm_robust() with one additional argument
lmlin_out <- lm_lin(y ~ z, covariates = ~ x, data = dat)
tidy(lmlin_out)

# Works with multiple pre-treatment covariates
lm_lin(y ~ z, covariates = ~ x + x2, data = dat)

# Also centers data AFTER evaluating any functions in formula
lmlin_out2 <- lm_lin(y ~ z, covariates = ~ x + log(x3), data = dat)
lmlin_out2$scaled_center["log(x3)"]
mean(log(dat$x3))
```

```
# Works easily with clusters
dat$clusterID <- rep(1:20, each = 2)
dat$z_clust <- cluster_ra(clusters = dat$clusterID)

lm_lin(y ~ z_clust, covariates = ~ x, data = dat, clusters = clusterID)

# Works with multi-valued treatments
dat$z_multi <- sample(1:3, size = nrow(dat), replace = TRUE)
lm_lin(y ~ z_multi, covariates = ~ x, data = dat)

# Stratified estimator with blocks
dat$blockID <- rep(1:5, each = 8)
dat$z_block <- block_ra(blocks = dat$blockID)

lm_lin(y ~ z_block, ~ factor(blockID), data = dat)

## Not run:
  # Can also use 'margins' package if you have it installed to get
  # marginal effects
  library(margins)
  lmlout <- lm_lin(y ~ z_block, ~ x, data = dat)
  summary(margins(lmlout))

  # Can output results using 'texreg'
  library(texreg)
  texregobj <- extract(lmlout)

## End(Not run)
```

---

lm_robust   *Ordinary Least Squares with Robust Standard Errors*

Description

This formula fits a linear model, provides a variety of options for robust standard errors, and conducts coefficient tests

Usage

```
lm_robust(
  formula,
  data,
  weights,
  subset,
  clusters,
  fixed_effects,
  se_type = NULL,
  ci = TRUE,
```

```
    alpha = 0.05,
    return_vcov = TRUE,
    try_cholesky = FALSE
)
```

Arguments

formula	an object of class formula, as in [lm](#)
data	A data.frame
weights	the bare (unquoted) names of the weights variable in the supplied data.
subset	An optional bare (unquoted) expression specifying a subset of observations to be used.
clusters	An optional bare (unquoted) name of the variable that corresponds to the clusters in the data.
fixed_effects	An optional right-sided formula containing the fixed effects that will be projected out of the data, such as ~ blockID. Do not pass multiple-fixed effects with intersecting groups. Speed gains are greatest for variables with large numbers of groups and when using "HC1" or "stata" standard errors. See 'Details'.
se_type	The sort of standard error sought. If clusters is not specified the options are "HC0", "HC1" (or "stata", the equivalent), "HC2" (default), "HC3", or "classical". If clusters is specified the options are "CR0", "CR2" (default), or "stata". Can also specify "none", which may speed up estimation of the coefficients.
ci	logical. Whether to compute and return p-values and confidence intervals, TRUE by default.
alpha	The significance level, 0.05 by default.
return_vcov	logical. Whether to return the variance-covariance matrix for later usage, TRUE by default.
try_cholesky	logical. Whether to try using a Cholesky decomposition to solve least squares instead of a QR decomposition, FALSE by default. Using a Cholesky decomposition may result in speed gains, but should only be used if users are sure their model is full-rank (i.e., there is no perfect multi-collinearity)

Details

This function performs linear regression and provides a variety of standard errors. It takes a formula and data much in the same was as [lm](#) does, and all auxiliary variables, such as clusters and weights, can be passed either as quoted names of columns, as bare column names, or as a self-contained vector. Examples of usage can be seen below and in the [Getting Started vignette](#).

The mathematical notes in [this vignette](#) specify the exact estimators used by this function. The default variance estimators have been chosen largely in accordance with the procedures in [this manual](#). The default for the case without clusters is the HC2 estimator and the default with clusters is the analogous CR2 estimator. Users can easily replicate Stata standard errors in the clustered or non-clustered case by setting `se_type` = "stata".

The function estimates the coefficients and standard errors in C++, using the RcppEigen package. By default, we estimate the coefficients using Column-Pivoting QR decomposition from the Eigen

C++ library, although users could get faster solutions by setting `try_cholesky` = TRUE to use a Cholesky decomposition instead. This will likely result in quicker solutions, but the algorithm does not reliably detect when there are linear dependencies in the model and may fail silently if they exist.

If `fixed_effects` are specified, both the outcome and design matrix are centered using the method of alternating projections (Halperin 1962; Gaure 2013). Specifying fixed effects in this way will result in large speed gains with standard error estimators that do not need to invert the matrix of fixed effects. This means using "classical", "HC0", "HC1", "CR0", or "stata" standard errors will be faster than other standard error estimators. Be wary when specifying fixed effects that may result in perfect fits for some observations or if there are intersecting groups across multiple fixed effect variables (e.g. if you specify both "year" and "country" fixed effects with an unbalanced panel where one year you only have data for one country).

As with `lm()`, multivariate regression (multiple outcomes) will only admit observations into the estimation that have no missingness on any outcome.

Value

An object of class `"lm_robust"`.

The post-estimation commands functions summary and [tidy](#) return results in a data.frame. To get useful data out of the return, you can use these data frames, you can use the resulting list directly, or you can use the generic accessor functions coef, vcov, confint, and predict. Marginal effects and uncertainty about them can be gotten by passing this object to [margins](#) from the **margins**, or to emmeans in the **emmeans** package.

Users who want to print the results in TeX of HTML can use the [extract](#) function and the **texreg** package.

If users specify a multivariate linear regression model (multiple outcomes), then some of the below components will be of higher dimension to accommodate the additional models.

An object of class `"lm_robust"` is a list containing at least the following components:

coefficients	the estimated coefficients
std.error	the estimated standard errors
statistic	the t-statistic
df	the estimated degrees of freedom
p.value	the p-values from a two-sided t-test using coefficients, std.error, and df
conf.low	the lower bound of the 1 - alpha percent confidence interval
conf.high	the upper bound of the 1 - alpha percent confidence interval
term	a character vector of coefficient names
alpha	the significance level specified by the user
se_type	the standard error type specified by the user
res_var	the residual variance
N	the number of observations used
k	the number of columns in the design matrix (includes linearly dependent columns!)
rank	the rank of the fitted model

vcov	the fitted variance covariance matrix
r.squared	The R^2, $$R^2 = 1 - Sum(e[i]^2)/Sum((y[i] - y^*)^2),$$ where y^* is the mean of $y[i]$ if there is an intercept and zero otherwise, and $e[i]$ is the ith residual.
adj.r.squared	The R^2 but penalized for having more parameters, rank
fstatistic	a vector with the value of the F-statistic with the numerator and denominator degrees of freedom
weighted	whether or not weights were applied
call	the original function call
fitted.values	the matrix of predicted means

We also return terms and contrasts, used by predict. If fixed_effects are specified, then we return proj_fstatistic, proj_r.squared, and proj_adj.r.squared, which are model fit statistics that are computed on the projected model (after demeaning the fixed effects).

References

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Halperin, I. 1962. "The product of projection operators." Acta Scientiarum Mathematicarum (Szeged) 23(1-2): 96-99.

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Pustejovsky, James E, and Elizabeth Tipton. 2016. "Small Sample Methods for Cluster-Robust Variance Estimation and Hypothesis Testing in Fixed Effects Models." Journal of Business & Economic Statistics. Taylor & Francis. doi:10.1080/07350015.2016.1247004.

Samii, Cyrus, and Peter M Aronow. 2012. "On Equivalencies Between Design-Based and Regression-Based Variance Estimators for Randomized Experiments." Statistics and Probability Letters 82 (2). doi:10.1016/j.spl.2011.10.024.

Examples

```
set.seed(15)
library(fabricatr)
dat <- fabricate(
  N = 40,
  y = rpois(N, lambda = 4),
  x = rnorm(N),
  z = rbinom(N, 1, prob = 0.4)
```

```
)

# Default variance estimator is HC2 robust standard errors
lmro <- lm_robust(y ~ x + z, data = dat)

# Can tidy() the data in to a data.frame
tidy(lmro)
# Can use summary() to get more statistics
summary(lmro)
# Can also get coefficients three ways
lmro$coefficients
coef(lmro)
tidy(lmro)$estimate
# Can also get confidence intervals from object or with new 1 - `alpha`
lmro$conf.low
confint(lmro, level = 0.8)

# Can recover classical standard errors
lmclassic <- lm_robust(y ~ x + z, data = dat, se_type = "classical")
tidy(lmclassic)

# Can easily match Stata's robust standard errors
lmstata <- lm_robust(y ~ x + z, data = dat, se_type = "stata")
tidy(lmstata)

# Easy to specify clusters for cluster-robust inference
dat$clusterID <- sample(1:10, size = 40, replace = TRUE)

lmclust <- lm_robust(y ~ x + z, data = dat, clusters = clusterID)
tidy(lmclust)

# Can also match Stata's clustered standard errors
lm_robust(
  y ~ x + z,
  data = dat,
  clusters = clusterID,
  se_type = "stata"
)

# Works just as LM does with functions in the formula
dat$blockID <- rep(c("A", "B", "C", "D"), each = 10)

lm_robust(y ~ x + z + factor(blockID), data = dat)

# Weights are also easily specified
dat$w <- runif(40)

lm_robust(
  y ~ x + z,
  data = dat,
  weights = w,
  clusters = clusterID
)
```

```
# Subsetting works just as in `lm()`
lm_robust(y ~ x, data = dat, subset = z == 1)

# One can also choose to set the significance level for different CIs
lm_robust(y ~ x + z, data = dat, alpha = 0.1)

# We can also specify fixed effects
# Speed gains with fixed effects are greatest with "stata" or "HC1" std.errors
tidy(lm_robust(y ~ z, data = dat, fixed_effects = ~ blockID, se_type = "HC1"))

## Not run:
  # Can also use 'margins' or 'emmeans' package if you have them installed
  # to get marginal effects
  library(margins)
  lmrout <- lm_robust(y ~ x + z, data = dat)
  summary(margins(lmrout))

  # Can output results using 'texreg'
  library(texreg)
  texreg(lmrout)

  # Using emmeans to obtain covariate-adjusted means
  library(emmeans)
  fiber.rlm <- lm_robust(strength ~ diameter + machine, data = fiber)
  emmeans(fiber.rlm, "machine")

## End(Not run)
```

---

lm_robust_fit   *Internal method that creates linear fits*

Description

Internal method that creates linear fits

Usage

```
lm_robust_fit(
  y,
  X,
  yoriginal = NULL,
  Xoriginal = NULL,
  weights,
  cluster,
  fixed_effects = NULL,
  ci = TRUE,
  se_type,
```

```
    has_int,
    alpha = 0.05,
    return_vcov = TRUE,
    return_fit = TRUE,
    try_cholesky = FALSE,
    iv_stage = list(0)
)
```

Arguments

y	numeric outcome vector
X	numeric design matrix
yoriginal	numeric outcome vector, unprojected if there are fixed effects
Xoriginal	numeric design matrix, unprojected if there are fixed effects. Any column named "(Intercept)" will be dropped
weights	numeric weights vector
cluster	numeric cluster vector
fixed_effects	character matrix of fixed effect groups
ci	boolean that when T returns confidence intervals and p-values
se_type	character denoting which kind of SEs to return
has_int	logical, whether the model has an intercept, used for R^2
alpha	numeric denoting the test size for confidence intervals
return_vcov	logical, whether to return the vcov matrix for later usage
return_fit	logical, whether to return fitted values
try_cholesky	logical, whether to try using a cholesky decomposition to solve LS instead of a QR decomposition
iv_stage	list of length two, the first element denotes the stage of 2SLS IV estimation, where 0 is used for OLS. The second element is only used for the second stage of 2SLS and has the first stage design matrix. For OLS, the default, list(0), for the first stage of 2SLS list(1), for second stage of 2SLS list(2, first_stage_design_mat).

---

na.omit_detailed.data.frame
Extra logging on na.omit handler

Description

Extra logging on na.omit handler

Usage

```
na.omit_detailed.data.frame(object)
```

Arguments

object   a data.frame

Value

a normal `omit` object, with the extra attribute `why_omit`, which contains the leftmost column containing an NA for each row that was dropped, by column name, if any were dropped.

See Also

`na.omit`

---

permutations_to_condition_pr_mat

Builds condition probability matrices for Horvitz-Thompson estimation from permutation matrix

---

Description

Builds condition probability matrices for Horvitz-Thompson estimation from permutation matrix

Usage

```
permutations_to_condition_pr_mat(permutations)
```

Arguments

permutations   A matrix where the rows are units and the columns are different treatment permutations; treated units must be represented with a 1 and control units with a 0

Details

This function takes a matrix of permutations, for example from the `obtain_permutation_matrix` function in **randomizr** or through simulation and returns a 2n*2n matrix that can be used to fully specify the design for `horvitz_thompson` estimation. You can read more about these matrices in the documentation for the `declaration_to_condition_pr_mat` function.

This is done by passing this matrix to the condition_pr_mat argument of

Value

a numeric 2n*2n matrix of marginal and joint condition treatment probabilities to be passed to the condition_pr_mat argument of `horvitz_thompson`.

See Also

`declare_ra`, `declaration_to_condition_pr_mat`

Examples

```
# Complete randomization
perms <- replicate(1000, sample(rep(0:1, each = 50)))
comp_pr_mat <- permutations_to_condition_pr_mat(perms)

# Arbitrary randomization
possible_treats <- cbind(
  c(1, 1, 0, 1, 0, 0, 0, 1, 1, 0),
  c(0, 1, 1, 0, 1, 1, 0, 1, 0, 1),
  c(1, 0, 1, 1, 1, 1, 1, 0, 0, 0)
)
arb_pr_mat <- permutations_to_condition_pr_mat(possible_treats)
# Simulating a column to be realized treatment
z <- possible_treats[, sample(ncol(possible_treats), size = 1)]
y <- rnorm(nrow(possible_treats))
horvitz_thompson(y ~ z, condition_pr_mat = arb_pr_mat)
```

---

predict.lm_robust   *Predict method for* lm_robust *object*

Description

Predict method for lm_robust object

Usage

```
## S3 method for class 'lm_robust'
predict(
  object,
  newdata,
  se.fit = FALSE,
  interval = c("none", "confidence", "prediction"),
  alpha = 0.05,
  na.action = na.pass,
  pred.var = NULL,
  weights,
  ...
)
```

Arguments

object	an object of class 'lm_robust'
newdata	a data frame in which to look for variables with which to predict
se.fit	logical. Whether standard errors are required, default = FALSE
interval	type of interval calculation. Can be abbreviated, default = none

alpha	numeric denoting the test size for confidence intervals
na.action	function determining what should be done with missing values in newdata. The default is to predict NA.
pred.var	the variance(s) for future observations to be assumed for prediction intervals.
weights	variance weights for prediction. This can be a numeric vector or a bare (unquoted) name of the weights variable in the supplied newdata.
...	other arguments, unused

Details

Produces predicted values, obtained by evaluating the regression function in the frame `newdata` for fits from `lm_robust` and `lm_lin`. If the logical se.fit is TRUE, standard errors of the predictions are calculated. Setting intervals specifies computation of confidence or prediction (tolerance) intervals at the specified level, sometimes referred to as narrow vs. wide intervals.

The equation used for the standard error of a prediction given a row of data x is:

$\sqrt{(x\Sigma x')}$,

where Σ is the estimated variance-covariance matrix from `lm_robust`.

The prediction intervals are for a single observation at each case in `newdata` with error variance(s) `pred.var`. The the default is to assume that future observations have the same error variance as those used for fitting, which is gotten from the fit [lm_robust](#) object. If weights is supplied, the inverse of this is used as a scale factor. If the fit was weighted, the default is to assume constant prediction variance, with a warning.

Examples

```
# Set seed
set.seed(42)

# Simulate data
n <- 10
dat <- data.frame(y = rnorm(n), x = rnorm(n))

# Fit lm
lm_out <- lm_robust(y ~ x, data = dat)
# Get predicted fits
fits <- predict(lm_out, newdata = dat)
# With standard errors and confidence intervals
fits <- predict(lm_out, newdata = dat, se.fit = TRUE, interval = "confidence")

# Use new data as well
new_dat <- data.frame(x = runif(n, 5, 8))
predict(lm_out, newdata = new_dat)

# You can also supply custom variance weights for prediction intervals
new_dat$w <- runif(n)
predict(lm_out, newdata = new_dat, weights = w, interval = "prediction")
```

Description

Prepare model fits for stargazer

Usage

```
starprep(
  ...,
  stat = c("std.error", "statistic", "p.value", "ci", "df"),
  se_type = NULL,
  clusters = NULL,
  alpha = 0.05
)
```

Arguments

...	a list of lm_robust or lm objects
stat	either "std.error" (the default), "statistic" (the t-statistic), "p.value", "ci", or "df"
se_type	(optional) if any of the objects are lm objects, what standard errors should be used. Must only be one type and will be used for all lm objects passed to starprep. See commarobust for more.
clusters	(optional) if any of the objects are lm objects, what clusters should be used, if clusters should be used. Must only be one vector and will be used for all lm objects passed to starprep. See commarobust for more.
alpha	(optional) if any of the objects are lm objects, what significance level should be used for the p-values or confidence intervals

Details

Used to help extract statistics from lists of model fits for stargazer. Prefers lm_robust objects, but because stargazer does not work with lm_robust objects, starprep can also take lm objects and calls commarobust to get the preferred, robust statistics.

Value

a list of vectors of extracted statistics for stargazers

Examples

```
library(stargazer)

lm1 <- lm(mpg ~ hp, data = mtcars)
lm2 <- lm(mpg ~ hp + wt, data = mtcars)
```

```
# Use default "HC2" standard errors
stargazer(lm1, lm2,
          se = starprep(lm1, lm2),
          p = starprep(lm1, lm2, stat = "p.value"),
          omit.stat = "f")
# NB: We remove the F-stat because stargazer only can use original F-stat
# which uses classical SEs

# Use default "CR2" standard errors with clusters
stargazer(lm1, lm2,
          se = starprep(lm1, lm2, clusters = mtcars$carb),
          p = starprep(lm1, lm2, clusters = mtcars$carb, stat = "p.value"),
          omit.stat = "f")

# Can also specify significance levels and different standard errors
stargazer(lm1, lm2,
          ci.custom = starprep(lm1, lm2, se_type = "HC3", alpha = 0.1, stat = "ci"),
          omit.stat = "f")
```

Index