Package 'rankdist'

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Type Package

Title Distance Based Ranking Models

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Description Implements distance based probability models for ranking data.
The supported distance metrics include Kendall distance, Spearman distance, Footrule distance, Hamming distance,
Weighted-tau distance and Weighted Kendall distance.
Phi-component model and mixture models are also supported.

License GPL (>= 2)

Depends R (>= 2.10)

Imports Rcpp (>= 0.11.4), hash, optimx, permute, methods

LinkingTo Rcpp

LazyData true

Suggests testthat

NeedsCompilation yes

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R topics documented:

`rankdist-package` *A package for fitting distance based ranking models*

Description

The rankdist package implements distance based probability models for ranking data. Mixture models are also supported. Ranking data are stored as S4 objects to avoid confusions about representations.

Details

Package:	rankdist
Type:	Package
Version:	1.1.4
Date:	2019-07-27
License:	GPL (>= 2)

Distance based models are effective ways to model ranking data. This package supports models based on Kendall distance and weighted Kendall distance. Mixture models can be easily fitted as well. The package includes a well-studied ranking data set, the APA Election data.

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References

Qian Z, Yu L. H. P (2019) "Weighted Distance-Based Models for Ranking Data Using the R Package rankdist." *Journal of Statistical Software*, **90**(5), 1-31. doi: 10.18637/jss.v090.i05

Examples

```
## Not run:
fitted_model <- RankDistanceModel(rankdata,rankinit,rankctrl)

## End(Not run)
```

`apa_obj` *American Psychological Association (APA) election data*

Description

A dataset containing 5738 complete votes in APA election. There are 5 candidates in total.

Usage

```
apa_obj
```

Format

a RankData object

References

Marden, J. I. (1995). Analyzing and Modeling Rank Data (94-96). Chapman Hall, New York.

See Also

`apa_partial_obj`

`apa_partial_obj` *American Psychological Association (APA) election data (partial rankings included)*

Description

A dataset containing 5738 complete votes and 9711 partial votes in APA election. There are 5 candidates in total.

Usage

```
apa_partial_obj
```

Format

a RankData object

References

Marden, J. I. (1995). Analyzing and Modeling Rank Data (94-96). Chapman Hall, New York.

See Also

`apa_obj`

DistanceBlock *Calculate Kendall distance between one ranking and a matrix of rankings*

Description

Calculate Kendall distance between one ranking and a matrix of rankings

Usage

```
DistanceBlock(mat, r)
```

Arguments

`mat`	a matrix of rankings. Each row stores a ranking.
`r`	a single ranking

Value

a vector of Kendall distances

DistanceMatrix *Calculate Kendall distance matrix between rankings*

Description

Calculate Kendall distance matrix between rankings

Usage

```
DistanceMatrix(ranking)
```

Arguments

`ranking`	a matrix of rankings

Value

Kendall distance matrix between rankings. The value in ith row and jth column is the Kendall distance between the ith and jth rankings.

DistancePair *Calculate Kendall distance between a pair of rankings*

Description

Calculate Kendall distance between a pair of rankings

Usage

```
DistancePair(r1, r2)
```

Arguments

r1	a single ranking
r2	a single ranking

Value

Kendall distance value

GenerateExample *Generate simple examples*

Description

This function generates simple examples for illustrative proposes. The sample contains rankings of five objects and the underlying model is a Mallows' phi model with default dispersion parameter set to 0.2 and modal ranking set to (1,2,3,4,5)

Usage

```
GenerateExample(ranking = TRUE, central = 1:5, lambda = 0.2)
```

Arguments

ranking	TRUE if "ranking" representation is used in the output data; otherwise "ordering" representation is used.
central	The modal ranking.
lambda	The parameter in the model.

GenerateExampleTopQ

Generate simple examples of top-q rankings

Description

This function generates simple examples for illustrative proposes. The sample contains the top-3 rankings of five objects and the underlying model is a weighted Kendall distance model with default weights set to (0.7,0.5,0.3,0) and modal ranking set to (1,2,3,4,4)

Usage

```
GenerateExampleTopQ(central = c(1, 2, 3, 4, 4), w = c(0.7, 0.5, 0.3, 0))
```

Arguments

central	The modal ranking.
w	The weights in the model.

HashtoRank

Obtain Ranking from Hash Value

Description

HashToRank returns rankings from given hash values. Maximum 52 objects are supported.

Usage

```
HashtoRank(h)
```

Arguments

h	A vector of hash values.

Value

a matrix of rankings if input has more than one element or a single ranking (numeric vector) if input has only one element

See Also

RanktoHash for a reverse operation.

ModelSummary *Print a brief summary of the fitted model*

Description

Print a brief summary of the fitted model. This includes information about goodness of fit as well as parameter estimation.

Usage

```
ModelSummary(model)
```

Arguments

model	a ranking model returned by a call to RankDistanceModel function.

MomentsEst *Find Initial Values of phi*

Description

MomentsEst finds the initial values of phi which can be used in the subsequent optimization problems. Linear model is fitted to the log odds of rankings.This function is only useful to the Weighted Kendall model.

Usage

```
MomentsEst(dat, size, pi0 = NULL)
```

Arguments

dat	a RankData object
size	the number of samples to take in the linear model
pi0	an optional argument showing the location of central ranking. If not provided, Borda Count method is used to estimate the central ranking.

Value

estimated phi

Examples

```
MomentsEst(apa_obj,40)
```

OrderingToRanking *Transformation between Rankings and Orderings*

Description

`OrderingToRanking` transforms between ranking representation and ordering representation.

Usage

```
OrderingToRanking(ordering)
```

Arguments

`ordering`	a matrix of orderings or rankings. Each row contains an observation.

Details

Ranking representation encodes the position of objects. Ordering representation is an ordered sequence of objects. For example ranking (2 3 1 4) is equivalent to ordering (3 1 2 4), which means object 3 is first, object 1 is second, followed by object 2 and 4. Also note that we can use this function to transform rankings into orderings, and applying this function twice will not change the input value.

Value

a matrix of transformed rankings or orderings. Each row contains an observation.

RankControl-class *RankControl Class*

Description

A virtual S4 class to store control parameters for model fitting.

Details

RankControl class must be extended to reflect what distance metric should be used. Possibles extensions are `RankControlWeightedKendall`, `RankControlKendall`, `RankControlPhiComponent`, `RankControlWtau`, `RankControlSpearman`, `RankControlFootrule`, `RankControlHamming`, and `RankControlCayley`.

The control parameters that start with prefix `EM_` are intended for the EM iteration. The ones with prefix `SeachPi0` control the behaviour of searching model ranking.

Slots

`EM_limit` maximum number of EM iteration

`EM_epsilon` convergence error for weights and cluster probabilities in EM iteration

`SearchPi0_limit` maximum number of iterations in the local search of pi0.

`SearchPi0_FUN` a function object that gives a goodness of fit criterion. The default is log likelihood.

`SearchPi0_fast_traversal` a logical value. If TRUE (by default), immediately traverse to the neighbour if it is better than the current best. Otherwise, check all neighbours and traverse to the best one.

`SearchPi0_show_message` a logical value. If TRUE, the location of the current pi0 is shown.

`SearchPi0_neighbour` a character string specifying which type of neighbour to use in the local search. Supported values are: "Cayley" to use neighbours in terms of Cayley distance or "Kendall" to use neighbours in terms of Kendall distance. Note that Kendall neighbours are a subset of Cayley neighbours

User-defined Criterion

You can specify user-defined criterion to choose modal rankings. The function object SearchPi0_FUN takes a list as argument. The components in the list include the following. `obs`: the number of observations. `w.est`: the estimated weights. `log_likelihood`: the estimated log_likelihood. With this information, most of the popular information criterion can be supported and customized criterion can also be defined. A larger returned value indicates a better fit. Note that if you are fitting a mixture model the EM algorithm always tries to maximized the log likelihood. Thus the default value should be used in this case.

References

Qian Z, Yu L. H. P (2019) "Weighted Distance-Based Models for Ranking Data Using the R Package rankdist." *Journal of Statistical Software*, **90**(5), 1-31. doi: 10.18637/jss.v090.i05

See Also

`RankData`, `RankInit`

`RankControlCayley-class` *RankControlCayley Class*

Description

A S4 class for the Cayley distance model fitting. It is derived from class `RankControl-class`.

Slots

`EM_limit` maximum number of EM iteration

`EM_epsilon` convergence error for weights and cluster probabilities in EM iteration

`SearchPi0_limit` maximum number of iterations in the local search of pi0.

`SearchPi0_FUN` a function object that gives a goodness of fit criterion. The default is log likelihood.

`SearchPi0_fast_traversal` a logical value. If TRUE (by default), immediately traverse to the neighbour if it is better than the current pi0. Otherwise, check all neighbours and traverse to the best one.

`SearchPi0_show_message` a logical value. If TRUE, the location of the current pi0 is shown.

`SearchPi0_neighbour` a character string specifying which type of neighbour to use in the local search. Supported values are: "Cayley" to use neighbours in terms of Cayley distance or "Kendall" to use neighbours in terms of Kendall distance. Note that Kendall neighbours are a subset of Cayley neighbours

See Also

`RankData`, `RankInit`, `RankControl`

`RankControlFootrule-class` *RankControlFootrule Class*

Description

A S4 class for the Footrule distance model fitting. It is derived from class `RankControl-class`.

Slots

`EM_limit` maximum number of EM iteration

`EM_epsilon` convergence error for weights and cluster probabilities in EM iteration

`SearchPi0_limit` maximum number of iterations in the local search of pi0.

`SearchPi0_FUN` a function object that gives a goodness of fit criterion. The default is log likelihood.

`SearchPi0_fast_traversal` a logical value. If TRUE (by default), immediately traverse to the neighbour if it is better than the current pi0. Otherwise, check all neighbours and traverse to the best one.

`SearchPi0_show_message` a logical value. If TRUE, the location of the current pi0 is shown.

`SearchPi0_neighbour` a character string specifying which type of neighbour to use in the local search. Supported values are: "Cayley" to use neighbours in terms of Cayley distance or "Kendall" to use neighbours in terms of Kendall distance. Note that Kendall neighbours are a subset of Cayley neighbours

See Also

`RankData`, `RankInit`, `RankControl`

RankControlHamming-class
RankControlHamming Class

Description

A S4 class for the Hamming distance model fitting. It is derived from class `RankControl-class`.

Slots

`EM_limit` maximum number of EM iteration

`EM_epsilon` convergence error for weights and cluster probabilities in EM iteration

`SearchPi0_limit` maximum number of iterations in the local search of pi0.

`SearchPi0_FUN` a function object that gives a goodness of fit criterion. The default is log likelihood.

`SearchPi0_fast_traversal` a logical value. If TRUE (by default), immediately traverse to the neighbour if it is better than the current pi0. Otherwise, check all neighbours and traverse to the best one.

`SearchPi0_show_message` a logical value. If TRUE, the location of the current pi0 is shown.

`SearchPi0_neighbour` a character string specifying which type of neighbour to use in the local search. Supported values are: "Cayley" to use neighbours in terms of Cayley distance or "Kendall" to use neighbours in terms of Kendall distance. Note that Kendall neighbours are a subset of Cayley neighbours

See Also

`RankData`, `RankInit`, `RankControl`

RankControlKendall-class
RankControlKendall Class

Description

A S4 class to store control parameters for Kendall distance model fitting (Mallow's Phi Model). It is derived from class `RankControl-class`.

Details

`RankControlKendall` is derived from virtual class `RankControl`. This control class tells the solver to fit a model based on Kendall distance. The control parameters that start with prefix `EM_` are intended for the EM iteration. The ones with prefix `SeachPi0` control the behaviour of searching model ranking.

Slots

`EM_limit` maximum number of EM iteration

`EM_epsilon` convergence error for weights and cluster probabilities in EM iteration

`SearchPi0_limit` maximum number of iterations in the local search of pi0.

`SearchPi0_FUN` a function object that gives a goodness of fit criterion. The default is log likelihood.

`SearchPi0_fast_traversal` a logical value. If TRUE (by default), immediately traverse to the neighbour if it is better than the current pi0. Otherwise, check all neighbours and traverse to the best one.

`SearchPi0_show_message` a logical value. If TRUE, the location of the current pi0 is shown.

`SearchPi0_neighbour` a character string specifying which type of neighbour to use in the local search. Supported values are: "Cayley" to use neighbours in terms of Cayley distance or "Kendall" to use neighbours in terms of Kendall distance. Note that Kendall neighbours are a subset of Cayley neighbours

See Also

`RankData`, `RankInit`, `RankControl`

Examples

```
# enabling messages
testctrl = new("RankControlKendall",SearchPi0_show_message=TRUE)
```

`RankControlPhiComponent-class`
RankControlPhiComponent Class

Description

A S4 class to store control parameters for Phi component model fitting. It is derived from class `RankControl-class`.

Details

`RankControlKendall` is derived from virtual class `RankControl`. This control class tells the solver to fit a model based on a stage-wise generalization of Kendall distance. The control parameters that start with prefix `EM_` are intended for the EM iteration. The ones with prefix `SeachPi0` control the behaviour of searching model ranking.

Slots

`EM_limit` maximum number of EM iteration

`EM_epsilon` convergence error for weights and cluster probabilities in EM iteration

`SearchPi0_limit` maximum number of iterations in the local search of pi0.

`SearchPi0_FUN` a function object that gives a goodness of fit criterion. The default is log likelihood.

`SearchPi0_fast_traversal` a logical value. If TRUE (by default), immediately traverse to the neighbour if it is better than the current pi0. Otherwise, check all neighbours and traverse to the best one.

`SearchPi0_show_message` a logical value. If TRUE, the location of the current pi0 is shown.

`SearchPi0_neighbour` a character string specifying which type of neighbour to use in the local search. Supported values are: "Cayley" to use neighbours in terms of Cayley distance or "Kendall" to use neighbours in terms of Kendall distance. Note that Kendall neighbours are a subset of Cayley neighbours

See Also

`RankData`, `RankInit`, `RankControl`

Examples

```
# enabling messages
testctrl = new("RankControlPhiComponent",SearchPi0_show_message=TRUE)
```

`RankControlSpearman-class`
RankControlSpearman Class

Description

A S4 class for the Spearman distance model fitting. It is derived from class `RankControl-class`.

Slots

`EM_limit` maximum number of EM iteration

`EM_epsilon` convergence error for weights and cluster probabilities in EM iteration

`SearchPi0_limit` maximum number of iterations in the local search of pi0.

`SearchPi0_FUN` a function object that gives a goodness of fit criterion. The default is log likelihood.

`SearchPi0_fast_traversal` a logical value. If TRUE (by default), immediately traverse to the neighbour if it is better than the current pi0. Otherwise, check all neighbours and traverse to the best one.

`SearchPi0_show_message` a logical value. If TRUE, the location of the current pi0 is shown.

SearchPi0_neighbour a character string specifying which type of neighbour to use in the local search. Supported values are: "Cayley" to use neighbours in terms of Cayley distance or "Kendall" to use neighbours in terms of Kendall distance. Note that Kendall neighbours are a subset of Cayley neighbours

See Also

RankData, RankInit, RankControl

RankControlWeightedKendall-class

RankControlWeightedKendall Class

Description

A S4 class to store control parameters for Weighted Kendall distance model fitting. It is derived from class RankControl-class.

Details

RankControlWeightedKendall is derived from virtual class RankControl. All slots in RankControl are still valid. This control class tells the solver to fit a model based on Weighted Kendall distance. The control parameters that start with prefix EM_ are intended for the EM iteration. The ones with prefix SeachPi0 control the behaviour of searching model ranking.

Slots

EM_limit maximum number of EM iteration

EM_epsilon convergence error for weights and cluster probabilities in EM iteration

SearchPi0_limit maximum number of iterations in the local search of pi0.

SearchPi0_FUN a function object that gives a goodness of fit criterion. The default is log likelihood.

SearchPi0_fast_traversal a logical value. If TRUE (by default), immediately traverse to the neighbour if it is better than the current pi0. Otherwise, check all neighbours and traverse to the best one.

SearchPi0_show_message a logical value. If TRUE, the location of the current pi0 is shown.

SearchPi0_neighbour a character string specifying which type of neighbour to use in the local search. Supported values are: "Cayley" to use neighbours in terms of Cayley distance or "Kendall" to use neighbours in terms of Kendall distance. Note that Kendall neighbours are a subset of Cayley neighbours

optimx_control a list to be passed to optimx. The list must not contain a component maximize=TRUE since internally the negation of the likelihood function is minimized.

assumption A character string specifying which assumption to use when handling top-q rankings. Supported choices are "equal-probability" and "tied-rank".

See Also

RankData, RankInit, RankControl

Examples

```
# enabling  warnings
testctrl = new("RankControlWeightedKendall",optimx_control=list(dowarn=TRUE))
```

RankControlWtau-class

RankControlWtau Class

Description

A S4 class for the Weighted tau model fitting. It is derived from class RankControl-class.

Slots

EM_limit maximum number of EM iteration

EM_epsilon convergence error for weights and cluster probabilities in EM iteration

SearchPi0_limit maximum number of iterations in the local search of pi0.

SearchPi0_FUN a function object that gives a goodness of fit criterion. The default is log likelihood.

SearchPi0_fast_traversal a logical value. If TRUE (by default), immediately traverse to the neighbour if it is better than the current pi0. Otherwise, check all neighbours and traverse to the best one.

SearchPi0_show_message a logical value. If TRUE, the location of the current pi0 is shown.

SearchPi0_neighbour a character string specifying which type of neighbour to use in the local search. Supported values are: "Cayley" to use neighbours in terms of Cayley distance or "Kendall" to use neighbours in terms of Kendall distance. Note that Kendall neighbours are a subset of Cayley neighbours

optimx_control a list to be passed to optimx. The list must not contain a component maximize=TRUE since internally the negation of the likelihood function is minimized.

See Also

RankData, RankInit, RankControl

RankData-class *RankData Class*

Description

A S4 class to represent ranking data

It is well understood that the ranking representation and ordering representation of ranking data can easily be confused. I thus use a S4 class to store all the information about the ranking data. This can avoid unnecessary confusion.

Details

It is possible to store both complete and top-q rankings in the same RankData object. Three slots `topq`, `subobs`, and `q_ind` are introduced for this purpose. Note that there is generally no need to specify these slots if your data set only contains a single "q" level (for example all data are top-10 rankings). The "q" level for complete ranking should be `nobj-1`. Moreover, if the rankings are organized in chunks of increasing "q" levels (for example, top-2 rankings followed by top-3 rankings followed by top-5 rankings etc.), then slots `subobs`, and `q_ind` can also be inferred correctly by the initializer. Therefore it is highly recommender that you organise the ranking matrix in this way and utilize the initializer.

Slots

`nobj` The number of ranked objects. If not provided, it will be inferred as the maximum ranking in the data set. As a result, it must be provided if the data is top-q ranking.

`nobs` the number of observations. No need to be provided during initialization since it must be equal to the sum of slot `count`.

`ndistinct` the number of distinct rankings. No need to be provided during initialization since it must be equal to the number of rows of slot `ranking`.

`ranking` a matrix that stores the ranking representation of distinct rankings. Each row contains one ranking. For top-q ranking, all unobserved objects have ranking `q+1`.

`count` the number of observations for each distinct ranking corresponding to each row of `ranking`.

`topq` a numeric vector to store top-q ranking information. More information in details section.

`subobs` a numeric vector to store number of observations for each chunk of top-q rankings.

`q_ind` a numeric vector to store the beginning and ending of each chunk of top-q rankings. The last element has to be `ndistinct+1`.

References

Qian Z, Yu L. H. P (2019) "Weighted Distance-Based Models for Ranking Data Using the R Package rankdist." *Journal of Statistical Software*, **90**(5), 1-31. doi: 10.18637/jss.v090.i05

See Also

`RankInit`, `RankControl`

Examples

```
# creating a data set with only complete rankings
rankmat <- replicate(10,sample(1:52,52), simplify = "array")
countvec <- sample(1:52,52,replace=TRUE)
rankdat <- new("RankData",ranking=rankmat,count=countvec)
# creating a data set with both complete and top-10 rankings
rankmat_in <- replicate(10,sample(1:52,52), simplify = "array")
rankmat_in[rankmat_in>11] <- 11
rankmat_total <- cbind(rankmat_in, rankmat)
countvec_total <- c(countvec,countvec)
rankdat2 <- new("RankData",ranking=rankmat_total,count=countvec_total, nobj=52, topq=c(10,51
```

RankDistanceModel *Fit A Mixture of Distance-based Models*

Description

`RankDistanceModel` fits ranking models based on inputs

Usage

```
RankDistanceModel(dat, init, ctrl)
```

Arguments

`dat`	A RankData object.
`init`	A RankInit object.
`ctrl`	A RankControl object.

Details

The procedure will estimate central rankings, the probability of each cluster and weights.

Value

A list containing the following components:

`modal_ranking.est` the estimated modal ranking for each cluster.

`p` the marginal probability of each cluster.

`w.est` the estimated weights of each cluster.

`param.est` the phi parametrisation of weights of each cluster (for Weighted Kendall model only).

`SSR` the sum of squares of Pearson residuals

`log_likelihood` the fitted log_likelihood

`BIC` the fitted Bayesian Information Criterion value

`free_params` the number of free parameters in the model

`expectation` the expected value of each observation given by the model

`iteration` the number of EM iteration

`model.call` the function call

See Also

RankData, RankInit, RankControl

RankInit-class *RankInit Class*

Description

A S4 class to store initialization information of model fitting

The RankInit class is used to give initial values of model fitting procedures.

Slots

param.init a list containing initial values of the positive parametrization of weights.

modal_ranking.init a list containing starting points for the modal ranking search.

clu an integer containing the number of clusters used in the model.

p.init a numeric vector containing the initial values for cluster probabilities.

References

Qian Z, Yu L. H. P (2019) "Weighted Distance-Based Models for Ranking Data Using the R Package rankdist." *Journal of Statistical Software*, **90**(5), 1-31. doi: 10.18637/jss.v090.i05

See Also

RankData, RankControl

Examples

```
c1init = new("RankInit",param.init=list(rep(1,4)),
     modal_ranking.init=list(c(2,3,4,1,5)),clu=1L)
c2init = new("RankInit",param.init=list(rep(0.1,4),rep(0.1,4)),
     modal_ranking.init = list(c(2,3,4,1,5),c(2,5,1,4,3)),clu=2L,p.init=c(0.5,0.5))
```

RanktoHash *Create Hash Value for Ranking*

Description

Sometimes it is handy to deal with rankings as a hash value. `RanktoHash` returns hash values for ranks. Maximum 52 objects are supported.

Usage

```
RanktoHash(r)
```

Arguments

`r`	a vector or matrix of rankings. Each row of the matrix represents a ranking. The ranking should be a integer from one to number of objects. No NA is allowed

Value

a vector of character strings representing the hash values.

See Also

`HashtoRank` for a reverse operation.