

# Package ‘rwt’

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**Title** 'Rice Wavelet Toolbox' Wrapper

**Description** Provides a set of functions for 1D and 2D wavelet and filter bank design, analysis, and processing. Functions for denoising are also included. The package can be used for image denoising or deconvolution.

**Depends** R (>= 2.15)

**Imports** matlab

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rwt-package	<i>'Rice Wavelet Toolbox' Wrapper</i>
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### Description

Provides a set of functions for 1D and 2D wavelet and filter bank design, analysis, and processing. Functions for denoising are also included. The package can be used for image denoising or deconvolution.

### Details

Package: rwt  
 Type: package  
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For a complete list of functions, use `library(help="rwt")`.

For a high-level summary of the changes for each revision, use `file.show(system.file("NEWS", package="rwt"))`.

### Author(s)

P. Roebuck <proebuck1701@gmail.com>

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daubcqf	<i>Daubechies Filter Creation</i>
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### Description

Computes the Daubechies' scaling and wavelet filters (normalized to  $\sqrt{2}$ ).

### Usage

`daubcqf(N, type = PHASE.MINIMUM)`

**Arguments**

N	numeric scalar specifying length of filter (must be even)
type	Distinguishes the minimum phase, maximum phase and mid-phase solutions. Valid values are:  PHASE.MINIMUM PHASE.MID PHASE.MAXIMUM

**Value**

Returns a list with components:

h.0	minimal phase Daubechies' scaling filter
h.1	minimal phase Daubechies' wavelet filter

**Author(s)**

P. Roebuck <proebuck1701@gmail.com>

**References**

Ingrid Daubechies  
*Orthonormal Bases of Compactly Supported Wavelets*  
CPAM (Oct. 1988), 7(41), 909-996  
[doi:10.1002/cpa.3160410705](https://doi.org/10.1002/cpa.3160410705)

**Examples**

```
h <- daubcqf(6)
```

---

denoise *Wavelet-based Denoising*

---

**Description**

Denoise the signal  $x$  using the 2-band wavelet system described by the filter  $h$  using either the traditional discrete wavelet transform (DWT) or the linear shift invariant discrete wavelet transform (also known as the undecimated DWT (UDWT)).

**Usage**

```
denoise(x, h, type, option)
denoise.dwt(x, h, option = default.dwt.option)
denoise.udwt(x, h, option = default.udwt.option)
```

**Arguments**

x	1D or 2D signal to be denoised
h	numeric scalar specifying scaling filter to be applied
type	type of transform. Valid values are:  DWT.TRANSFORM.TYPE UDWT.TRANSFORM.TYPE
option	list containing desired transformation settings

**Details**

The transformation settings in the option list are:

**threshold.low.pass.part:** logical scalar. If TRUE, threshold the low-pass component.

**threshold.multiplier:**  $thld = c * MAD(noise\_estimate)$

**variance.estimator:** Valid values are:

MAD.VARIANCE.ESTIMATOR	Mean absolute deviation
STD.VARIANCE.ESTIMATOR	Classical numerical std estimate

**threshold.type:** Valid values are:

SOFT.THRESHOLD.TYPE	Soft thresholding
HARD.THRESHOLD.TYPE	Hard thresholding

**num.decompression.levels:** number of levels in wavelet decomposition. Setting this to MAX.DECOMPOSITION will allow maximal decomposition.

**threshold:** actual threshold to use. Setting this to anything but CALC.THRESHOLD.TO.USE will disable the variance.estimator setting.

**Value**

Returns a list with components:

xd	estimate of noise free signal
xn	estimated noise signal (x-xd)
option	list of actual parameters used. It is configured the same way as the input option list with an additional element - option[[7]] = type.

**Note**

Both denoise.dwt and denoise.udwt are convenience routines that call the denoise routine with appropriate default arguments.

**Author(s)**

P. Roebuck <proebuck1701@gmail.com>

**Examples**

```
sig <- makesig(SIGNAL.DOPPLER)
h <- daubcwf(6)
ret.dwt <- denoise.dwt(sig$x, h$h.0)
```

---

makesig                      *Make Signal*

---

**Description**

Creates artificial test signal identical to the standard test signals proposed and used by D. Donoho and I. Johnstone in WaveLab, a MATLAB toolbox for wavelet analysis developed at Stanford University.

**Usage**

```
makesig(sigName, N)
```

**Arguments**

sigName                      character string specifying name of desired signal. Valid values are:

SIGNAL.ALL  
 SIGNAL.HEAVY.SINE  
 SIGNAL.BUMPS  
 SIGNAL.BLOCKS  
 SIGNAL.DOPPLER  
 SIGNAL.RAMP  
 SIGNAL.CUSP  
 SIGNAL.SING  
 SIGNAL.HI.SINE  
 SIGNAL.LO.SINE  
 SIGNAL.LIN.CHIRP  
 SIGNAL.TWO.CHIRP  
 SIGNAL.QUAD.CHIRP  
 SIGNAL.MISH.MASH  
 SIGNAL.WERNER.SORROWS (Heisenberg)  
 SIGNAL.LEOPOLD (Kronecker)

N                              numeric scalar specifying length in samples of desired signal (512 by default)

**Value**

Returns a list with components:

x                              vector (or matrix) of test signals  
 N                              length of signal returned

**Note**

Using the value `SIGNAL.ALL.SIG` for `sigName` returns a matrix containing the vectors of all the other signals.

**Author(s)**

P. Roebuck <proebuck1701@gmail.com>

**References**

J. Buckheit, S. Chen, D. Donoho, I. Johnstone, & J. Scargle  
*WaveLab* (version 0.700; 1995) [Computer software].  
<https://statweb.stanford.edu/~wavelab/WaveLab701.html>

**Examples**

```
ret.sig <- makesig(SIGNAL.DOPPLER, 32)
```

---

mdwt

*Discrete Wavelet Transform*

---

**Description**

Computes the discrete wavelet transform `y` for input signal `x` using the scaling filter `h`.

**Usage**

```
mdwt(x, h, L)
```

**Arguments**

<code>x</code>	Finite 1D or 2D signal (implicitly periodized)
<code>h</code>	Scaling filter to be applied
<code>L</code>	Number of levels in wavelet decomposition. In the case of a 1D signal, <code>length(x)</code> must be divisible by $2^L$ ; in the case of a 2D signal, the row and the column dimension must be divisible by $2^L$ . If no argument is specified, a full DWT is returned for maximal possible <code>L</code> .

**Value**

Returns a list with components:

<code>y</code>	Wavelet transform of the signal
<code>L</code>	Number of levels in wavelet decomposition

**Author(s)**

P. Roebuck <proebuck1701@gmail.com>

**Examples**

```
sig <- makesig(SIGNAL.LIN.CHIRP, 8)
h <- daubcwf(4)
L <- 2
ret.mdwt <- mdwt(sig$x, h$h.0, L)
```

---

midwt

*Inverse Discrete Wavelet Transform*

---

**Description**

Computes the inverse discrete wavelet transform  $x$  for input signal  $y$  using the scaling filter  $h$ .

**Usage**

```
midwt(y, h, L)
```

**Arguments**

$y$	Finite 1D or 2D signal (implicitly periodized)
$h$	Scaling filter to be applied
$L$	Number of levels in wavelet decomposition. In the case of a 1D signal, $\text{length}(x)$ must be divisible by $2^L$ ; in the case of a 2D signal, the row and the column dimension must be divisible by $2^L$ . If no argument is specified, a full DWT is returned for maximal possible $L$ .

**Value**

Returns a list with components:

$x$	Periodic reconstructed signal
$L$	Number of levels in wavelet decomposition

**Author(s)**

P. Roebuck <proebuck1701@gmail.com>

**Examples**

```
sig <- makesig(SIGNAL.LIN.CHIRP, 8)
h <- daubcwf(4)
L <- 1
ret.mdwt <- mdwt(sig$x, h$h.0, L)
ret.midwt <- midwt(ret.mdwt$y, h$h.0, ret.mdwt$L)
```

---

`mirdwt`*Inverse Redundant Discrete Wavelet Transform*

---

**Description**

Computes the inverse redundant discrete wavelet transform  $x$  for input signal  $y$  using the scaling filter  $h$ . (Redundant means here that the sub-sampling after each stage of the forward transform has been omitted.)

**Usage**

```
mirdwt(y1, yh, h, L)
```

**Arguments**

<code>y1</code>	Lowpass component
<code>yh</code>	Highpass components
<code>h</code>	Scaling filter to be applied
<code>L</code>	Number of levels in wavelet decomposition. In the case of a 1D signal, <code>length(y1)</code> must be divisible by $2^L$ ; in the case of a 2D signal, the row and the column dimension must be divisible by $2^L$ . If no argument is specified, a full DWT is returned for maximal possible <code>L</code> .

**Value**

Returns a list with components:

<code>x</code>	Finite length 1D or 2D signal
<code>L</code>	Number of levels in wavelet decomposition

**Author(s)**

P. Roebuck <proebuck1701@gmail.com>

**Examples**

```
sig <- makesig(SIGNAL.LEOPOLD, 8)
h <- daubcwf(4)
L <- 1
ret.mrdwt <- mrdwt(sig$x, h$h.0, L)
ret.mirdwt <- mirdwt(ret.mrdwt$y1, ret.mrdwt$yh, h$h.0, ret.mrdwt$L)
```



---

`mrdwt`*Redundant Discrete Wavelet Transform*

---

**Description**

Computes the redundant discrete wavelet transform  $y$  for input signal  $x$  using the scaling filter  $h$ . Redundant means here that the sub-sampling after each stage is omitted.

**Usage**`mrdwt(x, h, L)`**Arguments**

<code>x</code>	Finite 1D or 2D signal (implicitly periodized)
<code>h</code>	Scaling filter to be applied
<code>L</code>	Number of levels in wavelet decomposition. In the case of a 1D signal, $\text{length}(x)$ must be divisible by $2^L$ ; in the case of a 2D signal, the row and the column dimension must be divisible by $2^L$ . If no argument is specified, a full DWT is returned for maximal possible $L$ .

**Value**

Returns a list with components:

<code>y1</code>	Lowpass component
<code>yh</code>	Highpass components
<code>L</code>	Number of levels in wavelet decomposition

**Author(s)**

P. Roebuck <proebuck1701@gmail.com>

**Examples**

```
sig <- makesig(SIGNAL.LEOPOLD, 8)
h <- daubcwf(4)
L <- 1
ret.mrdwt <- mrdwt(sig$x, h$h.0, L)
```

plotSignalTransformation

*Plot Signal and its Transform*

---

### **Description**

Plots the signal *s* and its transform *x* on graphics device.

### **Usage**

```
plotSignalTransformation(x, s, title, col.x = 'blue', col.s = 'red')
```

### **Arguments**

<i>x</i>	wavelet transformed signal to be plotted
<i>s</i>	original signal to be plotted
<i>title</i>	overall title for the plot
<i>col.x</i>	color to be used for plotting <i>x</i> values as lines
<i>col.s</i>	color to be used for plotting <i>s</i> values as lines

### **Details**

Used by demo code to display the results of a transformation.

### **Value**

Returns no value – called for its side effect.

### **Author(s)**

P. Roebuck <proebuck1701@gmail.com>

---

threshold

*Threshold Input Signal*

---

### **Description**

Thresholds the input signal *y* with the threshold value *thld*.

### **Usage**

```
hardTh(y, thld)  
softTh(y, thld)
```

**Arguments**

<code>y</code>	1D or 2D signal to be thresholded
<code>thld</code>	numeric threshold value to be applied

**Value**

Returns numeric vector of thresholded values of the same length as `y`.

**Author(s)**

P. Roebuck <proebuck1701@gmail.com>

**References**

D.L. Donoho  
*De-noising via Soft-Thresholding*  
Tech. Rept. Statistics, Stanford (1992)

**Examples**

```
sig <- makesig(SIGNAL.WERNER.SORROWS, 8)
thld <- 1
x <- hardTh(sig$x, thld)
```

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