

Package ‘smile’

April 29, 2022

Title Spatial Misalignment: Interpolation, Linkage, and Estimation

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Description Provides functions to estimate, predict and interpolate areal data. For estimation and prediction we assume areal data is an average of an underlying continuous spatial process as in Moraga et al. (2017) <[doi:10.1016/j.spasta.2017.04.006](https://doi.org/10.1016/j.spasta.2017.04.006)>, Johnson et al. (2020) <[doi:10.1186/s12942-020-00200-w](https://doi.org/10.1186/s12942-020-00200-w)>, and Wilson and Wakefield (2020) <[doi:10.1093/biostatistics/kxy041](https://doi.org/10.1093/biostatistics/kxy041)>. The interpolation methodology is (mostly) based on Goodchild and Lam (1980, ISSN:01652273).

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SystemRequirements C++11, GDAL (>= 2.0.1), GEOS (>= 3.4.0), PROJ (>= 4.8.0)

LinkingTo Rcpp, RcppArmadillo

Imports numDeriv, Rcpp, sf, mvtnorm, stats, Matrix

Depends R (>= 3.5)

URL <https://lcgodoy.me/smile/>, <https://github.com/lcgodoy/smile/>

BugReports <https://github.com/lcgodoy/smile/issues/>

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VignetteBuilder knitr

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Author Lucas da Cunha Godoy [aut, cre]
(<<https://orcid.org/0000-0003-4265-972X>>)

Maintainer Lucas da Cunha Godoy <lucasdac.godoy@gmail.com>

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AI	<i>Areal Interpolation</i>
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Description

This function estimates variables observed at a "source" region into a "target" region. "Source" and "target" regions represent two different ways to divide a city, for example. For more details, see <https://lsgodoy.me/smile/articles/sai.html>.

Usage

```
ai(source, target, vars)
```

```
ai_var(source, target, vars, vars_var, sc_vars = FALSE, var_method = "CS")
```

Arguments

source	a sf object - source spatial data.
target	a sf object - target spatial data.
vars	a character representing the variables (observed at the source) to be estimated at the target data.
vars_var	a scalar of type character representing the name of the variable in the source dataset that stores the variances of the variable to be estimated at the target data.
sc_vars	boolean indicating whether vars should be scaled by its observed variance (if available).
var_method	a character representing the method to approximate the variance of the AI estimates. Possible values are "CS" (Cauchy-Schwartz) or "MI" (Moran's I).

Value

the target (of type sf) with estimates of the variables observed at the source data.

Examples

```
data(nyc_surv)
data(nyc_comd)

## creating variables that store the variance for each area
## this is done to exemplify the functionality of the package
nyc_surv <- transform(nyc_surv,
                      my_var = moe / qnorm(p = .975))
nyc_surv <- transform(nyc_surv, my_var = my_var * my_var)

## Not run:
## areal interpolation
estimate_comd <-
  ai(source = nyc_surv, target = nyc_comd,
     vars = "estimate")

## areal interpolation with uncertainty estimation
estimate_comd <-
  ai_var(source = nyc_surv, target = nyc_comd,
         vars = "estimate", vars_var = "my_var",
         var_method = "MI")

## End(Not run)
```

find_phi

Find phi parameter for the Exponential spatial auto-correlation function

Description

Function designed to find the phi parameter such that the correlation between points within a given distance d is at most a given value.

Usage

```
find_phi(
  d,
  nu,
  kappa,
  mu2,
  family = "matern",
  range = c(1e-04, 1000),
  cut = 0.05
)
```

Arguments

d	maximum distance for spatial dependence equal to cut.
nu	smoothness parameter associated with the Matern cov. function.
kappa	one of the smoothness parameters associated with the Generalized Wendland covariance function
mu2	one of the smoothness parameters associated with the Generalized Wendland covariance function
family	covariance function family, the options are c("matern", "gw", "cs", "spher", "pexp", "gaussian").
range	Minimum and maximum distance to be considered. The default is range = c(1e-04, 1000).
cut	desired spatial correlation at a distance d, the default is cut = .05.

Value

a numeric value indicating the range parameter such that the spatial correlation between two points at distance d is cut.

fit_spm

Fitting an underlying continuous process to areal data

Description

Fitting an underlying continuous process to areal data

Usage

```
fit_spm(x, ...)

## S3 method for class 'spm'
fit_spm(
  x,
  model,
  theta_st,
  nu = NULL,
  tr = NULL,
  kappa = 1,
  mu2 = 1.5,
  apply_exp = FALSE,
  opt_method = "Nelder-Mead",
  control_opt = list(),
  comp_hess = TRUE,
  ...
)
```

```

fit_spm2(
  x,
  model,
  nu,
  tr,
  kappa = 1,
  mu2 = 1.5,
  comp_hess = TRUE,
  phi_min,
  phi_max,
  nphi = 10
)

```

Arguments

x	an object of type <code>spm</code> . Note that, the dimension of <code>theta_st</code> depends on the 2 factors. 1) the number of variables being analyzed, and 2) if the input is a <code>spm</code> object.
...	additional parameters, either passed to <code>optim</code> .
model	a character scalar indicating the family of the covariance function to be used. The options are <code>c("matern", "pexp", "gaussian", "spherical", "gw")</code> .
theta_st	a numeric (named) vector containing the initial parameters.
nu	a numeric value indicating either the ν parameter from the Matern covariance function (controlling the process differentiability), or the "pexp" for the Powered Exponential family. If the <code>model</code> chosen by the user is Matern and <code>nu</code> is not informed, it is automatically set to <code>.5</code> . On the other hand, if the user chooses the Powered Exponential family and do not inform <code>nu</code> , then it is set to <code>1</code> . In both cases, the covariance function becomes the so called exponential covariance function.
tr	tapper range
kappa	$\kappa \in \{0, \dots, 3\}$ parameter for the GW cov function.
mu2	the smoothness parameter μ for the GW function.
apply_exp	a logical scalar indicating wheter the parameters that cannot assume negative values should be exponentiate or not.
opt_method	a character scalar indicating the optimization algorithm to be used. For details, see <code>optim</code> .
control_opt	a named list containing the control arguments for the optimization algorithm to be used. For details, see <code>optim</code> .
comp_hess	a boolean indicating whether the Hessian matrix should be computed.
phi_min	a numeric scalar representing the minimum <i>phi</i> value to look for.
phi_max	a numeric scalar representing the maximum <i>phi</i> value to look for.
nphi	a numeric scalar indicating the number of values to compute a grid-search over <i>phi</i> .

Details

This function uses the `optim` function optimization algorithms to find the Maximum Likelihood estimators, and their standard errors, from a model adapted from. The function allows the user to input the control parameters from the `optim` function through the argument `control_opt`, which is a named list. Additionally, the one can input lower and upper boundaries for the optimization problem, as well as the preferred optimization algorithm (as long as it is available for `optim`). The preferred algorithm is selected by the argument `opt_method`. In addition to the control of the optimization, the user can select a covariance function among the following: Matern, Exponential, Powered Exponential, Gaussian, and Spherical. The parameter `apply_exp` is a logical scalar such that, if set to `TRUE`, the `exp` function is applied to the nonnegative parameters, allowing the optimization algorithm to search for all the parameters over the real numbers.

The model assumes $\text{deqn}\{Y(\mathbf{s}) = \mu + S(\mathbf{s})\}$ at the point level. Where $\text{eqn}\{S \sim \text{GP}(\theta, \sigma^2 C(\|\text{Vert } \mathbf{s} - \text{Vert } \mathbf{s}_2 \text{rVert}; \theta))\}$. Further, the observed data is supposed to be $\text{eqn}\{Y(B) = \text{vert } B \text{rvert}^{-1} \int_{\{B\}} Y(\mathbf{s}) \, \text{d} \mathbf{s}\}$.

Value

a `spm_fit` object containing the information about the estimation of the model parameters.

Examples

```
data(liv_lsoa) ## loading the LSOA data

msoa_spm <- sf_to_spm(sf_obj = liv_msoa, n_pts = 500,
                    type = "regular", by_polygon = FALSE,
                    poly_ids = "msoa11cd",
                    var_ids = "leb_est")

## fitting model
theta_st_msoa <- c("phi" = 1) # initial value for the range parameter

fit_msoa <-
  fit_spm(x = msoa_spm,
         theta_st = theta_st_msoa,
         model = "matern",
         nu = .5,
         apply_exp = TRUE,
         opt_method = "L-BFGS-B",
         control = list(maxit = 500))

AIC(fit_msoa)

summary_spm_fit(fit_msoa, sig = .05)
```

goodness_of_fit	<i>Akaike's (and Bayesian) An Information Criterion for spm_fit objects.</i>
-----------------	--

Description

Akaike's (and Bayesian) An Information Criterion for spm_fit objects.

Usage

```
## S3 method for class 'spm_fit'
AIC(object, ..., k = 2)

## S3 method for class 'spm_fit'
BIC(object, ...)
```

Arguments

object	a spm_fit object.
...	optionally more fitted model objects.
k	numeric, the <i>penalty</i> per parameter to be used; the default 'k = 2' is the classical AIC. (for compatibility with stats::AIC.)

Value

a numeric scalar corresponding to the goodness of fit measure.

liv_lsoa	<i>Liverpool Lower Super Output Area.</i>
----------	---

Description

A dataset containing containing the LSOA's for Liverpool along with estimates for Index of Multiple Deprivation. Data taken from [Johnson et al. 2020](#)

Usage

```
liv_lsoa
```

Format

A sf data frame with 298 rows and 6 variables:

lsoa11cd LSOA code

lsoa11nm LSOA name

male Male population

female Female population

imdscore Index of Multiple Deprivation

area LMSOA area, in km^2

Details

The data was projected to EPSG 27700 and units changed to km

Source

<https://ij-healthgeographics.biomedcentral.com/articles/10.1186/s12942-020-00200-w>

liv_msoa

Liverpool Middle Super Output Area.

Description

A dataset containing containing the MSOA's for Liverpool along with estimates for Life Expectancy at Birth. Data taken from [Johnson et al. 2020](#)

Usage

liv_msoa

Format

A sf data frame with 61 rows and 4 variables:

msoa11cd MSOA code

msoa11nm MSOA name

lev_est Estimated life expectancy at birth, in years

area MSOA area, in km^2

Details

The data was projected to EPSG 27700 and units changed to km

Source

<https://ij-healthgeographics.biomedcentral.com/articles/10.1186/s12942-020-00200-w>

nyc_comd	<i>New York City community districts spatial geometries</i>
----------	---

Description

A dataset containing containing the CD's for New York City.

Usage

nyc_comd

Format

A sf data frame with 71 rows and 3 variables:

boro_cd unique identifier

shape_area Shape Area

shape_length Shape Length

est median income estimated using areal interpolation

se_est standard error associated with the estimates

Details

The data is project using EPSG 4326.

nyc_surv	<i>New York City survey data.</i>
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Description

A dataset containing containing the census tracts for New York City along with estimates for median income and a margin of error for this estimates.

Usage

nyc_surv

Format

A sf data frame with 2128 rows and 5 variables:

GEOID unique identifier

NAME census tract name

variable variable estimated

estimate median income estimate

moe median income estimate margin of error

Details

The data is project using EPSG 4326.

predict_spm	<i>Prediction over the same or a different set of regions (or points).</i>
-------------	--

Description

Realizes predictions that can be useful when researchers are interested in predict a variable observed in one political division of a city (or state) on another division of the same region.

Usage

```
predict_spm(x, ...)

## S3 method for class 'spm_fit'
predict_spm(x, .aggregate = TRUE, ...)

## S3 method for class 'sf'
predict_spm(x, spm_obj, n_pts, type, outer_poly = NULL, id_var, ...)
```

Arguments

x	a sf object such that its geometris are either points or polygons.
...	additional parameters
.aggregate	logical. Should the predictions be aggregated? In case the input is only a "fit" object, the aggregation is made over the polygons on which the original data was observed. In case the input x is composed by sf POLYGONS, the aggregation is made over this new partition of the study region.
spm_obj	an object of either class spm_fit or mspm_fit
n_pts	a numeric scalar standing for number of points to form a grid over the whole region to make the predictions
type	character type of grid to be generated. See st_sample in the package sf.
outer_poly	(object) sf geometry storing the "outer map" we want to compute the predictions in.
id_var	if x is a set of POLYGONS (areal data) instead of a set of points, the id_var is the name (or index) of the unique identifier associated to each polygon.

Value

a list of size 4 belonging to the class spm_pred. This list contains the predicted values and the mean and covariance matrix associated with the conditional distribution used to compute the predictions.

Examples

```

data(liv_lsoa) ## loading the LSOA data
data(liv_msoa) ## loading the MSOA data

msoa_spm <- sf_to_spm(sf_obj = liv_msoa, n_pts = 500,
                    type = "regular", by_polygon = FALSE,
                    poly_ids = "msoa11cd",
                    var_ids = "leb_est")

## fitting model
theta_st_msoa <- c("phi" = 1) # initial value for the range parameter

fit_msoa <-
  fit_spm(x = msoa_spm,
         theta_st = theta_st_msoa,
         model = "matern",
         nu = .5,
         apply_exp = TRUE,
         opt_method = "L-BFGS-B",
         control = list(maxit = 500))

pred_lsoa <- predict_spm(x = liv_lsoa, spm_obj = fit_msoa, id_var = "lsoa11cd")

```

sf_to_spm	<i>single sf to spm</i>
-----------	-------------------------

Description

Transforming a sf into a spm object (Internal use)

Usage

```

single_sf_to_spm(
  sf_obj,
  n_pts,
  type = "regular",
  by_polygon = FALSE,
  poly_ids = NULL,
  var_ids = NULL,
  trunc_d = NULL
)

sf_to_spm(
  sf_obj,
  n_pts,
  type = "regular",
  by_polygon = FALSE,

```

```

    poly_ids = NULL,
    var_ids = NULL,
    trunc_d = NULL
  )

```

Arguments

<code>sf_obj</code>	a sf object s.t. its geometries are polygons.
<code>n_pts</code>	a numeric scalar representing the number of points to create a grid in the study region on which the polygons in <code>sf_obj</code> is observed. Alternatively, it can be a vector of the same length as <code>nrow(sf_obj)</code> . In this case, it generates the given number of points for each polygon in <code>sf_obj</code> .
<code>type</code>	a character indicating the type of grid to be generated. The options are <code>c("random", "regular", "hexagonal")</code> . For more details, see <code>st_sample</code> in the <code>sf</code> package.
<code>by_polygon</code>	a logical indicating wheter we should generate <code>n_pts</code> by polygon or for the <code>n_pts</code> for the whole study region.
<code>poly_ids</code>	a character vector informing the name of the variable in <code>sf_obj</code> that represents the polygons unique identifiers. In case this is not informed, we assume the id of the polygons are given by their row numbers.
<code>var_ids</code>	a scalar or vector of type character indicating the (numerical) variables that are going to be analyzed.
<code>trunc_d</code>	truncation distance for grid points. Consider using half of the maximum distance between polygons

Value

a named list of size 6 belonging to the class `spm`. This list stores all the objects necessary to fit models using the `fit_spm`.

Examples

```

data(liv_lsoa) # loading the LSOA data

msoa_spm <- sf_to_spm(sf_obj = liv_msoa, n_pts = 1000,
                    type = "regular", by_polygon = FALSE,
                    poly_ids = "msoa11cd",
                    var_ids = "leb_est")

```

summary_spm_fit

Summarizing spm_fit

Description

Provides a data.frame with point estimates and confidence intervals for the paramters of the model fitted using the `spm_fit` function.

Usage

```
summary_spm_fit(x, sig = 0.05)
```

Arguments

x	a <code>spm_fit</code> object.
sig	a real number between 0 and 1 indicating significance level to be used to compute the confidence intervals for the parameter estimates.

Value

a `data.frame` summarising the parameters estimated by the `fit_spm` function.

vdl	<i>Voronoi Data Linkage</i>
-----	-----------------------------

Description

Reminder, have to create an example. This will be exported after we submit the paper for publication.

Usage

```
vdl(coords_sf, areal_sf, vars, buff)
```

Arguments

coords_sf	sf POINT target dataset.
areal_sf	sf POLYGON source dataset.
vars	a character representing the variables (observed at the source - polygon) to be estimated at the target data.
buff	scalar numeric. Mostly for internal use.

Value

a `sf` object for the `coords_sf` spatial data set.

vdl_var

Voronoi Data Linkage - Single variable and variance

Description

Reminder, have to create an example. This will be exported after we submit the paper for publication.

Usage

```
vdl_var(coords_sf, areal_sf, res_var, variance, var_method = "CS", buff)
```

Arguments

coords_sf	sf POINT target dataset.
areal_sf	sf POLYGON source dataset.
res_var	a character - the name of the variable in the areal_sf to be estimated in the coords_sf.
variance	a character - the name of the variable variance in the areal_sf to be estimated in the coords_sf.
var_method	a character representing the method to approximate the variance of the AI estimates. Possible values are "CS" (Cauchy-Schwartz) or "MI" (Moran's I).
buff	scalar numeric. Mostly for internal use.

Value

a sf object, containing the id_coords variable and the list_vars for the coords_sf spatial data set.

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